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A stochastic forward-looking model
to assess the profitability and solvency
of European insurers

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Abstract

In this paper, we develop an analytical framework for conducting forward-looking assessments of profitability and solvency of the main euro area insurance sectors. We model the balance sheet of an insurance company encompassing both life and non-life business and we calibrate it using country level data to make it representative of the major euro area insurance markets. Then, we project this representative balance sheet forward under stochastic capital markets, stochastic mortality developments and stochastic claims. The model highlights the potential threats to insurers solvency and profitability stemming from a sustained period of low interest rates particularly in those markets which are largely exposed to reinvestment risks due to the relatively high guarantees and generous profit participation schemes. The model also proves how the resilience of insurers to adverse financial developments heavily depends on the diversification of their business mix. Finally, the model identifies potential negative spillovers between life and non-life business through the redistribution of capital within groups.

Keywords: Financial Stability, Insurance, Interest Rate Risk, Stress Test

JEL Classification: G20, G22, G23

Non-technical Summary

In recent years, the level of interest rates has been declining to historical lows worldwide. This development has given rise to concerns for the stability of the financial system and in particular of insurers due to their exposure to downside risks in a low interest rate environment. Life insurance business – representing the lion's share of the balance sheet for European insurance companies – appears particularly vulnerable to low interest rates due to the extended use of financial guarantees which, in some markets, were massively sold to policyholders in the past and which are now becoming very expensive to fund. European life insurance business has been traditionally characterized by the presence of financial guarantees embedded in the savings products, i.e. a minimum rate of return that is granted to policyholders. In times of low interest rates, this business model might represent not only a threat for the profitability of the insurance companies but it might also endanger their solvency position. Insurance companies tend to allocate large portions of their investment portfolio to bonds in order to replicate their liability portfolio. Thus, as interest rates remain low and the reinvestment risk materializes, the expected return on investments declines, making it more difficult for companies to honour returns guaranteed to policyholders and consequently to generate profits. This effect is also reflected in the valuation of assets and liabilities: under a marked-to-market solvency regime, such as the Solvency II regime in Europe, the decline in interest rates increases the value of both assets and liabilities. However, due to the typical duration mismatch observed in the insurance business, i.e. the duration of liabilities being higher than the duration of assets, the value of liabilities tend to rise more than the value of assets, thereby reducing the market-consistent value of own funds of the company and in turn its solvency level. A comprehensive model that allows for studying the impact of different financial developments on the profitability and solvency of insurance companies or for regular financial stability assessments of the insurance sector is still missing. Within the financial stability mandate of central banks, such analysis appears to be fundamental to better understand the upcoming challenges that insurance companies and the financial system as a whole will have to face in the future. Moreover, in the insurance sector there is the need for models, which allow for timely analysis and the creation of early warning signals. This is a relevant aspect, since the insurance business as a long-term horizon business, tends to display very slow dynamics in which risks materialize only gradually in the balance sheet. Therefore, it is very important to have analytical frameworks which allow for a timely detection of potential downside risks and threats and thereby allow for prompt interventions. The present paper aims at filling this gap.

This paper has a twofold aim: on the one hand, to develop an analytical framework for financial stability analyses in which the effects on the profitability and solvency of the main euro-area insurance markets of different financial market scenarios as well as different features of the balance sheet of insurance companies can be investigated in a forward-looking manner; on the other hand, to conduct a quantitative forward-looking assessment of the effects that a persistent low interest rate

environment has on both the profitability and the solvency of the main euro area insurance sectors. More specifically, in this paper, we model the balance sheet of an insurance company encompassing both life and non-life business and we calibrate it using country level data to make it representative of the major euro area insurance markets. Then, we project this representative balance sheet forward under stochastic capital markets, stochastic mortality developments and stochastic claims. Against this background, this paper proposes an analysis that takes into consideration key elements of the insurance business which vary across markets. We calibrate the insurers balance sheet at country level as to introduce heterogeneity both in the business mix, e.g. life and non-life, and in business practices, e.g. duration mismatches. In fact, a more diversified business portfolio as well as better matching strategies have beneficial effects in terms of risk mitigation, which in turn positively influence both the profitability and the solvency of the insurance company.

The results of this work suggest that under a theoretical scenario featuring a protracted period of low interest rates, insurers more exposed to products with financial guarantees display a marked reduction in both profitability and solvency over time. As expected, we find that the specific local regulation and the applied business practices with respect to certain products (e.g. the minimum return guarantees and duration mismatches) are key drivers of both the profitability and solvency of insurers. Our model also highlights the importance of business portfolio diversification. Indeed, as the business portfolio becomes more diversified and less concentrated on interest rate sensitive business, e.g. financial guarantees, both profitability and solvency improve. The model also displays interesting results when it is extended to the group case, i.e. the insurers balance sheet includes both life and non-life business lines. In fact, under the assumption that within a group, capital can be managed and transferred to different lines of business to improve the solvency situation, negative spillovers may emerge. As the non-life business has in general a limited exposure to financial risk, its profitability and solvency position are less affected by the low interest rate environment, but largely depend on the performance of the underwriting portfolio. However, once we allow for capital redistribution within the group, we can observe how a low interest rate environment might also negatively affect the solvency position of the non-life business due to both lower return on assets and most importantly to capital that is redistributed from the non-life towards life business.

Overall, while keeping in mind that the results are model-specific and dependent on specific assumptions, the presented framework provides a new perspective on the financial stability assessment of insurance sectors, which may help policy authorities to design more effective macro- and micro-prudential policy actions.

1 Introduction

In recent years, the level of interest rates has been declining to historical lows worldwide. This development has given rise to concerns for the stability of the financial system and in particular of insurers due to their exposure to downside risks in a low interest rate environment.¹

Among insurers, life business appears to be the most vulnerable due to the extended use of financial guarantees which, in some markets, were massively sold to policyholders in the past and which are now becoming very expensive to fund. This is due to the fact that typical financial guarantees, in particular minimum guaranteed rates of return, are often set as share of the domestic representative sovereign yield at the time of inception: therefore, the transition from relatively higher interest rates experienced in the past to the current low interest rate environment, increases the value to policyholders of those minimum guaranteed rate of returns sold when interest rates were higher and that still did not come due, and represent a (relatively high) cost for insurers. More specifically, as rates decrease, returns on insurers investments decline and thus the margin between returns on investments and returns to be paid to policy holders gets compressed.

In Europe, life business and in particular traditional life savings products, represent the largest portion of investments for insurance companies: according to [Insurance Europe \(2015\)](#), in 2014 the amount of investments allocated to life business was €8.16 bn, whereas non-life amounted to €1.68 bn, corresponding to 83% and 17% of total investments respectively. Within the life business, more than 80% of premiums still come from traditional life business, i.e. products which risk is borne by shareholders, whereas the remainder stems from unit-linked products, i.e. products which risk is borne by policyholders.² Thus, life business represents the lion's share of the balance sheet for European companies, with traditional life business still playing a prominent role.

European life insurance business has been traditionally characterized by the presence of financial guarantees embedded in savings products, i.e. a minimum rate of return that is granted to policyholders. In times of low interest rates, this business model might represent not only a threat for the profitability of the insurance companies but it might also endanger their solvency position.³ Insurance companies tend to allocate large portions of their investment portfolio to bonds in order to replicate their liability portfolio.⁴ Thus, as interest rates remain low and the reinvestment risk materializes, the expected return on investments declines, making it more difficult for companies to honour returns guaranteed to policyholders and consequently to generate profits. This effect is also reflected in the valuation of assets and liabilities: under a marked-to-market solvency regime, such as the Solvency II (S II) regime in Europe, the decline in interest rates increases the value of

¹See for instance [Berdin et al. \(2015\)](#) and [EIOPA \(2015\)](#). The present paper outlines the model used in [Berdin et al. \(2015\)](#).

²In this context, risk essentially refers to financial risk.

³A study conducted by [Swiss Re \(2012\)](#) highlights how the sensitivity of these products to changes in interest rates appears to be particularly higher in some jurisdictions, such as Germany and Italy, and lower in others such as the U.K. and France.

⁴In 2013, directly held bonds represented 52.3% of total investments ([Insurance Europe, 2015](#)).

both assets and liabilities. However, due to the typical duration mismatch observed in the insurance business, i.e. the duration of liabilities being higher than the duration of assets, the value of liabilities tend to rise more than the value of assets, thereby reducing the market-consistent value of own funds of the company and in turn its solvency level.⁵

As interest rates have fallen to historical lows in recent years, the interest of both academics and policy makers on the resilience of the insurance sector to the low interest rate environment has materially increased, however the existing literature is still scant. Indeed, the works which focus on financial stability issues related to the insurance sector are limited and mostly qualitative.⁶ A first attempt to quantitatively estimate threats to German life insurers due to low interest rates is presented in [Berdin and Gründl \(2015\)](#). The authors propose a model in which insolvency probabilities can be derived. In their framework, a representative balance sheet of a German life insurer under the S II regulatory regime is developed; the analysis allows to observe the evolution of both the profitability and the solvency of the business in the low interest rate environment and the results suggest that there exists a relatively high vulnerability for a sub-set of German life insurers, in particular for those less capitalized.⁷ [Wedow and Kablau \(2011\)](#) using a different approach, study the evolution of the solvency of German life insurance companies. Although the study is based on the Solvency I regime, it confirms that should interest rates remain low, a portion of German life insurer would not been in the position to meet their capital requirement in a 10 year horizon. Similar conclusions were reached by [EIOPA Stress Test \(2014\)](#). The European authority carried out a stress test on the European insurance sector in 2014, in which a large portion of European insurance companies have been tested with respect to their resilience to both instantaneous asset market shocks and a protracted period of low interest rates. Findings confirm that, in a prolonged period of low interest rates, a relatively large portion of insurers would not meet their solvency capital requirements, thereby highlighting the strong reduction in their solvency levels. More recently, [Domanski et al. \(2015\)](#) propose an empirical analysis of the hunt for duration of German life insurers and conclude that, due to the low interest rate environment, German insurers buy more long date bonds to improve their matching strategy thereby further pushing down yield on bonds and, thus, creating a downward spiral which might become a further source of concern.

However, a comprehensive model that allows for studying the impact of different financial developments on the profitability and solvency of insurance companies or for more regular financial stability assessments of the insurance sector is still missing. Within the financial stability mandate of central banks, such analysis appears to be fundamental to better understand the upcoming challenges that insurance companies and the financial system as a whole will have to face in the future. Moreover, in the insurance sector there is the need for models, which allow for timely analysis

⁵In this context, duration refers to the Macaulay duration, i.e. the time weighted present value stream of future cashflows of a financial instrument ([Macaulay, 1938](#)).

⁶See among others [Tower and Impavido \(2009\)](#) and [Antolin et al. \(2011\)](#).

⁷The focus on the German life insurance industry is justified by the combination of very low rates on sovereign yields, which represent a large portion of bond holdings of German insurers, and relatively high existing guarantees in the back book.

and the creation of early warning signals. This is a relevant aspect, since the insurance business as a long-term horizon business, tends to display very slow dynamics in which risks materialize only gradually in the balance sheet. Therefore, it is very important to have analytical frameworks which allow for a timely detection (*forward-looking*) of potential downside risks and threats and thereby allow for prompt interventions. The present paper aims at filling this gap.

Thus, the present paper has a twofold aim: on the one hand, to quantitatively estimate the impact that a persistent low interest rate environment has on both the solvency and the profitability of the 5 biggest euro-area insurance markets in terms of total gross written premiums, i.e. Germany, France, Italy, the Netherlands and Spain⁸; on the other hand, to create an analytical tool for financial stability analyses in which the effects of different financial market scenarios as well as different features of the balance sheet of insurance companies, such as business mix, dividend payout policies and pricing policies can be investigated. The focus on both the profitability and solvency is essential to assess the stability of the insurance industry and of the financial system at large.⁹ In addition, this paper proposes an analysis that takes into consideration key elements of the insurance business which vary across markets. Indeed, in this paper, we calibrate the insurer's balance sheet at country level as to introduce heterogeneity both in the business mix, e.g. life and non-life, and in business practices, e.g. duration mismatches. In fact, a more diversified business portfolio as well as better matching strategies, have beneficial effects in terms of risk mitigation, which in turn positively influence both the profitability and the solvency of the insurance company.¹⁰ To the best of our knowledge, this is the first model which attempts to replicate all main features of the balance sheet of an insurance group, active in both the life and non-life businesses, and that can be calibrated to analyse the interplay of different aspects of the insurance business.¹¹

The results of this work suggest that under a theoretical scenario featuring a protracted period of low interest rates, insurers more exposed to products with financial guarantees display a marked reduction in both profitability and solvency over time. As expected, this work finds that the specific local regulation together with the applied business practices with respect to certain products (e.g. the minimum return guarantees and duration mismatches) are key drivers of both the profitability and solvency of insurers. Among the countries considered in the analysis, Germany appears to be the most exposed to a protracted period of low interest rates, due to both its relatively high level of outstanding guarantees and a more generous profit participation mechanism. However, under a severely adverse scenario coupling low interest rates with higher financial markets volatility, the

⁸See [Insurance Europe \(2015\)](#).

⁹In fact, low interest rates in presence of minimum guaranteed rate of returns might create incentives for excessive risk taking behaviour of managers and thereby create instability in the financial system. In the literature, this is commonly referred as the risk of *gambling for redemption* or *search for yield*, see for instance [Rajan \(2005\)](#) and [Antolin et al. \(2011\)](#). Moreover, recent empirical evidence suggests that long-term investors, such as life insurers and pension funds, reacted to the current low interest rate environment by increasing their risk taking behaviour, i.e. increasing the riskiness of the asset allocation, see for instance [Joyce et al. \(2014\)](#).

¹⁰For a discussion on insurance groups, see for instance [Schlütter and Gründl \(2012\)](#).

¹¹Indeed, the present framework can be used to analyse a wide range of important aspects of the insurance business, such as pricing/competition, demand for new products, lapse ratios, etc.

model shows that Italy and Spain display a very high volatility in their solvency ratios mainly due to home bias in their asset allocations. Finally, our model highlights the importance of business portfolio diversification. Indeed, as the business portfolio becomes more diversified and less concentrated on interest rate sensitive business, e.g. financial guarantees, both profitability and solvency improve. The model also displays interesting results when it is extended to the group case, i.e. the insurers balance sheet includes both life and non-life business lines. In fact, under the assumption that within a group, capital can be managed and transferred to different lines of business to improve the solvency situation, negative spillovers may emerge. As the non-life business has in general a limited exposure to financial risk, its profitability and solvency position are less affected by the low interest rate environment, but largely depend on the performance of the underwriting portfolio. Thus, once we allow for capital redistribution within the group, we can observe how a low interest rate environment might also negatively affect the solvency position of the non-life business due to capital that is redistributed from the non-life towards life business.¹² This is an innovative contribution to the existing literature on the effects of low interest rates on insurance companies. Indeed, this work provides a new perspective on the financial stability assessment of insurance companies, which may help supervisors and regulators to design more effective micro and macro-prudential policy actions.

The paper is organized as follows: In Section 2 the model and its features are presented: the insurer's asset side and the liability side are described, together with the regulatory constraints and the set of decisions the management faces in every period; In Section 3 the calibration of the different parameters of the model is introduced; In Section 4 the results of the different calibrations and different specifications are illustrated and finally, in Section 5 the main findings are discussed and the analysis is concluded.

2 The Model

2.1 Methodology

The methodology builds on [Berdin and Gründl \(2015\)](#) and [Berdin \(2016\)](#): the model features a representative balance sheet of an insurance group active in both life and non-life business, stochastic developments of financial markets, i.e. stochastic term structure of interest rates, stochastic yield spreads and stochastic stocks and real estate returns, and in addition stochastic developments of mortality and claims for non-life business. The model is then specifically calibrated for each one of the 5 countries of interest (i.e. Germany, France, Italy, the Netherlands and Spain): in particular, we specify different asset allocations, different liability structures and different regulatory requirements with respect to the pertaining legislation.¹³ Moreover, the stochastic developments

¹²Clearly, the opposite might also happen, i.e. capital redistribution from life towards non-life business, in particular when the performance of the underwriting portfolio is poor.

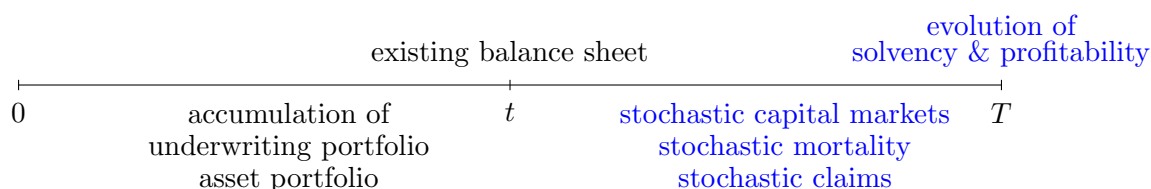
¹³In fact, even though European insurance markets in recent years have been largely harmonized in the light of the recent introduction of S II, some regulatory features still remain different at local level. This is particularly true

of interest rates, stocks and real estate returns, which take into account the correlations among the different processes, are also calibrated at country level. This is a key feature since it allows us to study how diverse developments of these variables across countries differently impact the balance sheet of the insurance company at country level. Ultimately, this reflects part of the heterogeneity across countries, which is an important part of the analysis.

Figure 1 depicts the timeline of the model: we create a balance sheet with an existing back book of contracts and an asset portfolio at time t by accumulating backward in time underwritten contracts (for the liability side) and available coupons (for the asset side). Against this background, we assume that the insurer sold a cohort of contracts each year and depending on the expected time to maturity of the contracts, we accumulate funds using past data on the total return granted to policyholders and the relative guarantee rate, up to the starting point t . In this way, we obtain at time t a fixed number of cohorts of insurance contracts, replicated by cohorts of bonds, each of them sold and bought yearly with a residual time to maturity from 1 year up to their expected time to maturity. See Figure 3. By doing so, we are able to model the legacy business, which is particularly important in life business, since the back book might be a major source of financial distress under certain financial market scenarios.

We then model an insurance group by consolidating the balance sheets of both the life and non-life business under a holding company: we take a simple approach and assume that the holding company fully owns the subsidiaries, i.e. life and non-life subsidiary, and that it has a claim on the free cash flow yearly generated by the subsidiary. The holding company ultimately is responsible for managing capital within the group and to pay out dividends to shareholders. Under certain conditions, the holding company can transfer shares of the generated cash flows to the subsidiary which is experiencing shortages of capital. The underlying assumption, as also highlighted in Schlütter and Gründl (2012), is the possibility of establishing intra-group reinsurance contracts, guarantees, or profit and loss transfer agreements, as well as lines of credit.¹⁴ Figure 4 depicts the group structure and its consolidation within the holding.

Figure 1: The Timeline of the Model



In this work, we specifically focus our attention on the marked-to-market balance sheet according in life business, in which the level of maximum allowed minimum guaranteed return and the level of minimum profit participation are set by the national regulator.

¹⁴A recent article in the German press ([Handelsblatt](#)) reports how many German holding companies are transferring funds to their life business subsidiary through credit lines.

to the S II regulatory regime. Although relevant metrics are at market-consistent values, the book value balance sheet (or historical cost) still plays a role, particularly for life business. In particular, the amount of profits to be distributed to policyholders is computed on the book value balance sheet. Therefore, the book values of relevant items in the balance sheet are also computed. The balance sheet structure of each subsidiary is represented in Figure 2. $A(t)$ and $L(t)$ respectively represent the portfolio of assets and liabilities at market value at time t . The market-consistent value of liabilities is given by $L(t) = L_t^{BE} + RM_t$ where L^{BE} is the sum of the best estimate of contracts and RM is a risk margin for non hedgeable risks.¹⁵

Figure 2: The Balance Sheet of the *life (l) / non-life (nl)* Subsidiary

| Assets | Liabilities |
|--------|-------------|
| $A(t)$ | $OF(t)$ |
| | $L(t)$ |

Finally $OF(t)$ is the market-consistent value of the own funds that the subsidiary can pledge for solvency purposes: under S II, $OF(t)$ must be larger or equal to the $SCR(t)$, where $SCR(t)$ is the solvency capital requirement, i.e. the minimum amount of capital that must be held at single entity level in order to continue operations.¹⁶

2.2 Stochastic Processes

The stochastic processes under consideration are defined on a filtered probability space containing processes for interest rates, stocks and real estate returns, a process for mortality development and the random variable that describes the development of claims. The filtered probability space is defined as $(\Omega, \mathcal{F}, \mathbb{F}, \mathbb{P})$ with filtration $\mathbb{F} = (\mathcal{F}_t)_{t \in [0, T]}$ which represents all the information available up to time $t \in [0, T]$.¹⁷ Against this background, the filtration \mathcal{F} contains the knowledge of the evolution of all state variables up to time t , namely interest rates, stocks and real estate developments, mortality developments and claims developments which are assumed to be independent from each other. Throughout the paper, we specify all processes under the real world probability measure \mathbb{P} .¹⁸ Moreover, we consider a discrete time setting, whereby variables still depend on time

¹⁵We follow the same definitions applied under S II.

¹⁶More precisely, there is a lower level of capital, i.e. the minimum capital requirement (MCR), under which the company ceases its operations.

¹⁷The usual conditions for the filtration are satisfied, i.e. right continuity and $(\mathbb{P}, \mathcal{F})$ - completeness. For further mathematical details see for instance [Shreve \(2004\)](#).

¹⁸ For pricing purposes, we would need to derive risk neutral martingale processes. As this is notoriously a challenging task, for the aim of the present work, we abstain from deriving an appropriate market price of risk.

but are defined within a partition of the time set $[0, T]$. Thus, T represents the number of years considered in the model with t representing $1/T$ of the time set.

2.2.1 Financial Markets Dynamics

In order to simulate the term structure of interest rates, we rely on the model presented by Vasicek (1977).¹⁹ The model introduces the following interest rate dynamics, i.e. a standard Ornstein-Uhlenbeck process, under the risk neutral measure \mathbb{Q}

$$dr(t) = k(\theta - r(t))dt + \sigma_r dW_r^{\mathbb{Q}}(t) \quad (1)$$

where $W_r^{\mathbb{Q}}(t)$ is a standard Brownian motion under \mathbb{Q} , $r(t)$ is the instantaneous interest rate, $k > 0$ is the speed of adjustment, $\theta > 0$ is the mean reversion level and $\sigma_r > 0$ is the volatility of the short rate dynamics. In addition, assuming the absence of arbitrage and a market price of risk $\lambda(t, r)$ of the special form $\lambda(t) = \lambda r(t)$, the short interest rate dynamics under the real world probability measure \mathbb{P} can be written as follows

$$dr(t) = [k\theta - (k + \lambda\sigma_r)r(t)]dt + \sigma_r dW_r^{\mathbb{P}}(t). \quad (2)$$

where $W_r^{\mathbb{P}}(t)$ is a standard Brownian motion under \mathbb{P} . Moreover, the model allows the pricing of a zero coupon bond according to

$$P(t, T) = A(t, T)e^{-H(t, T)r(t)} \quad (3)$$

where t is the time spot and T is the maturity time of the bond. $A(t, T)$ is defined as

$$A(t, T) = e^{\left\{ \left(\theta - \frac{\sigma_r^2}{2k^2} \right) [H(t, T) - T + t] - \frac{\sigma_r^2}{4k} H(t, T)^2 \right\}} \quad (4)$$

and the discount rate $H(t, T)$ is defined as

$$H(t, T) = \frac{1}{k} [1 - e^{-k(T-t)}]. \quad (5)$$

Thus, the model enables us to generate a (quasi) risk free term structure of interest rates²⁰ which we employ both to estimate future bonds' coupons and to determine the market value of assets

¹⁹The Vasicek model is a wide-spread interest rate model. Although its ability to reproduce observed term structure of interest rates has been challenged over the years, it allows, by using an appropriate calibration, to generate term structures of interest rates in which there exists a positive probability of observing negative rates on shorter maturities. This feature is in line with the current environment, in which negative rates have been persistently observed (European Central Bank, 2015).

²⁰By quasi (or alternatively locally) risk free term structure of interest rates, we imply the German term structure of interest rates, which is the safe haven (AAA rated) for capital markets in Europe and often the benchmark curve for bond markets. Of course, the presence of a term premium and a non-zero credit risk justifies the quasi risk free status.

and the market-consistent value of liabilities.²¹ The term structure of interest rates is given by the following equation

$$r_{f(t,T)} = -\frac{\ln(A(t,T))}{T-t} + \frac{H(t,T)}{T-t}r(t) \quad (6)$$

in which T is the maturity of the rate.²² In addition, we assume that risky bonds pay a stochastic premium on the risk free rate of return: for simplicity, we assume that such premium varies across issuers j (each issuer is either a sovereign (g) or a corporate (c)) but remains constant across maturities. Thus, the spread also follows an Ornstein - Uhlenbeck (mean reverting) process, although its distribution is truncated at 0, and it is defined as follows

$$d\delta_{g/c}^j(t) = \left\{ k(\overline{\delta_{g/c}^j} - \delta_{g/c}^j(t))dt + \sigma_{g/c}^j dW_{g/c}^{j,\mathbb{P}}(t) \right\}^+ \quad (7)$$

in which $\overline{\delta_{g/c}^j}$ is the mean reversion level and $\sigma_{g/c}^j$ its standard deviation. Thus, the term structure of risky bonds is given by

$$r_{c/g(t,T)}^j = r_{f(t,T)} + \delta_{g/c}^j(t) \quad (8)$$

which we employ to both value and determine coupons over time.

Stock (s) and Real Estate (re) returns also vary across issuer (j) and evolve over time following a Geometric Brownian Motion (GBM) which is specified as follows

$$dS_{s/re}^j(t) = \mu_{s/re}^j S_{s/re}^j(t) dt + \sigma_{s/re}^j S_{s/re}^j(t) dW_{s/re}^{j,\mathbb{P}}(t) \quad (9)$$

where $\mu_{s/re}^j$ is the drift rate and $\sigma_{s/re}^j$ is the volatility of the return. The solution to equation (9) is given by

$$S_{s/re}^j(t) = S_{s/re}^j(0) e^{\left(\mu_{s/re}^j - \frac{\sigma_{s/re}^j{}^2}{2} \right) t + \sigma_{s/re}^j W_{s/re}^{j,\mathbb{P}}(t)}. \quad (10)$$

Finally, all processes, namely the instantaneous interest rate process of the Vasicek model, stochastic spreads and stock and real estate returns, are correlated through a Cholesky decomposition.²³

2.2.2 Mortality Dynamics

We model the mortality developments using the standard Lee-Carter framework (LC model) with modifications as proposed by [Brouhns et al. \(2002a\)](#). The model specifies the central death

²¹However, the value of liabilities is subject to EIOPA guidelines which prescribe that only the first 20 years have to be considered at market values. Indeed, from the 20th-year maturity onward, rates have to converge to the *Ultimate Forward Rate* which foresees a rate of 4.2% at 60- year maturity.

²²For the sake of clarity, $r_{f(t,T)}$ is the spot risk free rate at time t with maturity T . For further details on the dynamics of the bond pricing equation refer to [Brigo and Mercurio \(2006\)](#) pp.58-62.

²³For more details on the Cholesky decomposition, see for instance [Hull \(2010\)](#) or [Björk \(2004\)](#).

rate or force of mortality $\mu_{x,t}$ as follows

$$\ln[\mu_{x,t}] = a_x + b_x \cdot k_t + \varepsilon_{x,t} \Leftrightarrow \mu_{x,t} = e^{a_x + b_x \cdot k_t + \varepsilon_{x,t}} \quad (11)$$

in which a_x and b_x are time constant parameters for age x that determine the shape and the sensitivity of the mortality rate to changes in k_t which is a time varying parameter capturing the changes in the mortality rates over time. Finally, $\varepsilon_{x,t}$ is a stochastic error term. As originally proposed by [Lee and Carter \(1992\)](#), \hat{a}_x , \hat{b}_x and \hat{k}_t can be estimated using ordinary least square (OLS) and future mortality developments can be projected by fitting the estimated time varying parameter \hat{k}_t to an *ARIMA* model using standard time series analysis techniques.²⁴ The *ARIMA*(p, d, q) process is given by the following equation

$$k_t = (\alpha_0 + \alpha_1 k_{t-1} + \alpha_2 k_{t-2} + \dots + \alpha_p k_{t-p} + \beta_1 \varepsilon_{t-1} + \beta_2 \varepsilon_{t-2} + \dots + \beta_q \varepsilon_{t-q}) + \varepsilon_t = \hat{k}_t + \varepsilon_t \quad (13)$$

in which the error term is defined as follows $\varepsilon \sim N(0, \sigma_k)$.²⁵ [Brouhns et al. \(2002a\)](#) propose a convenient modification of the original LC model: the authors develop a different estimation technique in which the homoscedasticity of errors, necessary to perform standard OLS estimations, can be released. They propose to model the realized number of deaths at age x and time t as follows

$$D_{x,t} \sim \text{Poisson}(E_{x,t} \cdot \mu_{x,t}) \Leftrightarrow D_{x,t} \sim \text{Poisson}(E_{x,t} \cdot e^{a_x + b_x \hat{k}_t}) \quad (14)$$

in which \hat{k}_t is the forecasted time varying parameter used to simulate random death rates (unsystematic mortality risk) and $E_{x,t}$ is the risk exposure at age x and time t defined as

$$E_{x,t} = \frac{n_{x-1,t-1} + n_{x,t}}{2} \quad (15)$$

in which $n_{x,t}$ is the number of living persons aged x at the end of year t . Parameters \hat{a}_x , \hat{b}_x and \hat{k}_t in [Brouhns et al. \(2002a\)](#) are estimated by maximizing the log-likelihood function based on eq. (14) which is given by the following expression

$$\mathcal{L}(a, b, k) = \sum_{x,t} \{D_{x,t}(a_x + b_x \cdot k_t) - E_{x,t} e^{a_x + b_x \cdot k_t}\} + c \quad (16)$$

²⁴The estimation procedure is more complex than a standard OLS since it relies on singular value decomposition technique. In general, the estimated parameters are such that they minimize the following expression

$$\sum_{x,t} (\ln[\widehat{\mu_{x,t}}] - a_x - b_x \cdot k_t)^2. \quad (12)$$

For more details refer to [Brouhns et al. \(2002a\)](#).

²⁵The term d indicates the grade of cointegration of the series. For further mathematical details refer to [Brockwell and Davis \(2009\)](#) pp. 273-320.

in which c is a constant. Moreover, [Brouhns et al. \(2002b\)](#) propose a transformation of (15) for simulation purposes as follows

$$E_t^i = \frac{-n_{t-1}^i q_t^i}{\ln(p_t^i)} \quad (17)$$

in which n^i is the reference population of the i^{th} cohort of policyholders and q_t^i and p_t^i are the (random) death and living probability given by the simulation of μ_t^i .²⁶ Thus, the number of living individuals for each cohort is given by

$$n_t^i = n_{t-1}^i - d_t^i \quad (18)$$

in which d_t^i is the simulated number of deaths. This is obtained by simulating a random draw from a Poisson distribution with $\lambda = E_t^i \cdot \mu_t^i$, in which E_t^i is the exposure to risk of the i^{th} cohort and μ_t^i is the simulated mortality rate (see 14). To simulate μ , we model different realizations of the time trend k_t in presence of noise. Formally, this is given by the following equation

$$k_t = \widehat{k}_t + \varepsilon_t \quad (19)$$

in which \widehat{k}_t is the expected time trend and $\varepsilon_t \sim (0, \sigma_k)$. The insertion of an error term allows for systematic changes in the mortality dynamics, i.e. the undiversifiable mortality risk.²⁷

2.2.2.1 Adverse Selection

In the context of life insurance business and in particular in presence of annuity business, a well-known problem regarding the self-selection of longer living individuals has to be addressed.²⁸ In [Brouhns et al. \(2002a\)](#) a model to quantify the impact of this phenomenon is presented: a Brass-type relational model defines the mortality rate of the pool of annuitants as a function of the mortality rates of the population. This is given by the following relation

$$\ln[\mu_t^{i,as}] = \phi_1 + \phi_2 \ln[\mu_t^i] \quad (20)$$

in which the term ϕ_2 reflects the speed of improvement in the mortality rates. [Gatzert and Wesker \(2012\)](#) insert a second term using a time index with the intent of reducing the speed of improvement as time goes by. Thus, the resulting relation is given by the following equation

$$\ln[\mu_t^{i,as}] = \phi_1 + \phi_2 \ln[\mu_t^i] + \phi_3 (\ln[\mu_t^i] \cdot \tau_{index}) \quad (21)$$

²⁶Please note that in our model we define i the cohort of policyholders which is equivalent to the specification x for the age of the population, since all cohorts of individuals enter the balance sheet at the same age and remain for an equal fixed period.

²⁷See for instance [Wills and Sherris \(2010\)](#), [Hanewald et al. \(2013\)](#) and [Gatzert and Wesker \(2012\)](#).

²⁸On a formal investigation of the problem, see among others [Finkelstein and Poterba \(2004\)](#).

where $\phi_3 < 0$ and τ_{index} is a linear time index which gives more weight to coefficient ϕ_3 as time goes by. Finally, in order to simulate the mortality developments of the annuitants population, we rewrite (21) as follows

$$\ln[\mu_t^{i,as}] = \phi_1 + \phi_2 \ln[\mu_t^i] + \phi_3(\ln[\mu_t^i] \cdot \tau_{index}) + \varepsilon_t \quad (22)$$

with $\varepsilon_{x,t} \sim N(0, \sigma_k)$.

2.2.3 Claims Developments

We take a simple approach for the stochastic development of claims: we assume that they evolve according to a log-normal distribution, which is known ex-ante and remains unchanged over time.²⁹ This simplification allows us to introduce uncertainty as well as fat tail results, both typical features of non-life claims. Thus, at every point in time t , claims in country j are a random draw from the following distribution

$$C^j(t) = \mathcal{LN}(\mu_C^j, \sigma_C^j) \quad (23)$$

which has the following arithmetic moments

$$\mathbb{E}[C^j] = e^{\mu_C^j + \frac{1}{2}\sigma_C^{j2}} \quad \text{Var}(C^j) = (e^{\sigma_C^{j2}} - 1)e^{2\mu_C^j + \sigma_C^{j2}}. \quad (24)$$

To be more precise, we define C as an index with expected value fixed at 1, i.e. $\mathbb{E}[C^j] \stackrel{!}{=} 1$ and consequently $\mu_C^j + \frac{1}{2}\sigma_C^{j2} \stackrel{!}{=} 0$, which determines in every period the amount of cash-outflows generated by outstanding claims when multiplied by the amount of premiums collected in the previous period.

2.3 Life Business

We model 2 main types of business at shareholders' risk: *endowment/annuity business* and *term life business*. Both are modelled as standard contracts sold yearly to a cohort of policyholders in country j . Endowment/annuity business represents a traditional savings product through which policyholders accumulate funds over a pre-defined period of time and then either get a lump sum payment at the end of the period or annuitize the accumulated wealth. The contract entails *i)* a fixed time to maturity, *ii)* a minimum guaranteed rate of return, *iii)* a minimum profit participation, *iv)* yearly premiums with a loading, *v)* early death benefits (at discount) and *vi)* the opportunity for a share θ^a of the living policyholders at maturity to annuitize the accumulated funds and get life-long benefit payments. By contrast *term life business* only offers protection against early death:

²⁹In the literature it is often assumed that claims develop following a GBM, see for instance [Gatzert and Schmeiser \(2008a\)](#) and [Gatzert and Schmeiser \(2008b\)](#): however, in a multi-period setting as the one in the present model, the volatility of claims that follow a GBM would tend to compound over time leading to very unstable developments with very high insolvency probabilities for insurers. Such feature would not be in line with observed claims developments.

it entails *i*) a fixed time to maturity, *ii*) yearly premiums with loadings and *iii*) benefits liquidated as lump sum contingent on death.³⁰

2.3.1 The Asset Side

We assume that at each point in time, the insurer invests in 4 asset classes, namely *sovereign bonds*, *corporate bonds*, *stocks* and *real estate*, all kept in fixed proportions (static asset allocation), namely ω^{sb} , ω^{cb} , ω^s , ω^{re} .³¹ The asset allocation is then subject to the following conditions $\sum_j \omega^j = 1 \wedge \omega^j \geq 0$ for $j = sb, cb, s, re$.

Bond-like asset classes are divided in sub-portfolios: 5 sub-portfolios for sovereign bonds, i.e. 1 per each of the countries considered in the model, in which each sub-portfolio comprises 20 coupons (20 YTM), with residual time to maturity from 1 to 20; 4 sub-portfolios for corporate bonds, i.e. ratings from AAA to BBB, in which each sub-portfolio comprises 10 coupons (10 YTM), each with residual time to maturity from 1 to 10. This portfolio structure is chosen in order to constantly keep a fixed number of coupons in the portfolio which serve as an approximation for a weighted average of available coupons in the market. The weights associated to each coupon are chosen to match the available average modified duration data. A natural implication of this approach is the presence in the portfolio of coupons bought at different point in time, which are then marked to market and subject to changes in their market value due to movements of the term structure of interest rates. For Stock-like asset classes we follow a similar approach: the stock portfolio comprises stock returns from country specific stock indexes, which can be thought as country specific portfolios; the same holds for the real estate portfolio, which comprises real estate returns from country specific real estate indexes. Moreover, weights within portfolios are chosen to reflect home bias.³² Finally the total market value of assets at time t is define as $A(t)^l$.

The price of a bond of the j^{th} issuer with residual time to maturity τ with payoff vector c which pays 1 unit at maturity is given by the following equation

$$P_t^{j,\tau} = c_t^{j,\tau} \cdot m_t^{j,\tau} \quad (25)$$

in which, recalling 2.2.1, m is the vector of stochastic discount factors; more precisely, we can

³⁰Please note that throughout the paper, we refer to premiums as *net* premiums, which together with *loadings* result in gross premiums.

³¹These represent the most common securities held by insurers, see [EIOPA Stress Test \(2014\)](#).

³²When calibrating the model, we give more weight to the domestic index with respect to the indexes of the other countries, i.e. we assign a higher coefficient within the portfolio to the index representing the home country, whereas all other indices are given the same lower coefficient (see Section 3). This is a typical feature of investors, see for instance [Kenneth and Poterba \(1991\)](#).

express c and m as follows³³

$$c_t^{j,\tau} = [c_t^{j,1}, \dots, c_t^{j,\tau} + 1], \quad m_t^{j,\tau} = \begin{bmatrix} e^{-(r_{f(t,1)} + \delta_t^j) \cdot 1} \\ \cdot \\ \cdot \\ \cdot \\ e^{-(r_{f(t,\tau)} + \delta_t^j) \cdot \tau} \end{bmatrix}. \quad (26)$$

Thus, the value of each bond portfolio is given by the following equation

$$B_t^{sb/cb} = A(t)^l \cdot \underbrace{\omega_t^{sb/cb}}_{class} \cdot \underbrace{\sum_{j=1}^N \omega^j}_{issuer} \cdot \underbrace{\sum_{\tau=1}^T \omega_t^{j,\tau}}_{time\ to\ maturity} \quad (27)$$

in which $\omega_t^{j,\tau}$ is the share of issuer j , i.e. country j in the case of sovereign, rating j in the case of corporate, with residual time to maturity τ which is yearly adjusted to reach the target duration.³⁴ More precisely, we can represent the relative weight of each coupon as follows

$$(sb) \Rightarrow \omega^j : \begin{bmatrix} \omega^{DE} \\ \omega^{FR} \\ \omega^{NL} \\ \omega^{IT} \\ \omega^{ES} \end{bmatrix}, \quad (cb) \Rightarrow \omega^j : \begin{bmatrix} \omega^{AAA} \\ \omega^{AA} \\ \omega^A \\ \omega^{BBB} \end{bmatrix}, \quad s.t. \mathbf{1}'\omega^j = 1 \wedge \omega^j \geq 0, \quad j = DE, \dots, BBB \quad (28)$$

and the relative weight yearly adjusted to keep the modified duration constant

$$\omega_t^{j,\tau} : \begin{bmatrix} \omega_t^{j,d_1} \\ \cdot \\ \cdot \\ \cdot \\ \omega_t^{j,d_n} \end{bmatrix}, \quad s.t. \mathbf{1}'\omega^{j,\tau} = 1 \wedge \omega^{j,\tau} \geq 0, \quad \tau = d_1, \dots, d_n. \quad (29)$$

Finally, once we have the share of the portfolio we allocate to each single bond and its price, it is easy to derive the amount of notional to be bought and the relative generated cash flows.³⁵

The stock and real estate portfolio have similar characteristics: the value of each portfolio is

³³The superscript τ indicates the residual time-to-maturity of the bond. Similarly, c and m are vectors with τ elements and carry the same superscript. More formally, the last element of these vectors, i.e. the last coupon and the principal for vector c and the discount factor with the same residual time-to-maturity for vector m , carry the same superscript τ , i.e. $c_t^{j,\tau} + 1$ and $e^{-(r_{f(t,\tau)} + \delta_t^j) \cdot \tau}$ in which τ is also the compounding factor (i.e. remaining years).

³⁴See Appendix A.3.

³⁵For instance, given $B^{sb/cb,j}$, i.e. the value of the bond sub-portfolio sb/cb issued by j , we know that the value allocated to each bond is given by $B^{sb/cb,j} \cdot \omega_t^{j,\tau}$ and therefore the quantity of unit bonds held in portfolio is given by $F^{sb/cb,j,\tau} = \frac{B^{sb/cb,j} \cdot \omega_t^{j,\tau}}{P^{sb/cb,j,\tau}}$ where F is the notional of the bond paying the coupon c .

given by the following equation

$$S_t^{s/re} = A(t)^l \cdot \omega^{s/re} \cdot \sum_{j=1}^N \omega_t^j \quad (30)$$

$$s.t. \mathbf{1}'\omega^j = 1 \wedge \omega^j \geq 0, \quad j = DE, \dots, ES \quad (31)$$

in which ω^j represents the weight allocated to issuer j , i.e. country. Stocks and real estate pay yearly contingent dividends/rents which are computed as follows

$$d_{t+1}^{j,s/re} = \psi^{s/re} \cdot \left\{ S_{t+1}^{*j,s/re} - S_t^{*j,s/re} \right\}^+ \quad (32)$$

in which $\psi^{s/re} \leq 1$ determines how much of the marginal growth is cashed in as dividend/rent and S^* is the index representing the dynamics of s/re of the j issuer. Finally, dividends and rents are subtracted to the value of each stock-like asset class which is given by the following equation

$$S_{t+1}^{j,s/re} = S_t^{j,s/re} \cdot e^{\left(\mu_{s/re}^{*j} - \frac{\sigma_{s/re}^{*j}{}^2}{2} + \sigma_{s/re}^{*j} dW_{s/re}^{*j,\mathbb{P}} \right)} - d_{t+1}^{j,s/re}. \quad (33)$$

2.3.2 The Liability Side

At each point in time a cohort of n^i individuals aged x buy a contract with annual (net) premium π , with an accumulation period of T years and hold it until maturity.³⁶ Thus, at each point in time the insurer has $N^l(t)$ cohorts of contracts in its balance sheet. On top of the premium, i.e. the amount that gets accumulated in the policyholder's account in case of endowment/annuity products or the amount used for actuarial calculations in case of term life products, the insurer charges a loading factor $\varrho^l \geq 0$ which is the same for every cohort and every type of product.³⁷ For endowment/annuity products, once the accumulation phase is terminated, a fraction $0 \leq \theta^a \leq 1$ of the living policyholders decide to annuitize the accumulated funds $n_t^{a,i} = \theta^a \cdot n_t^i$, whereas the remainder $n_t^{e,i} = (1 - \theta^a) \cdot n_t^i$ receive a lump sum payment equal to the accumulated funds. As policyholders decide to annuitize their wealth, the total number of cohorts simultaneously present in the balance sheet, N_t , grows over time. To be more precise, $N^{l,e}$ and $N^{l,tl}$ remain fixed, whereas $N_t^{l,a}$ is time dependent and grow over time. The insurer charges an additional loading factor to those who decide to annuitize: policyholders pay a loading factor out of the benefits, i.e. $mw = 1 - \varrho$ in which mw is the ratio of the present discount value of the expected annuity payments to the price (Cannon and Tonks, 2008).³⁸ Payments of both premiums and benefits are made in arrears,

³⁶We drop the superscript j which indicates the country in order to simplify the notation.

³⁷Operational costs are not modeled, therefore the loading factor ϱ can be thought of either as a markup on top of the marginal cost of insuring (which could be a function of the market power of the company) or as a reward (risk premium) for systematic mortality risk.

³⁸The loading factor is additional in the sense that it comes on top of the loading factors applied to expected mortality probabilities. In fact, it is common practice to load mortality probabilities in order to factor in potential

i.e. at the end of each year. In case death occurs before T for endowment products, policyholders receive a fraction $\vartheta \leq 1$ of the accumulated funds, i.e. a recovery value.

We define the aggregate value of the liability side of the balance sheet as the sum of endowment policies, annuities and term life policies: ω_t^e , ω_t^a and ω_t^{tl} represent the share of each type of business in the liability portfolio.³⁹ More formally, this can be expressed as follows

$$L(t)^l = \sum_{i=1}^{N^{l,e}} n^{e,i}(t) \cdot l^{e,i}(t) + \sum_{i=1}^{N^{l,a}} n^{a,i}(t) \cdot l^{a,i}(t) + \sum_{i=1}^{N^{l,tl}} n^{tl,i}(t) \cdot l^{tl,i}(t) \quad (34)$$

in which $l^{e,i}$ is the market-consistent value of the i^{th} cohort of contracts expected to be liquidated at the end of the period (i.e. endowment policies), $l^{a,i}$ is the market-consistent value of the i^{th} cohort of contracts expected to be annuitized and $l^{tl,i}$ is the market-consistent value of term life contracts.

In order to compute the market-consistent value, the book value technical reserves must also be computed at each point in time: thus, the aggregate value of the technical reserves, i.e. the simplified book value, can be expressed as follows

$$V(t) = \sum_{i=1}^{N^{l,e}} n^{e,i}(t) \cdot v^{e,i}(t) + \sum_{i=1}^{N^{l,a}} n^{a,i}(t) \cdot v^{a,i}(t) + \sum_{i=1}^{N^{l,tl}} v^{tl,i}(t) \quad (35)$$

in which $v^{e,i}$, $v^{a,i}$ and $v^{tl,i}$ represent the book value technical reserves for the contracts during the accumulation and decumulation phase (if annuitized) respectively. The amount of technical reserves is particularly important for savings products (endowments/annuities) since the computation of the amount of profits which need to be shared with policyholders every year is based on book value technical reserves.

2.3.2.1 The Book Value of Liabilities

Endowment/Annuity business

We first define the dynamics of the policyholders' accounts for the accumulation and decumulation phase: both endowment and annuities entail a profit sharing mechanism, through which during the accumulation phase, the distributed profits increase either the sum insured (i.e. the accumulated funds) or the yearly benefits for those who annuitize the distributed profits are liquidated every year and thereby increase the yearly benefits. Such mechanism implies that the amount of benefits to be paid out during the decumulation phase might vary according to both the dynamics of the asset return of the portfolio backing the liabilities and the dynamics of the mortality of the

deviations from unsystematic mortality.

³⁹Similar to the asset portfolio, the following conditions apply: $\sum_j \omega^j = 1 \wedge \omega_t^j \geq 0$ for $j = e, a, tl$.

underwriting portfolio. Thus, the dynamics is given by the following recursive equations

$$\begin{cases} n_t^{e,i} \cdot v_t^{e,i} = n_t^{e,i} \cdot \left[v_{t-1}^{e,i} (1 + r_t^{g,i}) + \pi_t^i \right] - (\vartheta + v^q (1 - \vartheta)) v_{t-1}^{e,i} \cdot d_t^i, & t : [1, T], \text{ accumulation} \\ n_t^{a,i} \cdot v_t^{a,i} = n_t^{a,i} \cdot v_{t-1}^{a,i} (1 + r^i) - b^i n_t^{a,i}, & t : [T + 1, \omega - x], \text{ annuitization} \end{cases} \quad (36)$$

in which b^i are the life long benefits paid out to living policyholders, $d_t^i = n_{t-1}^{e,i} - n_t^{e,i}$, $v_0^{e,i} = 0$, ${}_0p_x = 1$ and $q_\omega = 1$.⁴⁰ The return yearly granted to policyholders, i.e. $r_t^{g,i}$ is determined by the following condition

$$r_t^{g,i} = r^i + (v^a \cdot r_t^a - r^i)^+ + (v^q \cdot r_t^q)^+ \quad (37)$$

in which r_t^a is the rate of return of the insurers's asset portfolio at time t , r_t^q is the rate of return stemming from the actual mortality developments and $v^{a/q} \in [0, 1]$ is an exogenous constant through which the regulator forces insurers to distribute a minimum amount of financial and mortality returns to policyholders.⁴¹ More formally, r_t^a is given by

$$r_t^a = \frac{\sum_{j=1}^N \sum_{\tau=1}^T c_t^{j,\tau, sb} + \sum_{j=1}^N \sum_{\tau=1}^T c_t^{j,\tau, cb} + \sum_{j=1}^N d_t^{j,s} + \sum_{j=1}^N d_t^{j,re}}{A_t^{bv}} \quad (38)$$

the sum of coupons, bonds due and dividends and rents computed on the book value of assets.⁴² Profits from mortality developments come from two sources and can be summarized as follows

$$\begin{cases} (1 - \vartheta) \cdot v_{t-1}^{e,i} (\tilde{q}_t^i - \bar{q}_t^i), & \text{for } t \leq T, \text{ accumulation} \\ v_t^{a,i} \cdot (\bar{q}_t^i - \tilde{q}_t^i), & \text{for } t > T, \text{ decumulation} \end{cases} \quad (39)$$

in which \tilde{q}_t^i is the observed (stochastic) mortality of the i^{th} cohort determined as $\tilde{q}_t^i = \frac{\bar{n}_{t-1}^i - \bar{n}_t^i}{\bar{n}_{t-1}^i}$ whereas \bar{q}_t^i is the expected mortality probability used to compute the necessary reserves.⁴³ The

⁴⁰See Appendix A.1 For further mathematical details see Pitacco et al. (2009), pp.8 - 16.

⁴¹However, it is worth remarking that the way yearly returns are credited to policyholders varies across countries: some countries have strict regulations regarding the profit participation mechanism (e.g. Germany) while others do not have a specific regulation on the profit participation (e.g. the Netherlands). In particular, in many countries v is set by the regulator and it represents the minimum share of profits that must be credited to the policyholders' accounts, although such share of profits might differ for financial and mortality returns. Since we calibrate the model for different countries, we take into consideration the peculiarities of each underlying local regulatory regime and we provide an overview in Appendix A.6.

⁴²Analogously to the book value of liabilities, we also compute the book value of assets in each period: although we focus on the market value of assets, we indirectly derive historical costs by approximating the book value to the face value and update them yearly.

⁴³We load the underlying probability distribution of mortality according to the German Actuarial Association (DAV) guidelines and thereby compute the necessary reserves to hold in the balance sheet. We keep such loading equal across countries. See Table 9.

return on mortality is then computed as follows

$$r_t^q = \frac{\sum_{i=1}^{N_{t-1}^{l,e}} (1 - \vartheta) \cdot v_{t-1}^{e,i} \cdot (\tilde{q}_t^i - \bar{q}_t^i) + \sum_{i=1}^{N_{t-1}^{l,a}} v_t^{a,i} \cdot (\tilde{q}_t^i - \bar{q}_t^i)}{V_{t-1}}. \quad (40)$$

Finally, the book value for endowment/annuity liabilities is determined as the expected amount of funds to be paid in the future discounted at the technical interest rate r^i . More formally, for the endowment contract this is given by the following equation

$$\bar{v}_t^{e,i} = v_t^{e,i} \cdot \left[\sum_{s=0}^{T-t-1} (\vartheta + v^q(1 - \vartheta)) \cdot \frac{(1 + r^i)^s \cdot s\bar{p}_t^i \cdot \bar{q}_{t+s}^i}{(1 + r^i)^s} + \frac{(1 + r^i)^{T-t} \cdot T\bar{p}_t^i}{(1 + r^i)^{T-t}} \right] \quad (41)$$

$$= v_t^{e,i} \cdot \left[\sum_{s=0}^{T-t-1} (\vartheta + v^q(1 - \vartheta)) \cdot s\bar{p}_t^i \cdot \bar{q}_{t+s}^i + T\bar{p}_t^i \right] \quad (42)$$

in which $v_t^{e,i}$ are the accumulated funds at time t and \bar{p} and \bar{q} represent the surviving and mortality probability used for pricing purposes, with ${}_0\bar{p}_t^i = 1$.⁴⁴ It is worth remarking that the technical interest rate is indeed the guaranteed rate of return: by discounting with the rate r^i , the insurer explicitly assumes that the paid premiums will at least grow in the policyholder's account at the rate r^i and thereby provides a minimum guaranteed rate of return. Thus the book value of the contract is approximated as the mortality weighted current level of the policyholders' account diminished by the recovery value ϑ and also by the amount of returns that are given back to policyholders v^q .⁴⁵

Finally, for the annuity contract this is simply given by

$$\begin{cases} n_t^{a,i} \cdot v_t^{a,i} = mw \cdot n_t^{a,i} \cdot v_t^{e,i}, & t = T + 1 \\ n_t^{a,i} \cdot v_t^{a,i} = n_t^{a,i} \cdot v_{t-1}^{a,i} (1 + r^i) - b^i n_t^{a,i}, & t > T + 1 \end{cases} \quad (43)$$

in which mw is the money's worth ratio of the annuity contract and b are the yearly benefits of the annuity.⁴⁶

Term Life business

The book value for term life liabilities is also determined as the expected amount of funds to be paid out in the future discounted at the technical interest rate r^i . More formally, this is given by

$$v_t^{tl,i} = \sum_{s=0}^{T-t-1} \frac{DB^i \cdot s\bar{p}_t^i \cdot \bar{q}_{t+s}^i}{(1 + r^i)^{(s+1)}} - \frac{\pi^i \cdot s\bar{p}_t^i}{(1 + r^i)^s} \quad (44)$$

⁴⁴More formally, the expression introduces the conditional surviving probability which is given by the following expression ${}_T\bar{p}_t^i = \prod_{s=t}^T \bar{p}_s^i$, i.e. the probability that a $x + t$ year old individual survives for the next T years.

⁴⁵To be more precise, a v^q share of the amount $1 - \vartheta$ has to be given back to the survived policyholders, therefore the value that has to be booked as reserve in the balance sheet, i.e. paid out to policyholders in the future, is given by $\vartheta + v^q(1 - \vartheta)$.

⁴⁶See Appendix A.1.

in which DB are the actuarially fair benefits.⁴⁷

2.3.2.2 The Market Value of Liabilities

Endowment/Annuity business

At time t , the insurer computes the best estimate of its liabilities taking into account the guaranteed rate of return, the expected profit sharing dynamics and discounts the terminal value using the risk free rate term structure. This computation is close but not equivalent to a fair valuation of the contract, which would, however, require additional distributional assumptions (i.e. simulations) regarding the evolution of the asset side return, the mortality developments and the dynamics of the risk free term structure. Thus, for computational reasons, we abstain from such stochastic valuation and rely on an approximate computation of the best estimates.⁴⁸ The market consistent value of the endowment contract at time t is approximated by the following equation

$$l_t^{e,i} = v_t^{e,i} \cdot \left[\sum_{s=0}^{T-t-1} (\vartheta + v^q(1-\vartheta)) \cdot \frac{(1 + \{r^i, \hat{r}_{s+1}^g\}^+)^s \mathbb{E}[{}_s p_t^i] \cdot \mathbb{E}[q_{t+s}^i]}{(1 + r_{f(t,s+1)})^s} + \frac{(1 + \{r^i, \hat{r}_{s+1}^g\}^+)^{(s+1)} \cdot \mathbb{E}[{}_{s+1} p_t^i]}{(1 + r_{f(t,s+1)})^{(s+1)}} \right] \quad (45)$$

in which $\mathbb{E}[p_t]$ and $\mathbb{E}[q_t] = 1 - \mathbb{E}[p_t]$ are the expected mortality developments computed according to the expected mortality trend \hat{k}_t ,⁴⁹ and \hat{r}_{s+1}^g is a vector containing the expected future rate of return stemming from the profit sharing mechanism which value depends on the information set available at time t , i.e. from the observed rate of return granted to policyholders in the past.⁵⁰

For the annuity contract, the market consistent valuation has also to take the decumulation phase into consideration. Thus, the market consistent value of the annuity contract at time t is approximated by the following equation

$$l_t^{a,i} = \begin{cases} l_t^{e,i} - \left\{ l_t^{e,i} - \underline{b}_t^i \cdot \sum_{s=T+1}^{\omega-x} \frac{\mathbb{E}[{}_s p_{x+T}^i]}{(1+r_{f(t,s)})^s} \right\}, & \text{for } t^i < T \\ \underline{b}_t^i \cdot \sum_{s=T+1}^{\omega-x} \frac{\mathbb{E}[{}_s p_{x+T}^i]}{(1+r_{f(t,s)})^s}, & \text{for } t^i \geq T \end{cases} \quad (46)$$

in which \underline{b} is estimated in every year and indicates the minimum amount of benefits at every point in time. Finally, the actual market-consistent value shall consider the amount of policyholders who will annuitize at the end of the accumulation period. Finally, the market-consistent value of liabilities is obtained by adding the deterministic risk margin $rm^{e/a}$ on top of best estimates.

Term Life business

⁴⁷See Appendix A.2.

⁴⁸For further details, see for instance Grosen and Løchte Jørgensen (2000), Bauer et al. (2006) or Gatzert (2008).

⁴⁹In order to compute the best estimate, insurers need to project the actual mortality developments in the future, given the information they have at time t . Thus, to do so we include the past observed trend in mortality improvements obtained via the LC model (in expected value terms) in every simulated period and use it to compute the best estimate cash flows.

⁵⁰For further details on the future returns granted to policyholders, see Appendix A.4.

The market-consistent value for term life liabilities is also computed discounting the expected amount of funds to be paid out in the future at risk free. More formally, this is given by the best estimate of the contract

$$j_t^{tl,i} = \sum_{s=0}^{T-t-1} \frac{DB \cdot \mathbb{E}[{}_s p_t^i] \cdot \mathbb{E}[q_{t+s}^i]}{(1 + r_{f(t,s)})^{(s+1)}} - \frac{\pi^i \cdot \mathbb{E}[{}_s p_t^i]}{(1 + r_{f(t,s)})^s} \quad (47)$$

which is then aggregated and endowed with a deterministic risk margin (rm^{tl}).

2.4 Non-Life Business

We model a stylized generic property/liability protection contract with a fixed yearly maturity, in which premiums (including loadings) and claims are yearly cashed in and liquidated respectively.

2.4.1 The Asset Side

The investment portfolio has a similar structure as the portfolio presented in 2.3.1: we assume that the insurer only invests in bonds which have the same temporal horizon as the contracts they replicate, i.e. 1 year time to maturity. In addition, we assume that the insurer does not undertake any stock and real estate investments. Thus, the market value of assets $A(t)^{nl}$ at time t is the simple sum of the share of sovereign bonds (ω_t^{sb}) and corporate bonds (ω_t^{cb}).⁵¹

2.4.2 The Liability Side

We define the market-consistent value of the liability side as follows⁵²

$$L(t)^{nl} = \frac{N^{nl} \cdot \pi^i \cdot (1 + rm^{nl})}{1 + r_{f(t,1)}} \quad (48)$$

in which N^{nl} represents the number of contracts, $\pi^i = k \cdot \mathbb{E}[C]$ is the premium per single contract with k being simply a constant to adjust the magnitude of the premium, and rm^{nl} is a deterministic risk margin. In order to determine the number of contracts, we assume that within the group the amount of non-life business reserves represents a share ω^{nl} of the total reserves at market-consistent value, which implies that $L(t)^{nl} = \frac{L(t)^l}{1 - \omega^{nl}} \cdot \omega^{nl}$. Thus, by fixing the value of π^i and rearranging terms, we obtain the following

$$N^{nl} = \frac{(1 + r_{f(t,1)}) \cdot L(t)^l \cdot \omega^{nl}}{\pi^i \cdot (1 + rm^{nl}) \cdot (1 - \omega^{nl})}. \quad (49)$$

⁵¹Similarly to the asset side for life business, the following conditions apply: $\sum_j \omega^j = 1 \wedge \omega^j \geq 0$ with $j = sb, cb$.

⁵²We drop the superscript j which indicates the country in order to simplify the notation.

Finally, the value of claims to be paid at time t is given by the following expression

$$\Psi_t^{nl} = N^{nl} \cdot \pi^i \cdot \tilde{C}(t) \quad (50)$$

and since we assume $\mathbb{E}[\tilde{C}^j] \stackrel{!}{=} 1$, it follows that $\mathbb{E}[\Psi] = N^{nl} \cdot \pi^i$.

2.5 The Free Cash Flow

2.5.1 Life Business

The free cash flow for the life business before dividends to shareholders is defined as follows

$$FCF_t^l = \underbrace{R_t^{a,l}}_{\text{coupons/dividends}} + \underbrace{F_t^l}_{\text{bonds due}} + \underbrace{\Pi_t^l}_{\text{premiums}} - \underbrace{\Psi_t^l}_{\text{benefits paid to PHs}} \quad (51)$$

in which

$$R_t^{a,l} = \sum_{j=1}^N \sum_{\tau=0}^{T-1} c_t^{sb,j,\tau} + \sum_{j=1}^N \sum_{\tau=0}^{T-1} c_t^{cb,j,\tau} + \sum_{j=1}^N d_t^{j,s} + \sum_{j=1}^N d_t^{j,re} \quad (52)$$

is the return on assets as sum of coupons and dividends.

$$F_t^l = \sum_{j=1}^N F_t^{sb,j,0} + \sum_{j=1}^N F_t^{cb,j,0} \quad (53)$$

is the sum of maturing bonds, i.e. notionals; premiums are given by the following expression

$$\Pi_t^l = \sum_{i=1}^{N^{l,e}} n_t^{e,i} \pi^{e/a,i} (1 + \varrho^l) + \sum_{i=1}^{N^{l,tl}} n_t^{tl,i} \pi^{tl,i} (1 + \varrho^l) \quad (54)$$

and finally, benefits paid to policyholders are given by

$$\Psi_t^l = (1 - \theta^a) \cdot v_t^{e,1} \cdot n_t^{e,1} \cdot \mathbb{1}_{\{t^i=T\}} + \quad (55)$$

$$+ \sum_{i=1}^{N^{l,e}} v_{t-1}^i \cdot \vartheta \cdot d_t^{l,i} \cdot \mathbb{1}_{\{t^i < T\}} + \sum_{i=1}^{N_t^{l,a}} (b^i + v_{t-1}^{a,i} \cdot \{r^{g,i} - r^i\}^+) \cdot n_t^{a,i} \cdot \mathbb{1}_{\{t^i > T\}} + \quad (56)$$

$$+ \sum_{i=1}^{N^{l,tl}} DB^i \cdot d_t^{tl,i} \quad (57)$$

in which (55) is the amount liquidated as lump sum to the matured cohort, (56) is the amount paid to early death individuals and to annuitants and (57) is the amount liquidated to policyholders who died during the year. The decision to pay out dividends to shareholders is taken by considering the minimum amount of capital the insurer must hold in order to comply with regulation, i.e. the

solvency capital requirement as per S II (SCR).⁵³ Thus, the amount of dividends is computed as follows

$$R_t^{sh,l} = \left\{ \min\{A(t^-)^l + FCF_{t^-}^l - L(t)^l - SCR(t)^l, r_{target}^{sh} \cdot OF^l(t-1)\} \right\}^+ \quad (58)$$

in which $A(t^-)^l$ is the total market value of assets before reinvestment, i.e. bonds which did not mature, stocks and real estate, $FCF_{t^-}^l$ is the free cash flow before dividends, $SCR(t)^l$ is the regulatory capital and r_{target}^{sh} is a maximum amount of dividends that can be paid out as ratio of the capital available (i.e. invested) in the previous period $OF(t-1)^l$. Finally, the cash to be actually reinvested, i.e. FCF_t^l , is computed as follows

$$FCF_t^l = FCF_{t^-}^l - R_t^{sh,l}. \quad (59)$$

The asset portfolio is then yearly rebalanced towards the initial allocation and towards the target duration.

2.5.2 Non-Life Business

The free cash flow for the non-life business before dividends to shareholders is defined as follows

$$FCF_{t^-}^{nl} = \underbrace{R_t^{a,nl}}_{\text{coupons/dividends}} + \underbrace{F_t^{nl}}_{\text{bonds due}} + \underbrace{\Pi_t^{nl}}_{\text{premiums}} - \underbrace{\Psi_t^{nl}}_{\text{claims paid to PHs}} \quad (60)$$

in which

$$R_t^{a,nl} = \sum_{j=1}^N c_t^{j, sb} + \sum_{j=1}^N c_t^{j, cb} \quad (61)$$

is the return on assets as sum of coupons and

$$F_t^{nl} = \sum_{j=1}^N F_t^{j, sb} + \sum_{j=1}^N F_t^{j, cb} \quad (62)$$

is the sum of maturing bonds, i.e. notional; finally, premiums are given by the following expression $\Pi^{nl} = N^{nl} \cdot \pi^{nl,i} \cdot (1 + \varrho^{nl})$. The decision to payout dividends to shareholders is taken by considering the minimum amount of capital the insurer must hold in order to comply with regulation, i.e. the solvency capital requirement as per S II (SCR).⁵⁴ Thus, the amount of dividends is computed as follows

$$R_t^{sh,nl} = \left\{ \min\{FCF_{t^-}^{nl} - L(t)^{nl} - SCR(t)^{nl}, r_{target}^{sh} \cdot OF^{nl}(t-1)\} \right\}^+ \quad (63)$$

in which $FCF_{t^-}^{nl}$ is the free cash flow before dividends, $SCR(t)^{nl}$ is the regulatory capital and r_{target}^{sh} and r_{target}^{sh} is a maximum amount of dividends that can be paid out as ratio of the capital available (i.e. invested) in the previous period $OF(t-1)^{nl}$. Finally, the cash to be reinvested, i.e. FCF_t^{nl} ,

⁵³For the computation of the SCR, see Appendix A.5.

⁵⁴For the computation of the SCR, see Appendix A.5.

is computed as follows

$$FCF_t^{nl} = FCF_{t^-}^{nl} - R_t^{sh,nl}. \quad (64)$$

The asset portfolio is then yearly rebalanced towards the initial allocation and towards the target duration.

2.6 Group Consolidation

The group balance sheet is simply the sum of the balance sheets of the subsidiaries, that is

$$\begin{aligned} A(t)^g &= A(t)^l + A(t)^{nl} \\ L(t)^g &= L(t)^l + L(t)^{nl} \\ OF^g(t) &= A(t)^g - L(t)^g. \end{aligned} \quad (65)$$

The function of the holding company in the model is to collect dividends coming from the subsidiaries and pay them to shareholders. In addition, it has the power to transfer capital from a subsidiary which has *excessive capital* (CE) to a subsidiary which has *capital shortage* (CS). Subsidiaries can have capital excess when

$$\begin{aligned} CE^{l/nl}(t) &= A(t)^{l/nl} + FCF(t)^{l/nl} - (L(t)^{l/nl} + SCR(t)^{l/nl}) > 0 \\ \iff A(t)^{l/nl} + FCF(t)^{l/nl} &> L(t)^{l/nl} + SCR(t)^{l/nl} \end{aligned} \quad (66)$$

or capital shortage when

$$\begin{aligned} CS^{l/nl}(t) &= L(t)^{l/nl} + SCR(t)^{l/nl} - (A(t)^{l/nl} + FCF(t)^{l/nl}) \geq 0 \\ \iff A(t)^{l/nl} + FCF(t)^{l/nl} &\leq L(t)^{l/nl} + SCR(t)^{l/nl}. \end{aligned} \quad (67)$$

Thus, there can be capital transfers in only 2 cases, i.e. case (1): $CE^l > 0 \wedge CS^{nl} > 0$ or case (2) $CE^{nl} > 0 \wedge CS^l > 0$. The amount of capital that is transferred is given by the following equations

$$\text{case (1): } \begin{cases} A(t)^l + FCF(t)^l - \min\{CE^l(t), CS^{nl}(t)\} - L(t)^l = OF^l(t) \\ A(t)^{nl} + FCF(t)^{nl} + \min\{CE^l(t), CS^{nl}(t)\} - L(t)^{nl} = OF^{nl}(t), \end{cases} \quad (68)$$

and

$$\text{case (2): } \begin{cases} A(t)^l + FCF(t)^l + \min\{CE^{nl}(t), CS^l(t)\} - L(t)^l = OF^l(t) \\ A(t)^{nl} + FCF(t)^{nl} - \min\{CE^{nl}(t), CS^l(t)\} - L(t)^{nl} = OF^{nl}(t). \end{cases} \quad (69)$$

In addition, total dividends are re-computed as follows

$$\text{case (1): } \begin{cases} R_t^{sh,l} = \min\{CE^l(t) - CS^{nl}(t)^+, r_{target}^{sh} \cdot OF^l(t-1)\} \\ R_t^{sh,nl} = 0 \end{cases} \quad (70)$$

and

$$\text{case (2): } \begin{cases} R_t^{sh,l} = 0 \\ R_t^{sh,nl} = \min\{CE^{nl}(t) - CS^l(t)^+, r_{target}^{sh} \cdot OF^{nl}(t-1)\}. \end{cases} \quad (71)$$

Finally, the marginal investment will include the capital transfer.

3 Calibration

3.1 Stochastic Processes

We simulate 1000 iterations for the financial market developments and 1000 iterations for the mortality developments. All balance sheets are calibrated as per end of 2014. For each iteration, we consider a 10 years horizon and, thus, we look at the evolution of solvency and profitability until year 2024.⁵⁵

3.1.1 Financial Markets Dynamics

To conduct a forward-looking cross-country assessment of the resilience of insurers balance sheets to different financial market developments, in particular the resilience to a protracted period of low interest rates, we define 3 scenarios: the *baseline scenario* foresees an interest rate level for the 10YTM German sovereign bond with convergence level to about 2%, coupled with the reversion to pre-crisis levels of corporate bonds spreads, stocks and real estate returns; the *adverse scenario* and the *severely adverse scenario* foresee a lower level of interest rates, with convergence level for the 10YTM German sovereign bond to about 1%. Moreover, under the adverse scenario corporate bond spreads, stocks and real estate returns revert to pre-crisis levels, whereas under the severely adverse scenario the calibration also encompasses a substantial increase in the volatility of the corporate bonds spreads, stocks and real estate returns as it occurred during the financial crisis. We calibrate the parameters k and σ_r of the Vasicek model on the data of the EONIA between January 2008 and December 2014 following (Brigo et al., 2009) to ensure a stronger mean reversion.⁵⁶ Moreover, we set the market price of risk at a relatively high level (i.e. $\lambda = 1$) to ensure a concavity of the yield curve close to the one typically observed in the markets. Had we set λ to a more common range of values, e.g. 0.05, the Vasicek model would generate rather flat yield curves due to the low interest rates foreseen by the assumed scenarios.⁵⁷ Table 1 reports the estimated parameters for the 3 scenarios whereas table 2 reports the correlation coefficients through which the processes are correlated. In addition, Figures 7 - 12 depict the results of simulations under the 3 scenarios.

⁵⁵To simulate all processes for financial markets we follow Brigo et al. (2009) and we use an Euler scheme to discretize the equations.

⁵⁶We chose such period for a more practical reason, i.e. the level of mean reversion we obtain allows for a stronger mean reversion compared using the EONIA data between January 1999 and December 2014 leads to a lower mean reversion.

⁵⁷See analogous considerations in Berdin and Gründl (2015)

3.1.2 Mortality Dynamics

Table 3 reports the estimated parameters for the Lee-Carter model at country level. In addition, an *adverse selection correction* was estimated by means of the results presented in Gatzert and Wesker (2012). Indeed, it is well known that, in presence of annuities, a self-selection of people with higher than the average life expectancy may arise.⁵⁸ Thus, we distinguish between the general population and the population who buys endowment/annuity products and we assume that the latter displays a mortality dynamics corrected for adverse selection as presented in table 3. Moreover, we assume that the population who buys term life products follows the general population.⁵⁹ This assumption is also reflected in the premium calculation and therefore taken into consideration by the management.⁶⁰

3.1.3 Claims Development

For the calibration of the claims development we follow a simple approach. More specifically, we assume that claims develop in the same fashion in every country and that they do not grow in expected value. In other words we assume that the collected premiums remain constant over time and that the business does not grow.⁶¹ Moreover, we assume that deviations from the expected amount of claims occur. In particular, we set the standard deviation to 10%, which is a more conservative figure than those presented among others in Gatzert and Schmeiser (2008a) or Gatzert and Schmeiser (2008b). The relatively low level of risk chosen for the development of claims is justified by the fact that combined ratios tend to be rather stable over time.⁶² Thus, by assuming fair pricing with loadings and a relatively moderate deviation from the expected value, we ensure a relatively stable combined ratio over time.⁶³ Table 4 reports the calibration of the model for the claim developments.

3.2 Asset and Liability Portfolios

The selected asset allocation for life business is reported in Figure 5, whereas for non-life business it is reported in Figure 6. The asset allocation for life business is shaped as to match both data available on the relative weight of single asset classes within the asset portfolio and the modified duration data as reported in EIOPA Stress Test (2014). For the sovereign bond portfolio, we assume

⁵⁸See for instance Finkelstein and Poterba (2004).

⁵⁹There is no reason why the mortality dynamics of policyholders who buy term life products should be identical to the mortality dynamics of the general population and thereby do not display any adverse selection behaviour. However, for the sake of simplicity we do not apply a correction term to this share of the business.

⁶⁰Loading factors are applied to the mortality assumptions used to compute premiums (loaded probabilities). This is in line with international practice, see for example Von Gaudecker and Weber (2004).

⁶¹This is a simplifying assumption: in fact one could introduce both for the life and non-life business, a growth rate for premiums at least in line with general inflation, which however is not modelled in the present framework.

⁶²A simplified combined ratio is computed as follows: $CR = \frac{\text{losses} + \text{expenses}}{\text{premiums}}$.

⁶³Further sensitivity analyses could test for different scenarios in which volatility is higher or pricing is subject to tougher competition and thereby profit margins tend to be low.

that the holdings of other sovereign bonds are equally distributed among the remaining countries. Table 5 reports in column (2) the relative weights of single sub-portfolios within the same asset class.⁶⁴ Moreover, in order to match the modified durations reported by *EIOPA Stress Test (2014)*, we apply the duration matching strategy presented in Section 2.3.1. More specifically, we select the last 20 YTM during the last 20 years as to be representative of the coupons simultaneously held in the portfolio: each coupon has a different expected time to maturity, i.e. the oldest coupon in portfolio is due in 1 year, whereas the youngest is due in 20 years. Then, in order to match the modified duration of the sub-portfolios, weights were chosen following the algorithm presented in Appendix A.3. We apply the same strategy also to corporate bond portfolios. In this context, the breakdown by credit quality is fixed across countries and the expected time to maturity for corporate bonds is 10. Therefore, the oldest coupon in the portfolio is due in 1 year whereas the youngest in 10 years. Weights are then assigned to each coupon to match the duration data reported by *EIOPA Stress Test (2014)* by applying the algorithm illustrated in Appendix A.3. Finally, for stocks and real estate sub-portfolios, due to data limitation, we apply a simpler approach.⁶⁵ In order to reproduce a plausible home bias, we assume that 60% of the stock and real estate portfolio is held in domestic assets while the remainder is equally distributed among the other countries. Table 5 reports the composition of stocks and real estate portfolios. The guaranteed rate of returns held in portfolio and the asset and liability durations are key drivers in the model. In particular, they are relevant for the endowment/annuity portfolio which is the most sensitive to interest rate changes. Table 6 reports the composition of the endowment/annuity portfolio at the beginning of the simulation (i.e. end of 2014). In this context, we apply the same methodology as in *Berdin and Gründl (2015)*, i.e. we accumulate cohorts of contracts using available past data and assuming a fixed time to maturity for the contracts over time. We then allow for an additional rate of return based on the available data from *EIOPA Stress Test (2014)* or based on the sovereign yields at country level. By doing so, we are able to reproduce the typical situation that life insurers face, i.e. the co-existence of different cohorts of contracts with different guaranteed rate of returns and different time horizons in portfolio. Moreover, this strategy also allows us to compute the modified duration of the endowment/annuity portfolio which is the most vulnerable to interest rate changes and which is reported in Table 7. The endowment/annuity portfolio is then matched by the asset portfolio and the difference between the duration of the 2 portfolios is reported in table 7 as well. The interpretation of the duration mismatch is the following: the higher the difference between the duration of the liability portfolio and the duration of the asset portfolio, the higher is the exposure to reinvestment risk and, therefore, the higher the sensitivity of the own funds to the movement of the term structure of interest rates. Finally, it is worth remarking that the presence of term

⁶⁴For instance, for Germany we use the data reported by *EIOPA Stress Test (2014)* on home sovereign holdings while the remainder of all sovereign holdings are equally distributed among French, Italian, Dutch and Spanish sovereign bonds. We follow the same approach for all countries, as we do not have more detailed data on sovereign holdings at country level.

⁶⁵Indeed, we do not have the geographical breakdown of stocks and real estate holdings.

life business and annuity business does change the duration mismatch in the balance sheet, as the modified duration of term life products is typically shorter than the modified duration of endowment products, whereas the modified duration of annuities is typically higher than the modified duration of endowment products. However, reserves allocated to term life and annuities in Europe are typically modest, thereby making the figures presented in Table 7 highly representative.

3.3 Specifications

We test 4 balance sheet compositions (i.e. specifications) in terms of business model: specification (1) foresees only endowment business, specification (2) foresees endowment business and term life business, specification (3) foresees endowment business, term life business and annuity business, whereas specification (4) introduces life and non-life business. Table 8 reports the different specifications and the relative weights of the different lines of business. This is an important aspect since traditionally endowment and annuity business tend to be very sensitive to interest rate risk and more in general to financial risk, whereas term life business and non-life business are rather insensitive to capital markets developments. Against this background, insurers have the possibility to diversify their liability portfolio and thereby increase resilience in case of adverse financial market conditions. Such resilience clearly depends on the relative weight of each line of business within the portfolio, which ultimately determines the solvency position and the profitability of the insurer. Since we do not have detailed data on the amount of reserves allocated to each line of business, i.e. endowment, term life and annuity business, and since we want to maintain a certain degree of comparability across countries, we define the different portfolio composition to be as realistic as possible given the data limitation (Table 8).⁶⁶

3.4 Other Balance Sheet Parameters

Table 9 reports the remaining parameters of the model. The share of reserves allocated to endowment/annuities is set to 95%, term life and the share of annuitants is set to 5%. We use data provided by BaFin for German life insurers (BaFin, 2013), in particular data on the amount of reserves allocated to term-life business, and we assume these figures are representative also for other countries.⁶⁷ By contrast, data for annuity business is very limited and not directly available from publicly available statistics. However, in general, annuities still represent a small business in continental Europe and, therefore, we assume 5% as to be a purely indicative figure. The split between life and non-life business at group level is calibrated using the data by the national insurance associations or by the local regulator in each country.⁶⁸ The number of cohorts

⁶⁶The availability of more granular data could allow clustering companies according to their business portfolios and thereby allowing for a more precise analysis.

⁶⁷We rely on German data to determine the relative weight of each line of business due to the lack of data and for comparability reasons.

⁶⁸The German Insurance Association (GDV) and Federal Financial Supervisory Authority (BaFin), the French Insurance Association (FFSA) and the Prudential Supervisory Authority (ACPR), the Italian Insurance Association

of contracts held in portfolio is a crucial variable as it allows to determine the time to maturity structure of the liability side. Unfortunately, we do not have sufficiently detailed data to estimate the expected time to maturity of typical endowment and term life contracts. However, based on the data on the duration of liabilities reported in the [EIOPA Stress Test \(2014\)](#), we can approximately infer the expected time to maturity of each cohort of contracts. In addition, to allow for comparability, we fix the expected time to maturity of term life contracts equal across countries. The money's worth ratio is based on data for Germany reported by [Von Gaudecker and Weber \(2004\)](#), whereas the loading factor for life premiums is fixed to 1% and for non-life to 5%: the difference between loading factors is justified by the fact that the non-life business displays fat tails in claim developments and therefore it requires higher premiums in order to hedge unexpected results.⁶⁹ The loading factor for mortality are taken from the German Actuarial Association and kept constant across countries.⁷⁰ Also premiums are computed using German data and kept constant across countries.⁷¹ Finally, the recovery value introduces an additional loading factor in case of early termination of the contract, the minimum share of r^a and r^q are taken from national regulations (if existent) and the risk margins are taken from [EIOPA QIS5 \(2010\)](#).

The dividend payout target and the initial (i.e. at the beginning of the simulation period) solvency ratio are 2 crucial parameters. The dividend payout ratio is a key variable in the model as it determines how much of the profits generated every year is cashed out to shareholders. To set this parameter, we refer to the statistical data released by EIOPA.⁷² In particular, we compute yearly averages at country level of the profit or losses realized over the year divided by the available solvency margin. In order to ensure comparability, we keep the average across country as reference parameter in every specification and for every country in the model. Moreover, we assume it to be fixed at group level.⁷³ The initial solvency ratio is also a crucial figure. Due to the lack of data availability and due to the need of ensuring comparability, we assume that all countries start the simulation period with the same solvency ratio, i.e. 165%. This value corresponds to the average European solvency ratio as reported in the [EIOPA QIS5 \(2010\)](#).⁷⁴

(ANIA) and the Insurance Supervisory Authority (IVASS), the Dutch Insurance Association (VAV) and the Dutch Central Bank (DNB) and finally the Spanish Insurance Association (UNESPA) and the [Ministry of Economy and Finance, DG for Insurance and Pension Funds](#).

⁶⁹Similar figures for loadings are reported for instance in [Gründl et al. \(2006\)](#).

⁷⁰The German Actuarial Association publishes a mortality tables including loading factors both for annuity business, i.e. DAV 2004R, and for term life business, i.e. DAV 2008T.

⁷¹Following the data reported by [BaFin \(2013\)](#), we extrapolate an approximate proportion among premiums for different insurance contracts.

⁷²[EIOPA Statistics - EU/EEA \(re\)insurance statistics 2005-2013](#).

⁷³The data suggest that there is a slightly higher propensity to generate profits in the non-life business, i.e. 8.3% compared to 7% in the life business. For the sake of simplicity we assume a unique dividend policy at group level.

⁷⁴The figure refers to both solo undertakings life and non-life, and insurance groups. In general we would expect non-life business to have a much higher solvency ratio compared to life, due to fat tails of the underlying risks: unfortunately the availability of data on SII ratios is scarce, therefore, we relied on an average figure for both lines of business and across countries, which in turn allow for greater comparability of results.

4 Results

Figures 13 - 17 report the results of the simulations for the baseline scenario, Figures 18 - 22 report the results of the simulations for the adverse scenario, whereas Figures 23 - 27 report the results of the simulations for the severely adverse scenario. For each country we look at 3 main variables which characterize the profitability and solvency dynamics over time: i) return on assets (computed at book values) which provides a measure of both the return policyholders expect on their accounts and the amount of cash generated from insurers financial assets⁷⁵, ii) return on equity measured as the ratio between the dividends paid out and the amount of own funds and iii) the solvency ratio as the most direct risk metrics. Finally, numerical results are summarized in Table 10.

4.1 The Baseline Scenario

Under specification 1 (Figure 13)⁷⁶, we observe a steady decline in the return on assets across all countries and across all specifications: this is the direct effect of the adjustment of the bond portfolios to the prevailing interest rate regime. More specifically, assuming an average duration spanning between 6 and 8 years, we might expect the asset portfolio to have completely turned around by the end of the simulation and, therefore, all available coupons to be in line with market rates. The return on equity displays a generalized decrease over time across all countries, except for Italy. The decrease in dividends is direct consequence of the solvency situation, which appears to be negatively affected in most countries. Indeed in our model, as soon as the solvency ratio approaches 100% (i.e. when own funds are close to the minimum regulatory amount), the management reduces the amount of dividends paid out to shareholders in order to increase the capital of the firm. The solvency ratio decreases dramatically in Germany as direct consequence of the high level of guarantees and the lower amount of profits generated from endowment business.⁷⁷ In fact, the solvency ratio decreases very rapidly, thus forcing the management to stop paying out dividends. France also displays a reduction in the amount of dividends paid out to shareholders justified by the relatively surprising decrease in the solvency ratio. Although the level of outstanding guarantees is substantially lower compared to Germany, this sharp reduction is mainly explained by the calibration of the asset portfolio. Indeed, based on our data, the asset portfolio foresees a relatively high exposure to stock-like asset classes which do not generate sufficient cash inflows

⁷⁵We do not take capital gains/losses into considerations since changes in market values directly affect the solvency ratio and, therefore, are better captured by the solvency ratio dynamics.

⁷⁶Specification 1 only includes endowment business.

⁷⁷It is worth stressing that for a portfolio of endowment business, additional source of return such as mortality profits are very small since the company has very limited exposition to mortality and, therefore, does not make profits out of mortality developments. For instance in [Berdin and Gründl \(2015\)](#), results for Germany look substantially different due to the deterministic inclusion of mortality gains (as much as 1% of outstanding reserves) which are indeed an important source of profit for life insurers. Thus, specification 2, in which term life business adds substantial profits, features a remarkable improve of the solvency situation.

to keep up with the liability portfolio.⁷⁸ The Netherlands and Spain display similar dynamics with respect to the return on equity, although for the Netherlands the situation improves along with the simulation, whereas for Spain the amount of dividends tends to zero by the end of the simulation. Both countries also display a reduction in their solvency position at the beginning, however consistently with the dynamics of the dividends, the situation improves for the Netherlands whereas it deteriorates further for Spain. Italy is a remarkable exception. Indeed, the dividend payout ratio does not seem to be strongly affected under this scenario, so is not the solvency ratio, although over the medium term we observe a moderate reduction. Such difference compared to other countries can be explained in part by the moderate duration mismatch, and in part by regulation: indeed Italian insurers are heavily exposed to Italian sovereign debt, which provides higher returns with moderate solvency capital requirements, thus improving the overall solvency situation.

Under specification 2 (Figure 14)⁷⁹, we can observe a generalized improvement across all countries of both profitability (in terms of return on equity) and solvency when compared to the results obtained under specification 1. However, the German balance sheet still displays a marked reduction in the solvency position over time, although less rapid than under specification 1: the reduction in the solvency position in turn reduces the amount of dividends paid out to shareholders, thus, highlighting how the German business model under a protracted period of low rates present vulnerabilities both in terms of profitability and solvency. France and Spain only show a minor reduction in their solvency positions towards the end of the simulation period, whereas Italy and the Netherlands appear to be in a better position.

This generalized improvement is essentially due to the diversification of the business portfolio. The inclusion of the term life business (corresponding to 5% of total liabilities) increases the free cash flow and, thereby, allows the insurer to pay out more dividends and to remain compliant with the solvency regulation. Indeed, the term life business generates about 25% of the total income premium although its share, appears moderate.⁸⁰ In addition, the pricing for the term life business is conducted with loaded mortality probabilities and additional loading on premiums which allow the insurer to collect on average more premiums than the benefits it has to liquidate.⁸¹ Thus, a more diversified portfolio has a beneficial effect on both profitability and solvency, which however heavily depend on the pricing of the products and more generally on the competitive stance of the market.⁸²

⁷⁸The share of stocks in France appears to be substantially higher compared to other countries, better data could help in understanding if insurers actually hold a high portion of stocks in their general account or part of these holdings are attributable to separate accounts.

⁷⁹Specification 2: Endowment and Term Life Business includes endowment and term-life business.

⁸⁰This figure is the average across countries: depending on the accumulated endowment liabilities, the amount of collected premiums changes, as the number of contracts sold yearly is calibrated to match the share of liabilities at market-consistent value.

⁸¹Clearly, the results are dependent on the underlying calibration which might be arbitrary. Indeed, we could expect lower profit margins as markets increase in competition. Therefore, further sensitivity analyses could shed additional light on the role of technical margins.

⁸²For instance, selling products at lower prices could increase the demand for such products but at the same time

Under specification 3 (Figure 15)⁸³, consistently with the results observed in specification 2, we note a further improvement of the insurers financial conditions. In fact, adding annuity business allows the insurer to smooth cash outflows over time and to increase expected profits via pricing. However, this occurs at the cost of taking other risks, in particular longevity risk. This combined effect of smoothing cash outflows and higher profits due to pricing, offsets the valuation effect due to the higher expected duration of the liability side. This is a particularly relevant aspect since under S II, insurers have the possibility of discounting liabilities using the ultimate forward rate, which in turn decreases the market-consistent value of liabilities compared to the theoretical marked-to-market valuation and thereby boosts its solvency position and its expected dividend payouts. Results once again heavily depends on the pricing of products, i.e. for annuities on the coefficient mw . Indeed, the higher is mw , the lower is the expected profit of the insurer and the higher is the exposure to longevity risk, which, however, materializes very slowly in the balance sheet and, therefore, it is hard to detect within the time horizon we consider.⁸⁴ Thus, with a more diversified portfolio insurers can better cope with a persistent low interest rate environment, although in the case of Germany we still observe a reduction in the solvency situation towards the end of the simulated period, with a consequent mild reduction in the dividend payout ratio.

Finally, specification 4 (Figures 16 and 17) introduces the group diversification and the possibility to redistribute capital within the group. Results are essentially similar to specification 3, however, a few caveats are necessary. The model we present for non-life business is highly stylized and does not feature some fundamental specificities of this business. Nevertheless, upon proper calibrations, the model allows for testing the resilience of an insurance group to different claims developments and different competitive stances of the market, and thereby to identify critical levels of capitalization. In general, we observe that the level of the asset return for non-life is much lower and the volatility much higher compared to life. This is due to the fact that we assume a very short duration, i.e. 1 year, for the asset allocation of the non-life business. Indeed, this assumption implies that the financial returns are exposed to the higher volatility of the short term rates. In addition, the volatility of the solvency ratio is much higher compared to life. This is due to the calibration of the claims distribution: indeed the deviation from the expected claims is substantial (refer to Table 5) and it results in marked changes in the solvency ratio. Moreover, the median level of the solvency ratio grows for all countries over time, implying that the business generates sufficient free cash flows to pay out dividends and increase the value of the own funds. The solvency ratio of the life business remains substantially unchanged compared to specification 3, thus, excluding capital redistributions from the life business towards non-life business.

In conclusion, we can say that a scenario in which interest rates converge towards 2% in the

it would expose the insurer to higher risks.

⁸³Specification 3: Endowment, Term Life and Annuity Business includes endowment, term-life business and annuity business.

⁸⁴For instance [Kojen and Yogo \(2014\)](#) provide evidence of sales at discount in the U.S. market during the financial crisis as a means to boost cash inflows in time of (potential) distress. The authors identify negative mark-ups, i.e. $mw > 1$, during the financial crisis, with picks of $mw > 1.15$ for 30 years term annuities.

long run and in which spreads, stocks and real estate developments return to pre-crisis level, would still represent a threat to those companies more exposed to financial guarantees, in particular in those markets in which contracts have long maturities and local regulation is more stringent in terms of profit participation.

4.2 The Adverse Scenario

Under specification 1 (Figure 18), we observe a generalized worsening of both profitability and solvency across almost all countries. Indeed, a lower level of interest rates has a profound impact on the valuation of both asset and liabilities, in which the latter increase more due to the higher duration. Such effect is particularly strong for Germany, which displays the higher outstanding levels of guarantees and (together with the Netherlands) the longest maturities. Thus, a higher value of expected future liabilities reduces the solvency ratio and thereby forces the management to reduce the dividend payouts, consistently with the results observed under the baseline scenario. Adding term life business (Figure 19) results in a generalized improvement for all countries but Germany. Indeed, Germany still experiences a strong reduction in the return on equity due to the lower solvency ratios, which in almost half of the simulated paths results below minimum requirements. Consistently with the results observed under calibration 1, adding term life and annuity business (Figure 20) improves the situation both for profitability and solvency across all countries. However, Germany still appears to be vulnerable even after the business diversification.

Finally, in specification 4 which feature both the life and non-life business (Figure 21), we can observe that the median solvency ratio for the non-life business has substantially decreased compared to the baseline scenario: such effect is mostly due to the lower return on assets that under the adverse scenario the assets allocated to the non-life business can achieve. In fact as the duration of the asset allocation is 1 year, the effect of low rates is immediately transmitted into the balance sheet, which results in lower cash inflows from coupons and thereby lower growth of own funds. In Figure 28 we report the relative decrease of the median solvency ratios for non-life business under the adverse scenario compared to the baseline scenario: it can be noted that the decrease ranges from 20 pp for Germany and Spain to almost 40 pp for France, Italy and Netherlands. Such difference is on the one hand due to the higher median solvency ratio under the baseline scenario, which then translates into a stronger drop under the adverse scenario, and on the other hand it is due to the idiosyncrasy in the asset allocation across countries and consequently in the different solvency capital requirements.

Capital transfers do not seem to play a role, meaning that the solvency level in the life business does not drop sufficiently to negatively affect the solvency position of the non-life business. Thus, we can conclude that lower rates may also reduce the solvency level of non-life insurers assuming an unchanged premium income. The speed of the transmission into the balance sheet of such effect clearly depends on the time to maturity structure of the asset allocation.

4.3 The Severely Adverse Scenario

Under specification 1 (Figure 23), we observe even worse results compared to the adverse scenario. This is mainly the effect of the higher volatility in financial markets, which substantially increases the volatility of the solvency ratio. This is particularly evident for Italy and Spain, which under the severely adverse scenario experience a high volatility of their sovereign debt and severely adverse stock and real estate market developments. This higher volatility has a detrimental effect on the solvency ratio for both markets. In particular, Italy, which never displays downside risks with respect to low interest rates, seems to be especially exposed to the volatility of its sovereign debt due to the strong home bias on bond investments. The higher volatility in financial markets decreases profitability across all markets as direct consequence of the reduce solvency ratio. By diversifying the liability portfolio, we can observe a generalized improvement (Figures 24 and 25). Overall, Germany and Spain seem to be the most exposed to this scenario, with both important reductions in profitability and solvency position.

Likewise to the adverse scenario, under specification 4, we can observe also a reduction in the median solvency ratio of the non-life business across all countries, although the reduction is less pronounced compared to the adverse scenario, especially for France, Italy and the Netherlands. Such result is due to 2 related phenomena: on the one hand, the higher volatility provides higher asset returns which are immediately visible in the balance sheet due to the short duration of the asset side; on the other hand, the short duration prevents the volatility to influence the solvency ratio since all bonds mature within the year and therefore capital gains and losses are not visible in the balance sheet. This is clearly a particular feature of the model: in fact a higher duration of the asset side would result in a higher volatility of the solvency ratio. However, such result does not hold for Spain and Germany: in fact, in Figure 28 we can observe how the drop in the median solvency ratio for the Spanish non-life business in the severely adverse scenario compared to the baseline is very strong in the first years of the simulation. Also for Germany we can observe a similar development, although less pronounced compared to Spain. This is the direct effect of the capital redistribution within the group: as the life business is exposed to high volatility and low interest rates, it drags capital from the non-life business and thereby reduces the solvency position of the non-life business. Once more this is an interesting development, since capital transfers within a group may be a potential source of interconnection and therefore spill overs across business lines.

5 Conclusion

In this paper, we present a forward-looking model for the assessment of solvency and profitability in insurance companies. We model the balance sheet of both life and non-life insurance business, which we then project under stochastic capital markets, stochastic mortality and stochastic claims. In our framework, we are able to test the resilience of insurance companies under different capital market scenarios, with particular focus on a protracted period of low interest rates. Our evidence

suggests that there are insurance markets which appear to be particularly exposed to downside risks due to their peculiarities and to their specific regulation. We observe that diversification of the business portfolio has a strong positive effect, which however depends very much on a number of factors that are key to the analysis. Those factors include pricing, the competitive stance, the demand for new contracts and the lapse ratio which all strongly determine the outcome of the model. Moreover, we can observe that low rates may also affect the solvency level of the non-life business through lower return on assets and also through capital redistribution within groups, which may represent a potentially negative spillover. This is a relevant aspect, in particular in light of the ongoing low interest rate environment in which life insurers are exposed to downside risks and might have need for additional capital in the future.

However, it is worth remarking that results should be taken with caution. Indeed the high number of inputs necessary for the model make the results dependent on the calibration whose quality in turn depends on the availability of data.⁸⁵ Moreover, the analysis assumes no changes in the asset allocations or portfolios of the insurance companies over the simulation period while such adjustments have already been taking place for some time, and might likely continue further. Additionally, the analysis does not take into account the long-term guarantee measures, which are an important part of the new Solvency II framework, and intend to diminish balance sheet volatility and have been already shown to have a significant dampening impact. Nevertheless, the results presented in this paper confirm some previous findings on the weaknesses of the life insurance industry in certain markets, in particular in Germany, and provide an additional warning on the potential threats to its stability that could derive by a protracted period of low interest rates. Further analyses could spark additional light on the policy measures necessary to prevent future crises. In conclusion, our research is one of the first attempts to create an analytical framework for assessing financial stability in the insurance sector. Our model not only allows to stress-test the balance sheet of an insurance group under different capital market developments, but it also allows considering other key aspects of the insurance business. In fact, the portfolio diversification, the role of pricing and the competitive stance are examples of influencing factors, which can be further analyzed for policy purposes. Moreover, our model provides a multi-period perspective, which is a relevant aspect in the insurance industry, as risks tend to accumulate over time. Indeed, we think that it is essential for policy authorities to have at their disposal rigorous tools which allow for forward looking assessments of this sector. Finally, further research is necessary, especially on more general equilibrium aspects of the analysis, such as policyholders' behavior and asset allocation dynamics. These features could be introduced in our framework and could potentially spark additional light on the underlying economics of the insurance business.

⁸⁵Indeed, more precise and granular data could of course increase the quality and reliability of results.

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A Appendix

A.1 Actuarially Fair Annuity Benefits

The actuarially fair yearly benefits are computed according to the following equivalence principle in which the present value of the inflow of premiums and return from reserves, i.e. the guaranteed return and the additional profit participation, is set equal to the present value of the outflow of benefits. At the inception for a single annuitant the equivalence is expressed as follows

$$\underbrace{\sum_{t=1}^T \frac{\pi^i \cdot {}_t p_x^i}{(1+r^i)^t}}_{\text{accumulation}} \stackrel{!}{=} b^i \underbrace{\sum_{t=T+1}^{\omega-x} \frac{{}_t p_x^i}{(1+r^i)^t}}_{\text{decumulation}} \quad (72)$$

in which b^i are the actuarially fair benefits granted to the annuitant and ${}_t p_x$ is the survival probability of the annuitant, i.e. the probability that an individual aged x survives the next t years. When a loading factor is applied, i.e. the annuity is not fairly priced, benefits are computed as follows

$$b_t^i \stackrel{!}{=} \frac{mw \cdot v_t^{e,i}}{\sum_{s=T+1}^{\omega-x} s p_t^i (1+r^i)^s} \quad (73)$$

in which the money's worth ratio is assumed to be $mw < 1$. This is a typical setting for annuity providers which is justified by both the need of charging a risk premium for unhedgeable risks and market power. Please note that the same result can be achieved by applying a loading factor to the actual survival probabilities.⁸⁶

A.2 Actuarially Fair Mortality Benefits

The actuarially fair death benefits are computed as follows⁸⁷

$$DB^i = \sum_{s=0}^{T-1} \frac{(1+r^i)^{(s+1)}}{s \bar{p}_x^i \cdot \bar{q}_{x+s}^i} \cdot \frac{\pi^i s \bar{p}_x^i}{(1+r^i)^s} \quad (74)$$

The same considerations regarding the loading on the actual survival probabilities hold for the mortality benefits, i.e. insurers typically load mortality probabilities thereby deviating from fair pricing.

A.3 Duration Matching Strategy

We develop a simple algorithm which enables us to keep the duration of the asset portfolio unchanged over time. Since in the portfolio there coexist a fixed number of coupons with fixed time to maturity, it is necessary to impose a certain relation among coupons, otherwise there would

⁸⁶For more details see for instance [Pitacco et al. \(2009\)](#) and [Cannon and Tonks \(2008\)](#).

⁸⁷See for instance [Gatzert and Wesker \(2012\)](#).

be infinite solutions. Thus, portfolio weights for each bond portfolio are computed following this algorithm:

$$\left\{ \begin{array}{l} \omega_1 \cdot d_1 + \dots + \omega_n \cdot d_n = \bar{D} \\ \omega_1 + \omega_2 + \dots + \omega_n = 1 \\ \omega_1 = k \cdot \omega_2 \\ \omega_2 = k \cdot \omega_3 \\ \cdot \\ \cdot \\ \omega_{n-2} = k \cdot \omega_{n-1} \\ \omega_{n-1} = k \cdot \omega_n \end{array} \right. \quad (75)$$

in which d_j are the mod. durations given by the coupons available and the chosen TtM structure (e.g. 1 bucket has 1 year TtM , ..., 1 bucket has 20 years TtM) and \bar{D} is the target for the portfolio mod. duration. finally, the system is solved for k , which determines the relation between each pair of adjacent coupons. Then it is straightforward to compute the weight to each single bucket of bonds.

A.4 Projection of Future Profit Distributions

The vector containing the expected future rate of return stemming from the profit sharing mechanism is a simple linear projection based on the information available at time t . More formally, $\mathbb{E}(r_{t+T}^g | \mathcal{F}_t)$ is estimated by extrapolating a trend on the set of observed past returns. The model is given by the following expression

$$\hat{r}_{t+1}^g = \phi_0 + \sum_{i=1}^p \phi_i r_{t-i}^g + \varepsilon_t \quad (76)$$

from which a drift is extrapolated in every period and used to project the expected future profit distribution.⁸⁸ The idea is to take into account at least part of the value of future profit distributions in the computation of the market-consistent value of liabilities, thereby valuing the option embedded in the product. Such valuation method is on the one hand computationally fast, but on the other it tends to neglect the complex path dependence dynamics of with profit participation policies. A more sophisticated approach should indeed include a stochastic component which would require the use of nested Monte Carlo simulations. However for the sope of the present work and for computational reasons, we abstain from the stochastic valuation of liabilities.

⁸⁸We fix $p = 10$, i.e. we consider always the last 10 observations.

A.5 Solvency Capital Requirements

A.5.1 Life Business

We adopt a simplified version of the Standard Formula proposed under S II: in particular we compute at each point in time the capital requirements for the *market module* and the *life module*: under the market module we consider the following sub-modules:

- Interest rate \Rightarrow for both Assets and Liabilities;
- Equity \Rightarrow for the stock investment, i.e S^s ;
- Property \Rightarrow for the real estate investment, i.e S^{re} ;
- Spread \Rightarrow for corporate bonds investment, i.e B^{cb} ;

whereas under the life module we consider the following sub-modules

- Mortality \Rightarrow for term life business, i.e. L^{tl} ;
- Longevity \Rightarrow for endowment/annuity business, i.e. $L^{e/a}$.

The 2 modules are then aggregated by means of given correlation coefficients.

A.5.2 Non-Life Business

For the non-life business we abstain from the standard formula under S II when computing the non-life sub-module, since we do not know all the information we would need in order to compute it as required. However, since we know the distribution of the claims over the next period, we can apply the $VaR_{0.995}$ (i.e. $\mathbb{P}\{OF_{t+1} < 0\} \leq 0.005$) which is the risk measure adopted under S II. The non-life sub-module is then computed as follows

$$SM^{nl} = N^{nl} \cdot \pi^i \cdot (e^{\mu_C + z\sigma_C} - 1) \quad (77)$$

in which $z = 2.58$, i.e. the coefficient taken from the standard normal distribution equivalent to 99.5%. Finally, SCR^{nl} is the sum of the non-life sub-module and the market sub-module aggregated by means of given correlation coefficients.

A.6 National Regulation

We report the main features of national regulations, i.e. *maximum allowed guaranteed return* and *profit participation* or *other specific requirements*.

A.6.1 The German Regulation

- *maximum allowed guaranteed return*: the regulator computes a reference interest rate (r_t^{ref}), which is the 10 year moving average of the 10 year Bund yield. It then consider 60% of it and reacts to the changes in interest rates as follows:

$$\begin{cases} r_{t+1}^i = r_t^i - \xi, & \text{if } 60\% \cdot r_t^{ref} \leq r_t^i \\ r_{t+1}^i = r_t^i + \xi, & \text{if } 60\% \cdot r_t^{ref} \geq r_t^i + \xi \\ r_{t+1}^i = r_t^i, & \text{otherwise} \end{cases} \quad (78)$$

where r_t^i is the maximum allowed guaranteed rate of return at time t and ξ is the marginal change decided by the regulator. For Germany this is fixed to 0.5 pp;

- *profit participation*: the profit sharing mechanism is given by the following equation

$$r_t^{g,i} = r^i + \{max[(r_t^a - r^i)^-, v \cdot r_t^a - r^i] + (v \cdot r_t^q)^+\}^+ \quad (79)$$

in which $v = 90\%$ (financial results and technical results).

- *other specific requirements*: there are additional mandatory requirements in the German market, such as an additional reserve in case of lower market rates and mandatory distribution of hidden reserves; we introduce it as in [Berdin and Gründl \(2015\)](#).

A.6.2 The French Regulation

- *maximum allowed guaranteed return*: the regulator computes a reference interest rate (r_t^{ref}), which is the 1 year moving average of the 10 year OAT yield. It then consider 60% of it and reacts to the changes in interest rates accordingly (source: [Banque de France](#)). More specifically, the basic rate for computation is given by the following

$$TME_t = \frac{1}{30} \sum_{t_i}^{30} r_{(t_i,10)}^{FR} + 0.05\%, \quad (80)$$

then the reference rate is derived as follows

$$r_t^{ref} = \frac{1}{6} \sum_{h=0}^5 TME_{t-h} \quad (81)$$

and finally the maximum allowed guaranteed return (or technical rate) is computed as follows

$$r_t^i = max(60\% \cdot r_t^{ref}, 3.5\%). \quad (82)$$

However, in order to comply with market practices in France, we assume that all new contracts issued after year 2000 are set to 0, i.e. $r_t^i = 0$;

- *profit participation*: the profit sharing mechanism is given by the following equation

$$r_t^{g,i} = r^i + (v^a \cdot r_t^a - r^i)^+ + (v^q \cdot r_t^q)^+ \quad (83)$$

in which $v^a = 85\%$ (financial results) and $v^q = 90\%$ (technical results).

For a brief but precise description of the French regulation, see for instance [Borel-Mathurin et al. \(2015\)](#).

A.6.3 The Italian Regulation

- *maximum allowed guaranteed return*: the regulator computes a reference interest rate (r_t^{ref}), which is the 1 year moving average of the 10 year BTP yield. It then consider 60% of it and reacts to the changes in interest rates accordingly. More specifically, the basic rate for computation is given by the following

$$TMO_t = \frac{1}{30} \sum_{t_i}^{30} r_{(t_i,10)}^{IT} + 0.05\% \quad (84)$$

then the reference rate is derived as follows

$$r_t^{ref} = \frac{1}{3} \sum_{h=0}^2 TMO_{t-h} \quad (85)$$

and finally the maximum allowed guaranteed return (or technical rate) is computed as follows

$$r_t^i = \max(60\% \cdot r_t^{ref}, 4\%); \quad (86)$$

- *profit participation*: the profit sharing mechanism is given by the following equation

$$r_t^{g,i} = r^i + (v^a \cdot r_t^a - r^i)^+ \quad (87)$$

in which $v^a = 80\%$ (financial results). However, there is no specific regulation regarding v^a which is usually agreed at inception in the contract. Thus 80% reflects the common practice in the Italian market and not a specific regulation.

A.6.4 The Dutch Regulation

- *maximum allowed guaranteed return*: no specific regulation applies;

- *profit participation*: the regulator publishes a reference interest rate through which companies can compute the amount of return to be transferred to policyholders. The reference rate is a weighted average of Dutch sovereign yields and it is computed as follows

$$u^{yield} = 0.1 * \frac{\sum_{\tau=1}^5 r_{(t,\hat{i})}^{NL}}{5} + 0.65 * \frac{\sum_{\tau=6}^{10} r_{(t,\hat{i})}^{NL}}{5} + 0.25 * \frac{\sum_{\tau=11}^{15} r_{(t,\hat{i})}^{NL}}{5} \quad (88)$$

and then the the profit sharing mechanism is given by the following equation

$$r_t^{g,i} = r^i + (u^{yield} - r^i)^+ \quad (89)$$

A.6.5 The Spanish Regulation

Due to limited information, we assume for the Spanish market the same underlying regulation as for the Italian market due to their similarities.

B Figures

Figure 3: Time to maturity structure: the figure depicts the time to maturity structure of both assets, i.e. cohorts of bonds, and liabilities, i.e. cohorts of insurance contracts. T^A and T^L represent the expected (fixed) time to maturity of bonds and insurance contracts in years: the structure implies that yearly, a cohort of bonds and a cohort of insurance contracts mature, and are replaced with a new cohort. In the model, on the asset side as well as on the liability side, there exist different asset classes as well as different life of business: each of them have the same time to maturity structure, in which the expected (fixed) time to maturity varies.



Figure 4: Model mechanics: the figure depicts the consolidation of the subsidiaries within the holding company, through which capital transfers can take place.

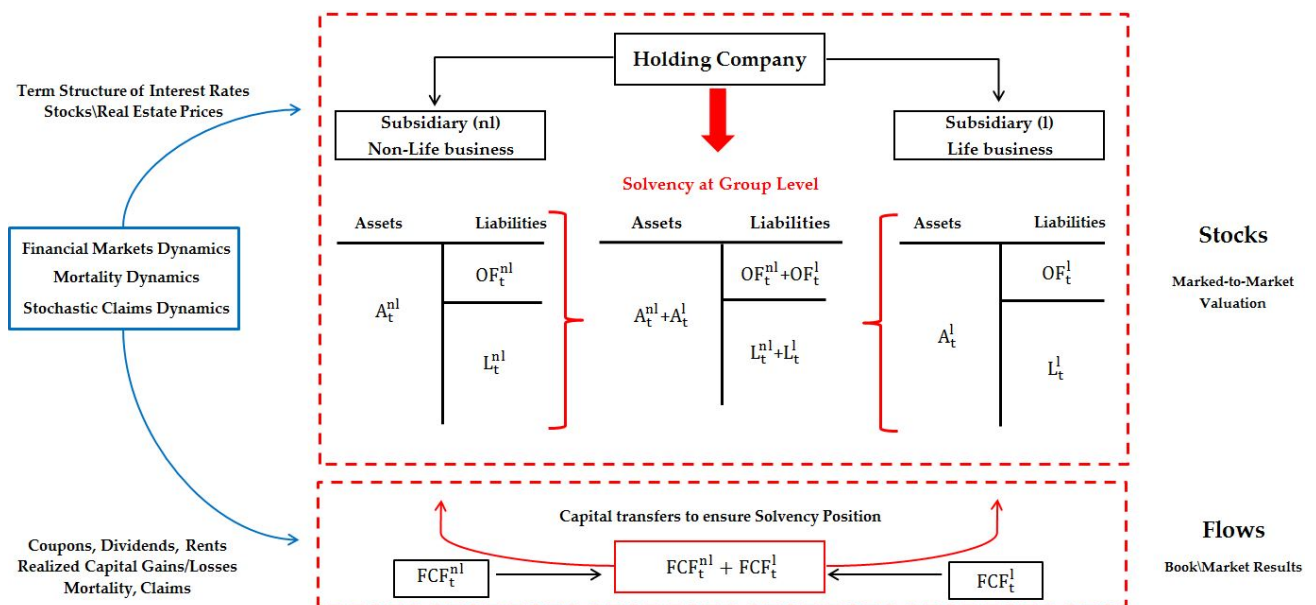


Figure 5: Asset Allocation Life Business: country level data have been retrieved from [EIOPA Stress Test \(2014\)](#), from national authorities and from national insurance associations.

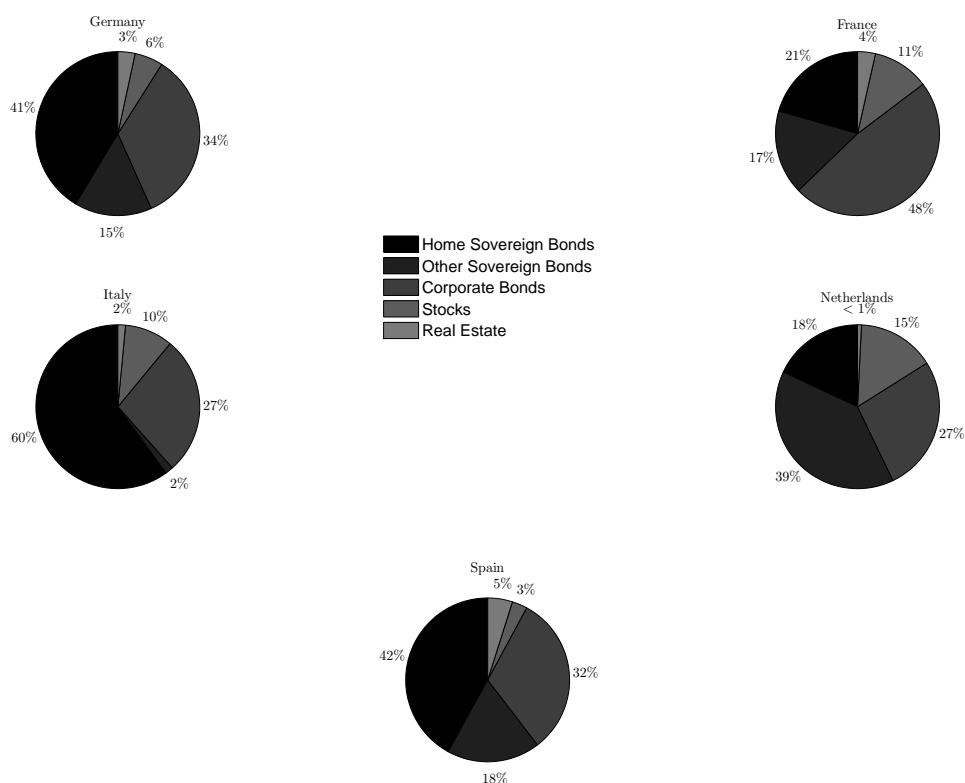


Figure 6: Asset Allocation Non-Life Business: the portfolio only includes bonds, sovereign and corporate which are held in same proportions as in the life business asset portfolio.

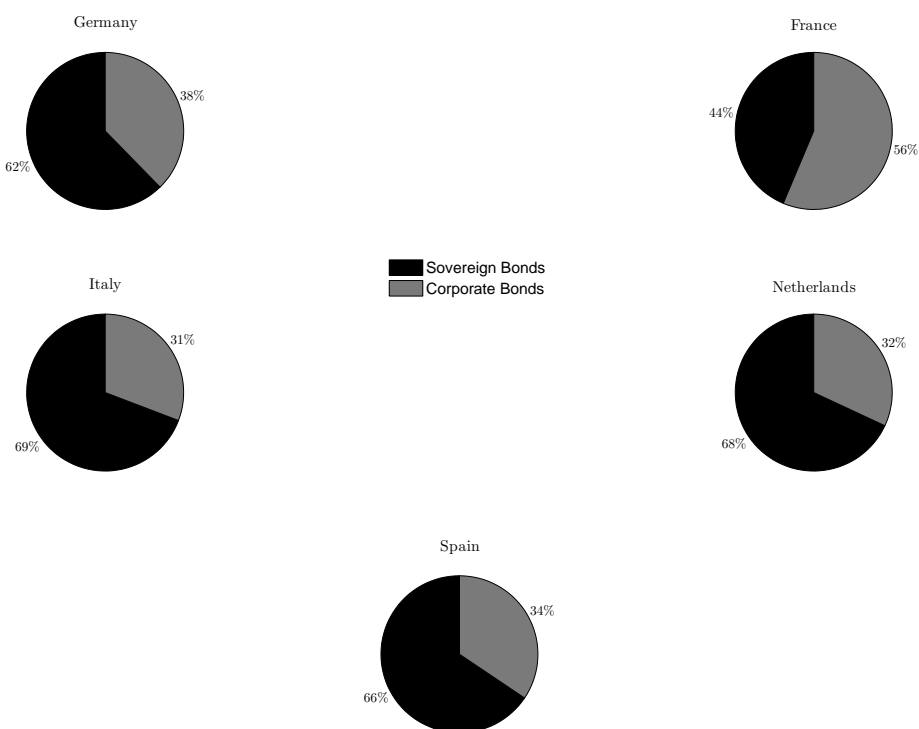
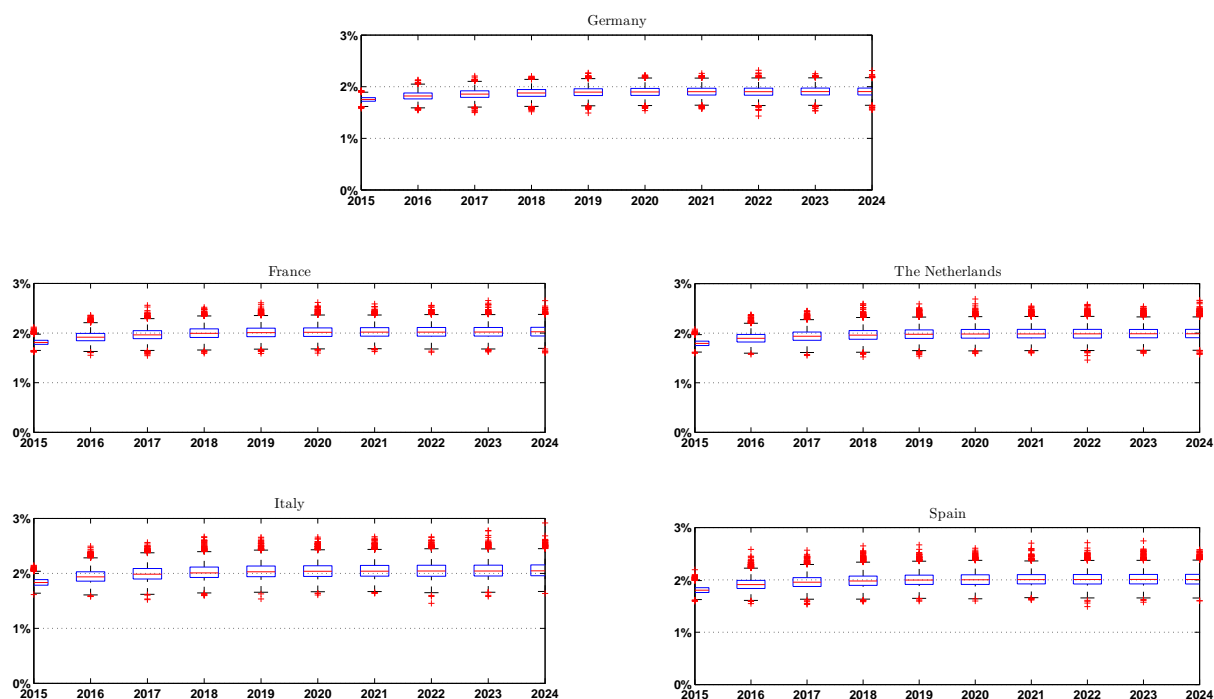


Figure 7: Baseline Scenario - 10 YTM Sovereign Bonds Yields

The graphs show the distribution of the simulation: the central red mark is the median, the edges of the box are the 25th and 75th percentiles respectively, the whiskers extend to the most extreme data points not considered outliers whereas outliers are plotted individually.



Baseline Scenario - 10 YTM Corporate Bonds Yields

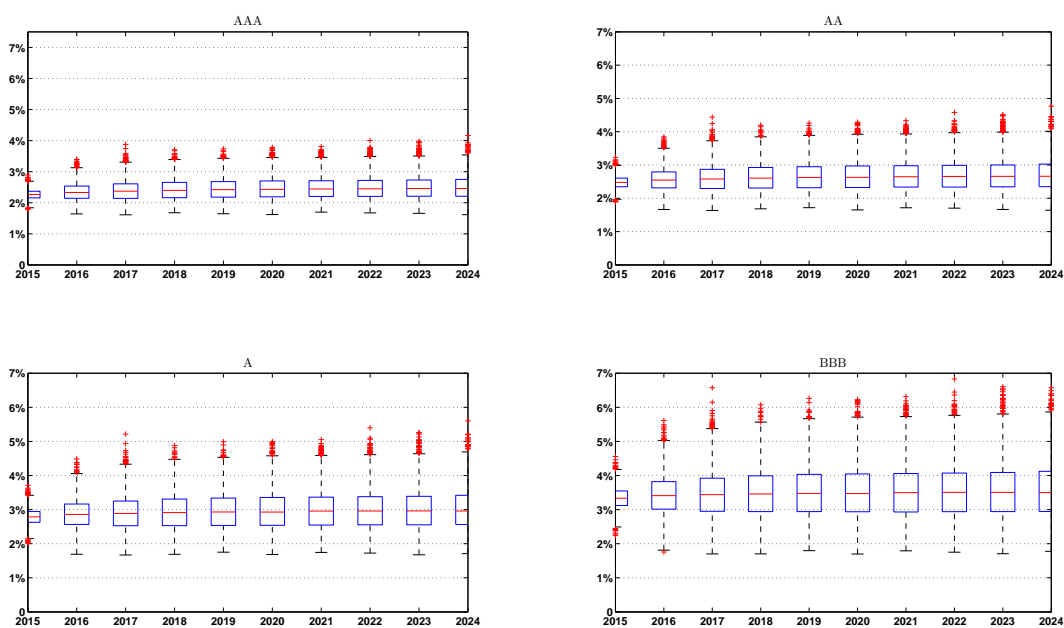
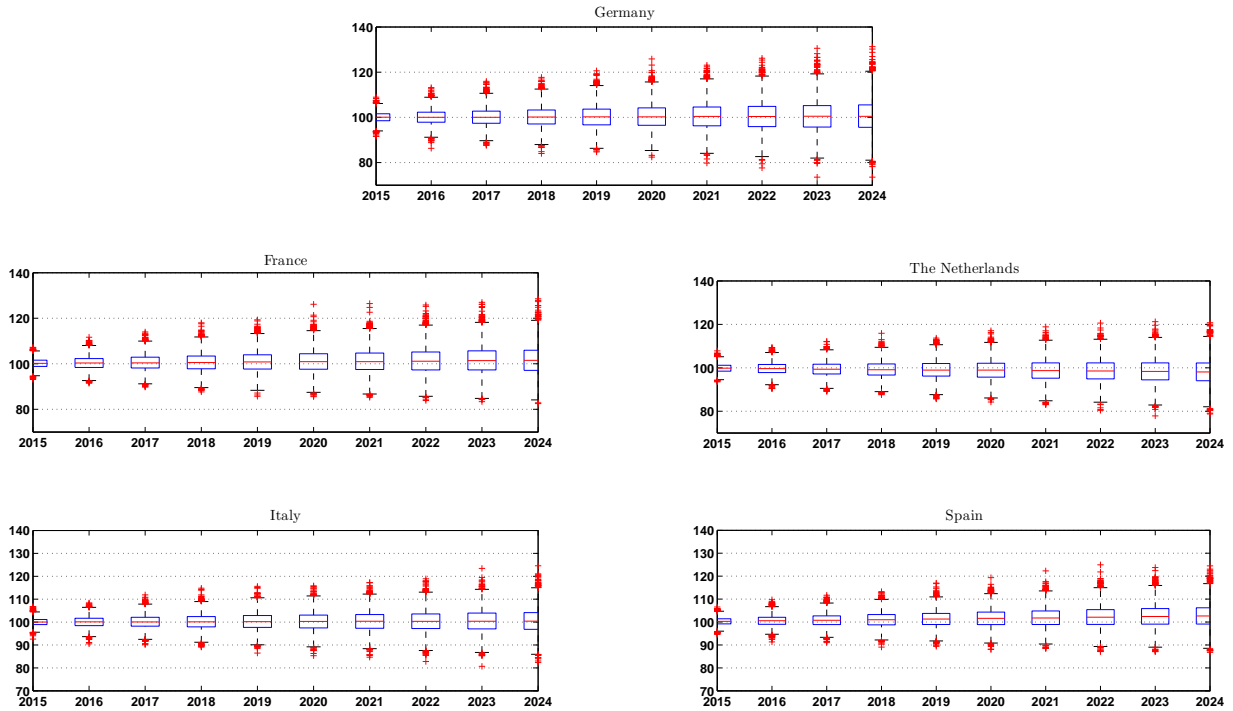


Figure 8: Baseline Scenario - Stock Indices:

The graphs show the distribution of the simulation: the central red mark is the median, the edges of the box are the 25th and 75th percentiles respectively, the whiskers extend to the most extreme data points not considered outliers whereas outliers are plotted individually.



Baseline Scenario - Real Estate Indices

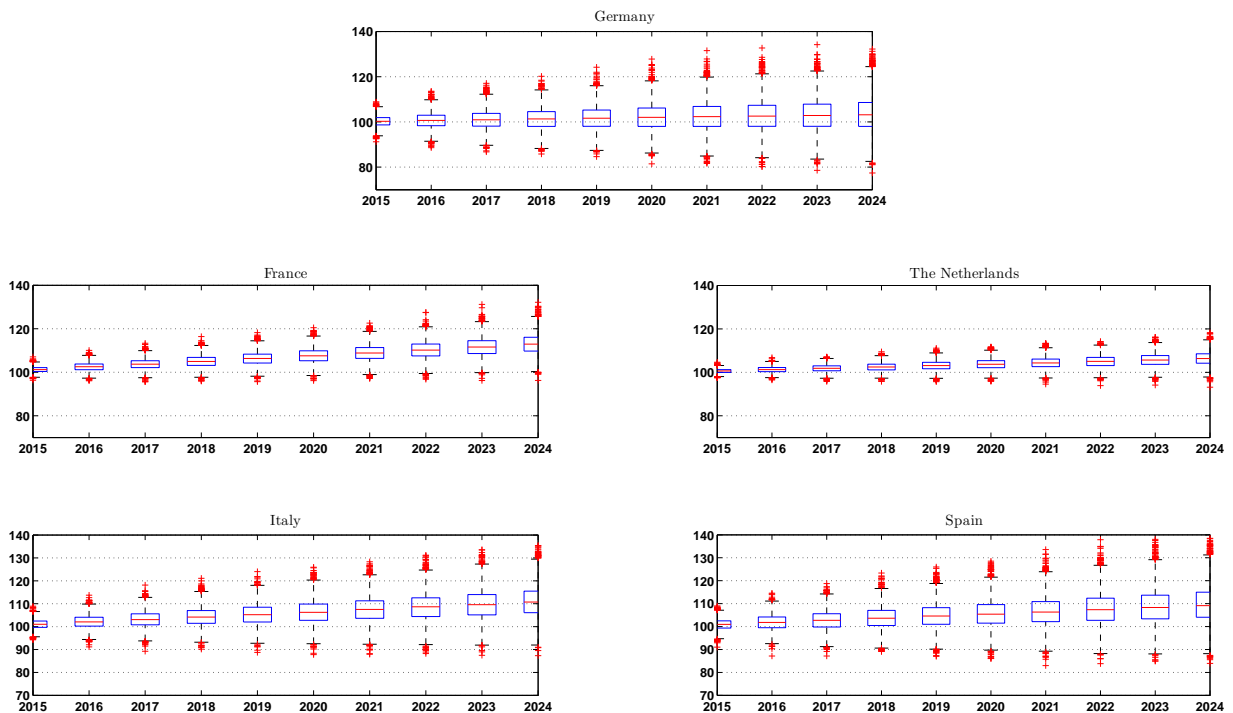
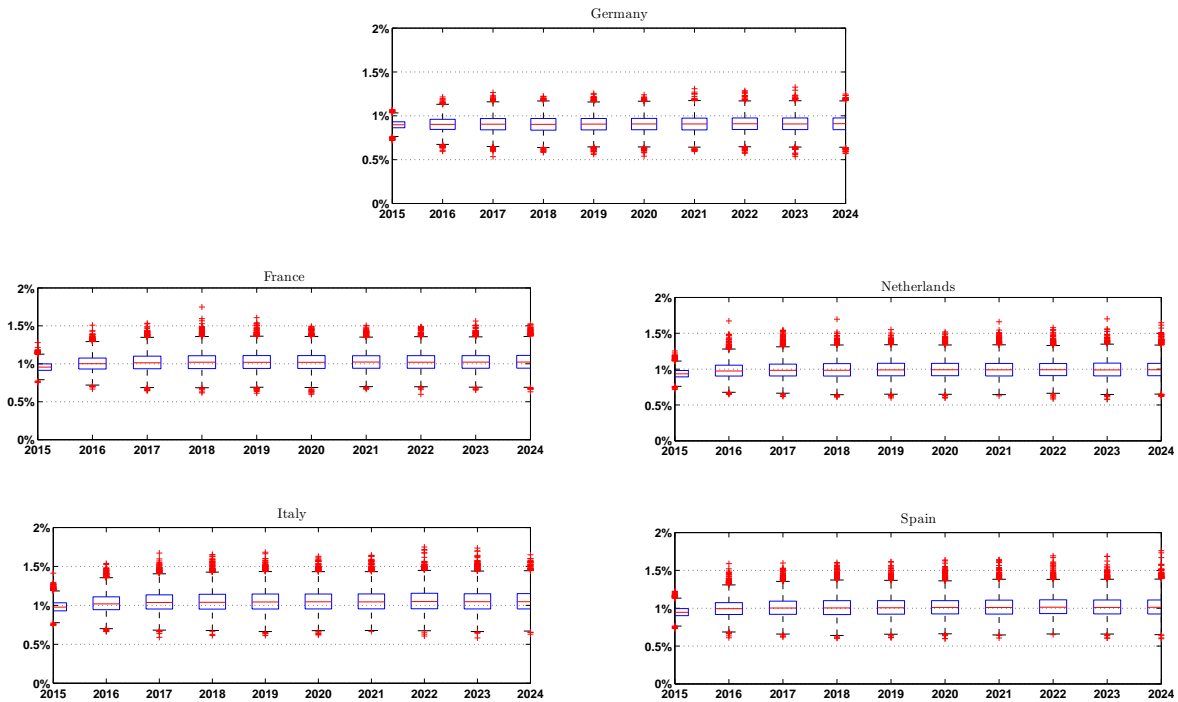


Figure 9: Adverse Scenario - 10 YTM Sovereign Bonds Yields:

The graphs show the distribution of the simulation: the central red mark is the median, the edges of the box are the 25th and 75th percentiles respectively, the whiskers extend to the most extreme data points not considered outliers whereas outliers are plotted individually.



Adverse Scenario - 10 YTM Corporate Bonds Yields

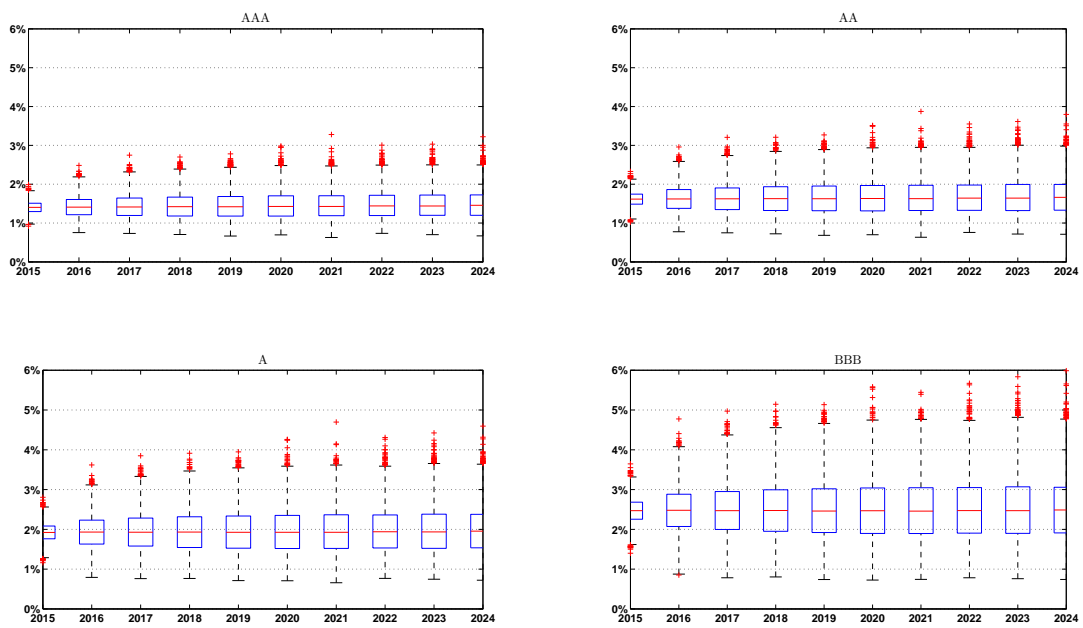
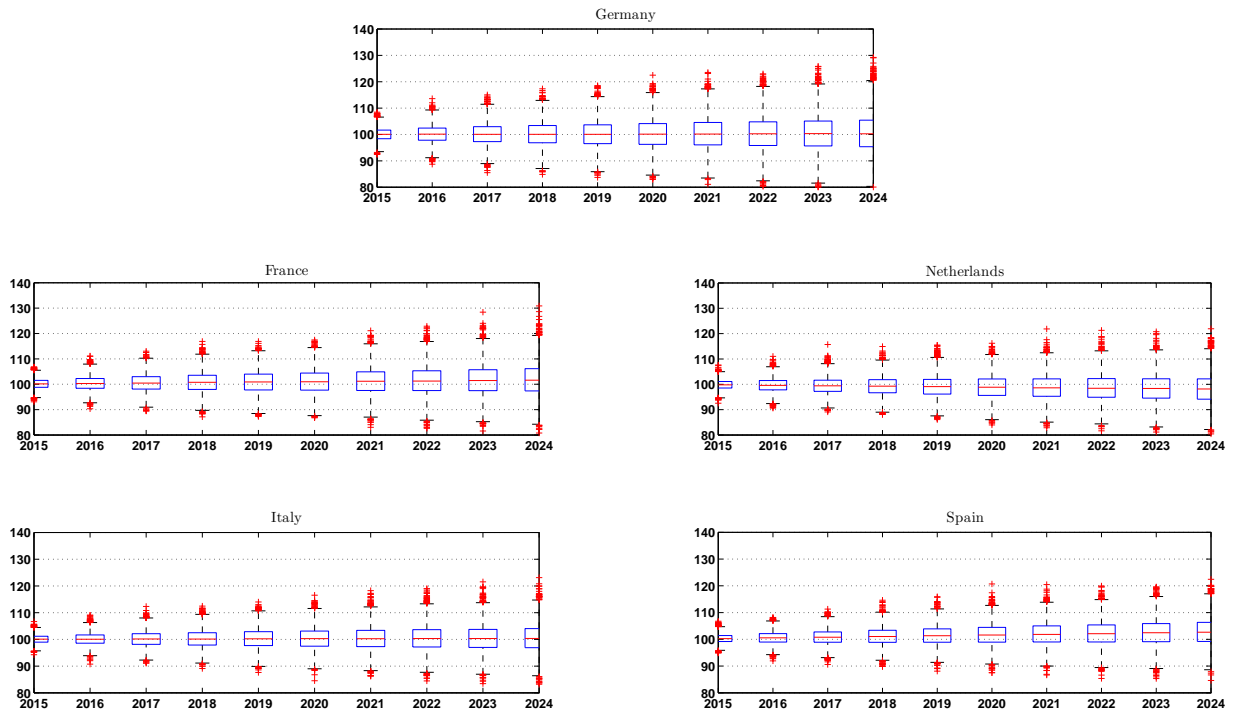


Figure 10: Adverse Scenario - Stock Indices:

The graphs show the distribution of the simulation: the central red mark is the median, the edges of the box are the 25th and 75th percentiles respectively, the whiskers extend to the most extreme data points not considered outliers whereas outliers are plotted individually.



Adverse Scenario - Real Estate Indices

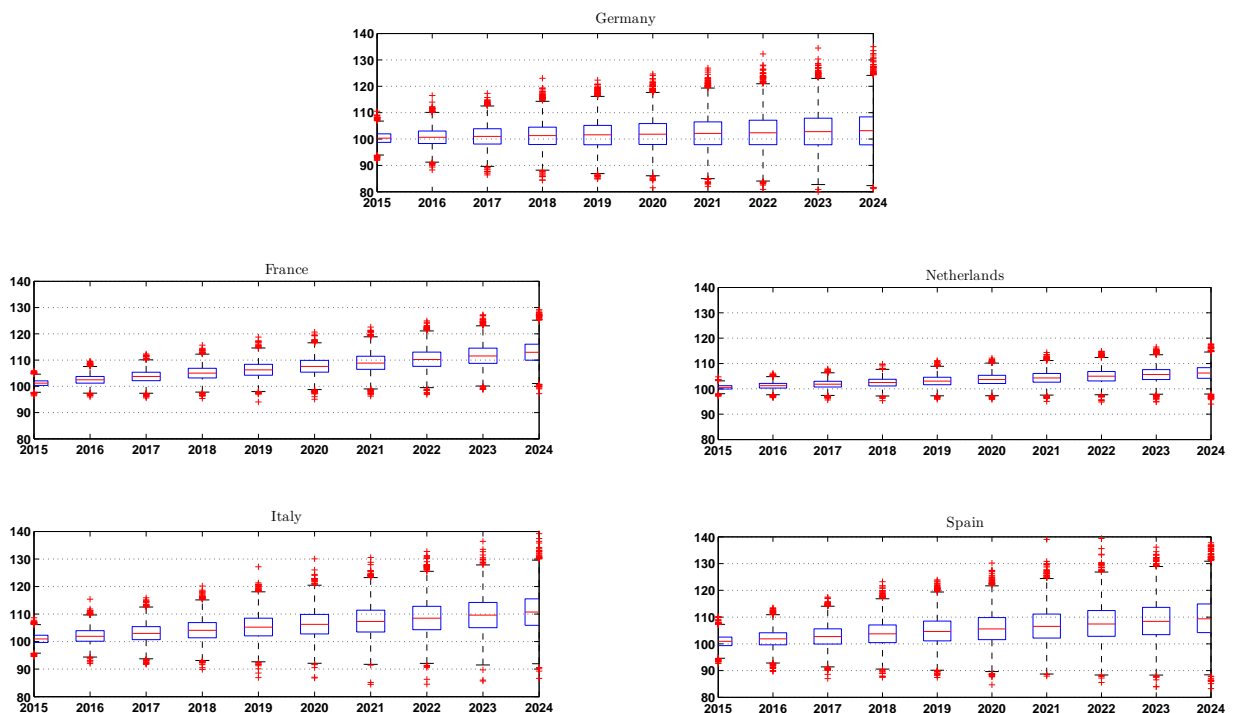
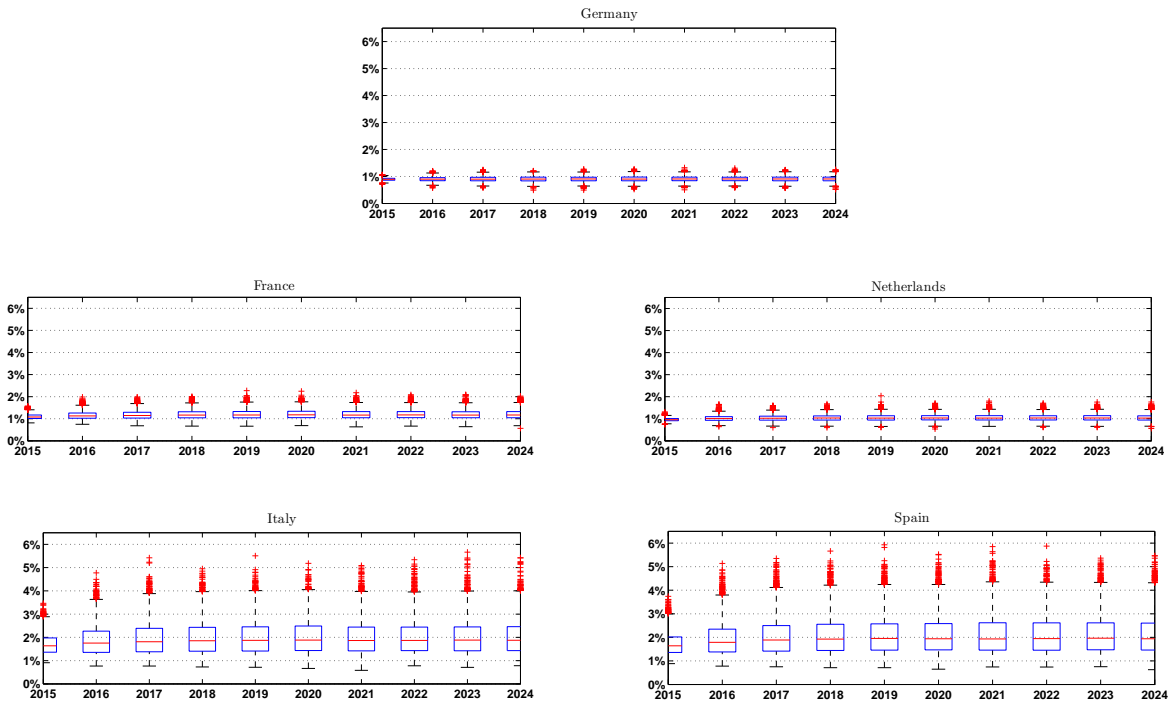


Figure 11: Severely Adverse Scenario - 10 YTM Sovereign Bonds Yields:

The graphs show the distribution of the simulation: the central red mark is the median, the edges of the box are the 25th and 75th percentiles respectively, the whiskers extend to the most extreme data points not considered outliers whereas outliers are plotted individually.



Severely Adverse Scenario - 10 YTM Corporate Bonds Yields

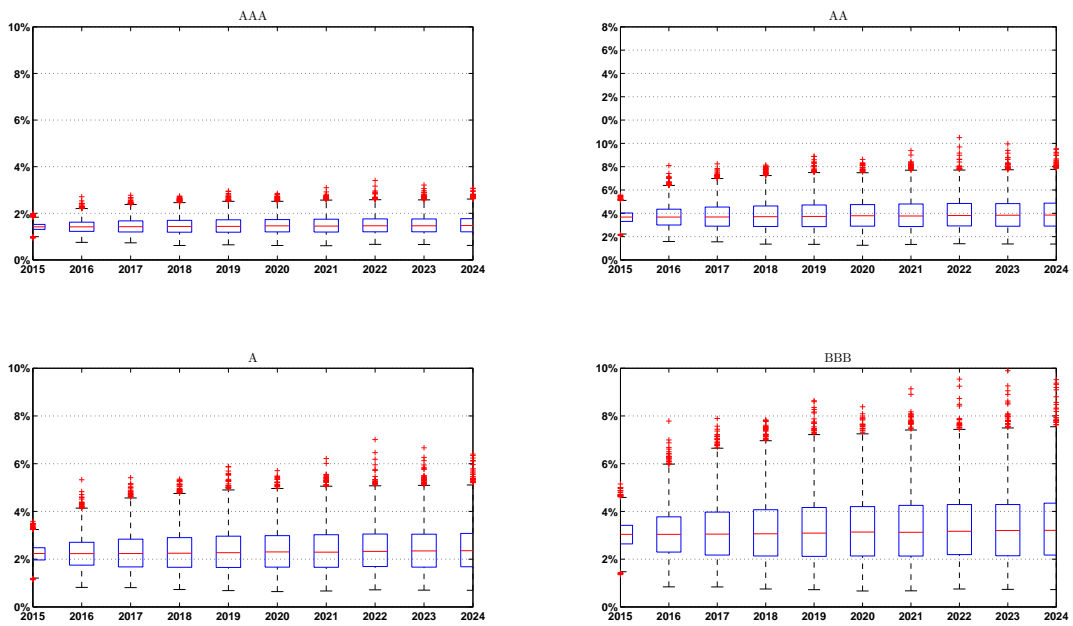
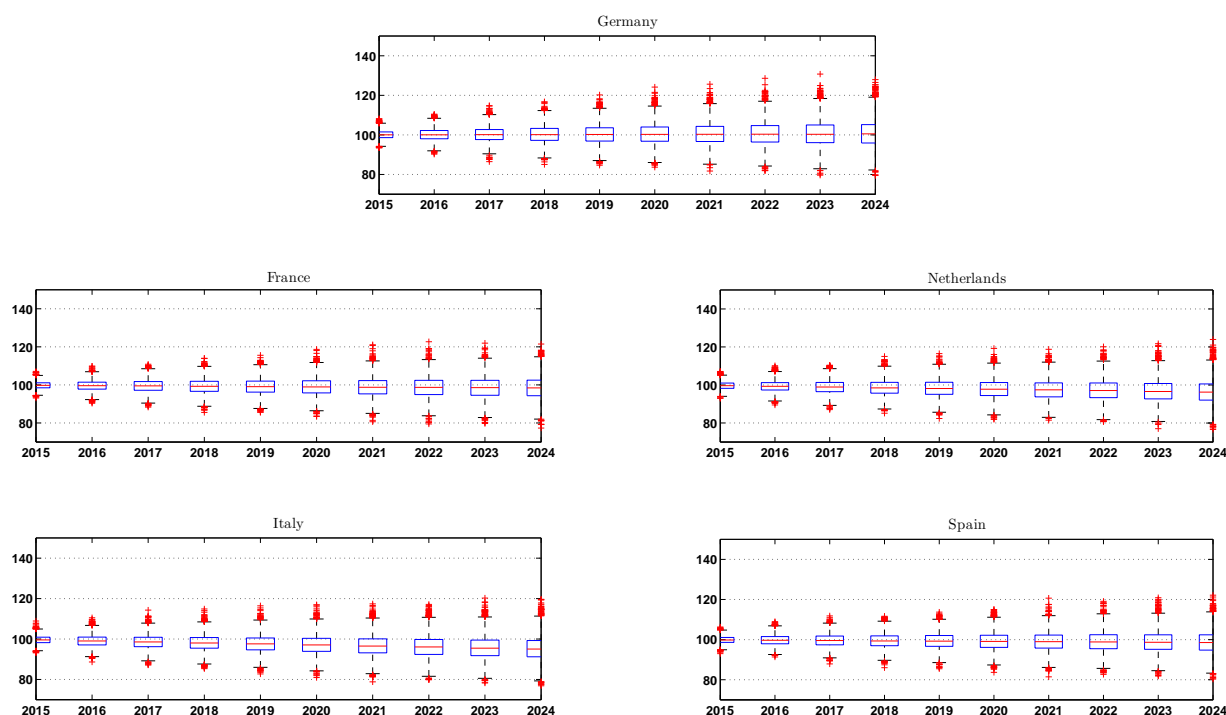


Figure 12: Severely Adverse Scenario - Stock Indices:

The graphs show the distribution of the simulation: the central red mark is the median, the edges of the box are the 25th and 75th percentiles respectively, the whiskers extend to the most extreme data points not considered outliers whereas outliers are plotted individually.



Severely Adverse Scenario - Real Estate Indices

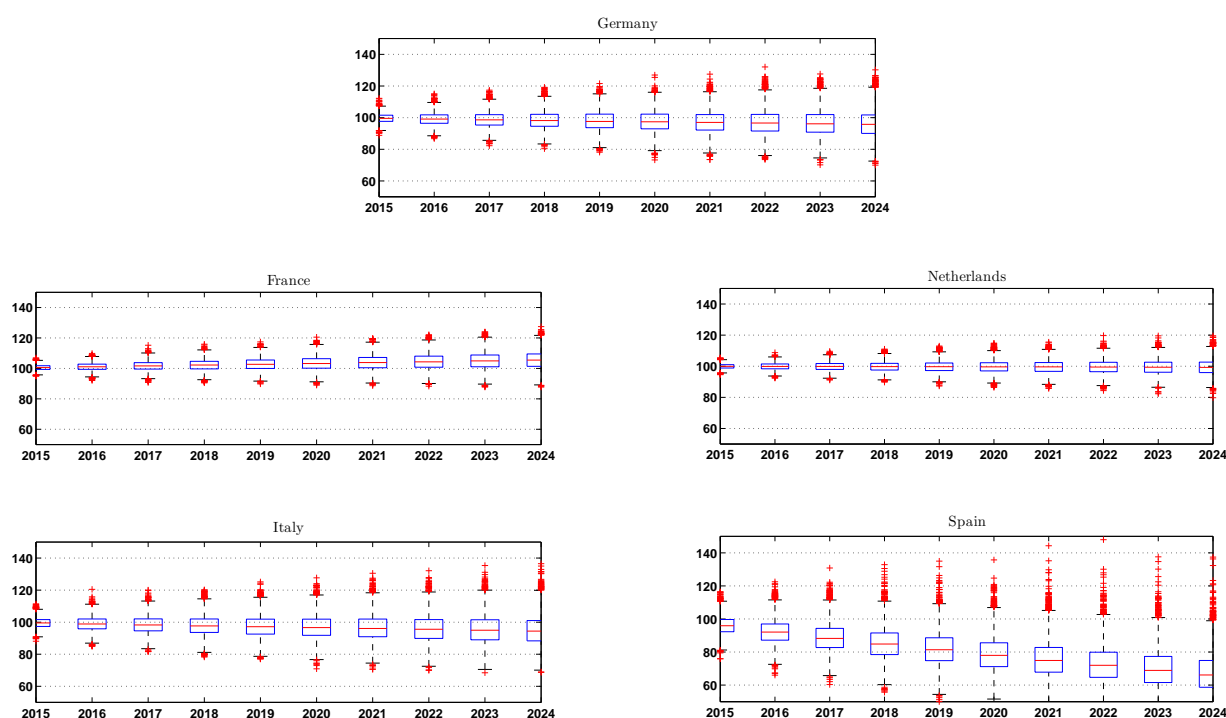


Figure 13: Results - Baseline Scenario - Specification 1: Endowment Business.

The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

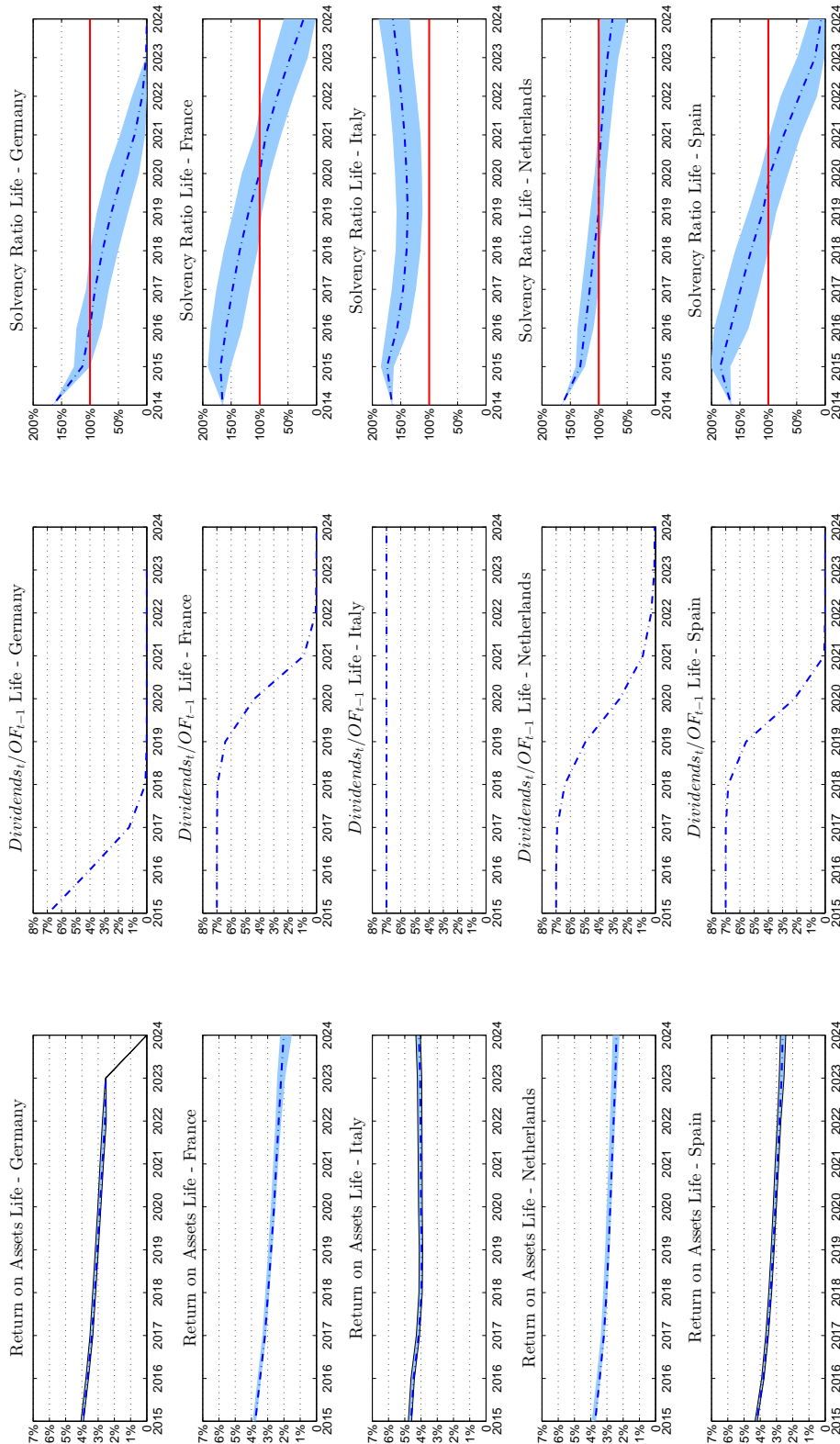


Figure 14: Results - Baseline Scenario - Specification 2: Endowment and Term Life Business.

The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

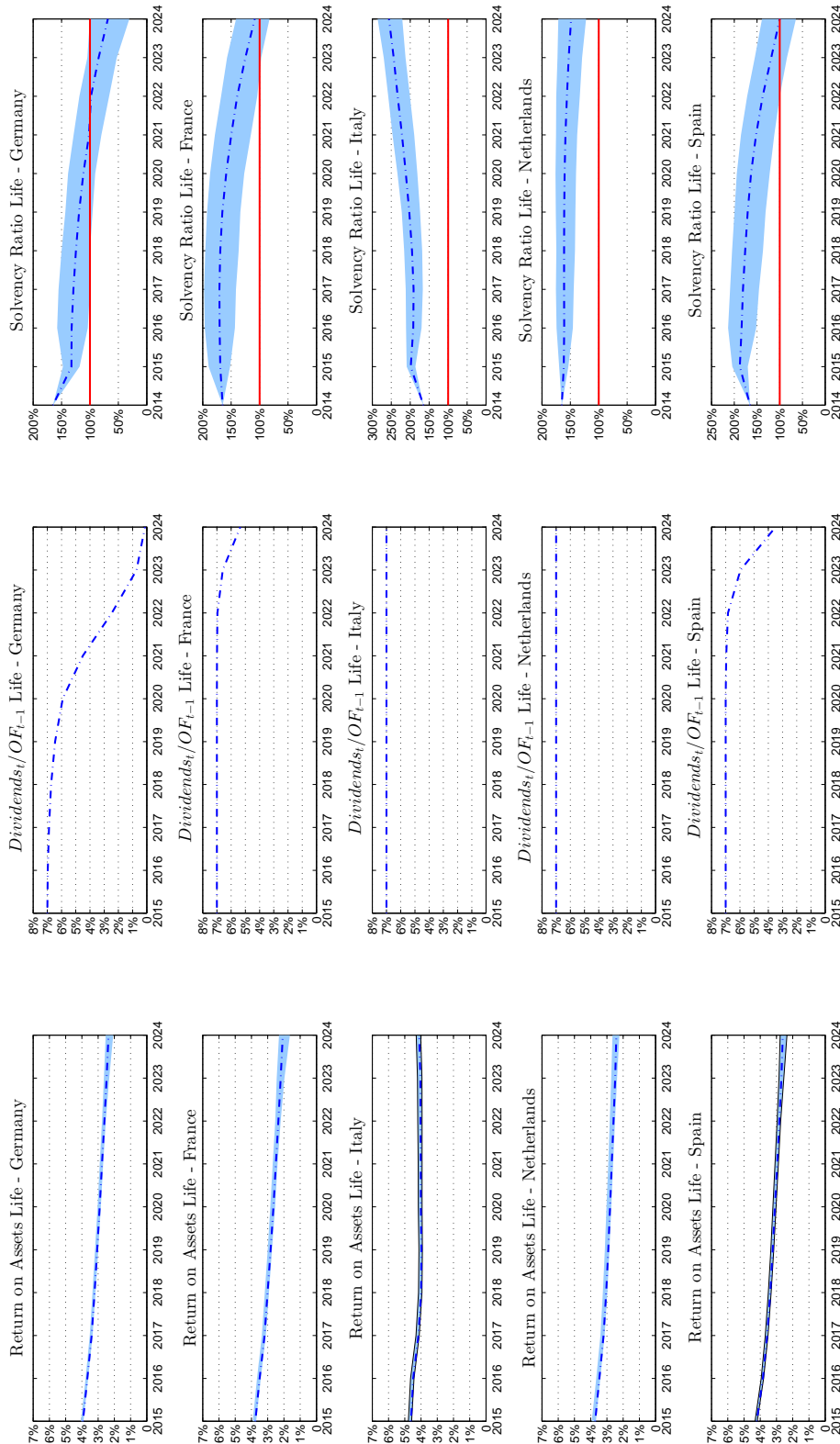


Figure 15: Results - Baseline Scenario - Specification 3: Endowment, Term Life and Annuity Business. The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

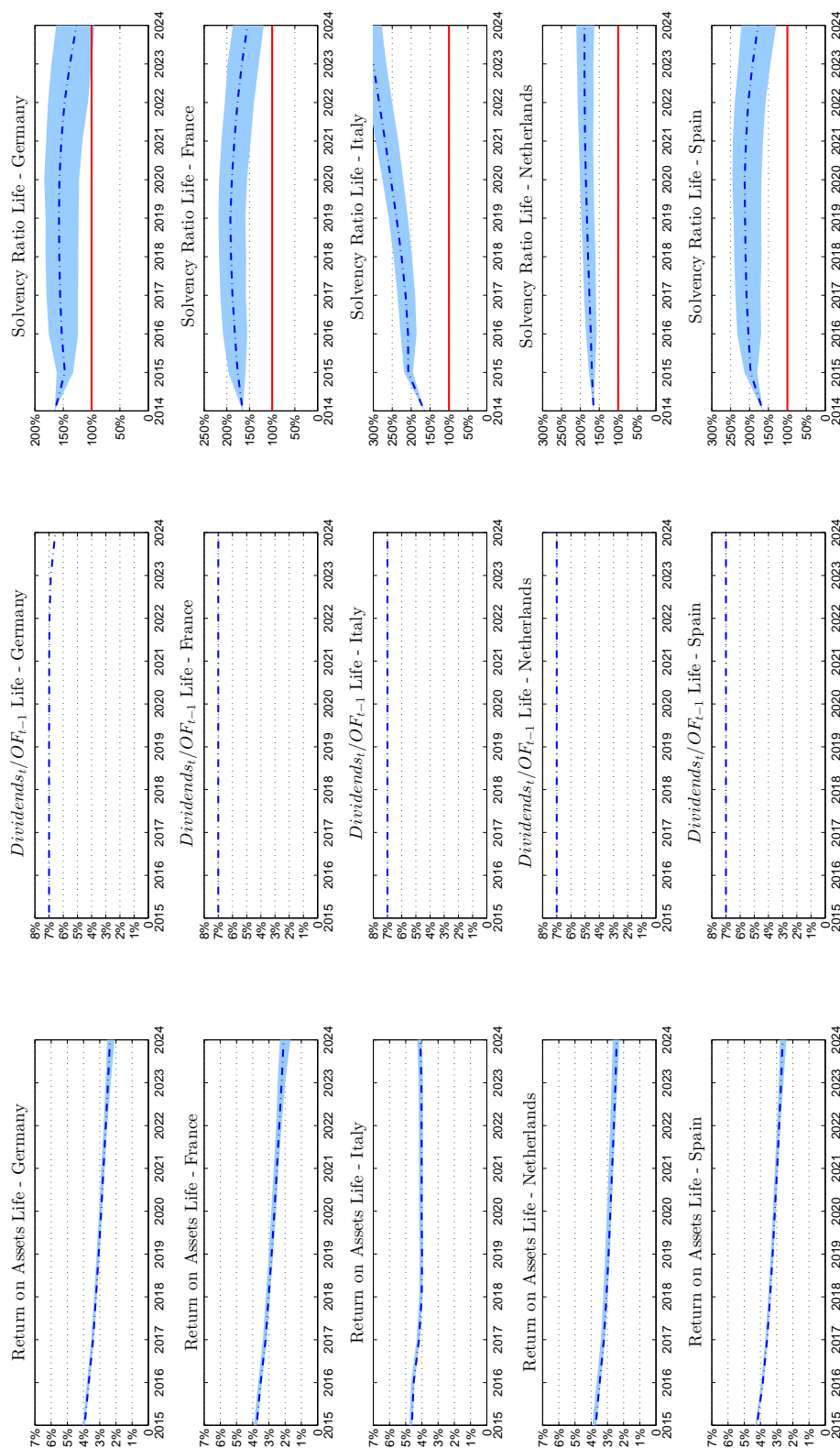


Figure 16: Results - Baseline Scenario - Specification 4: Endowment, Term Life, Annuity and Non-Life Business. The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio both for life and non-life; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

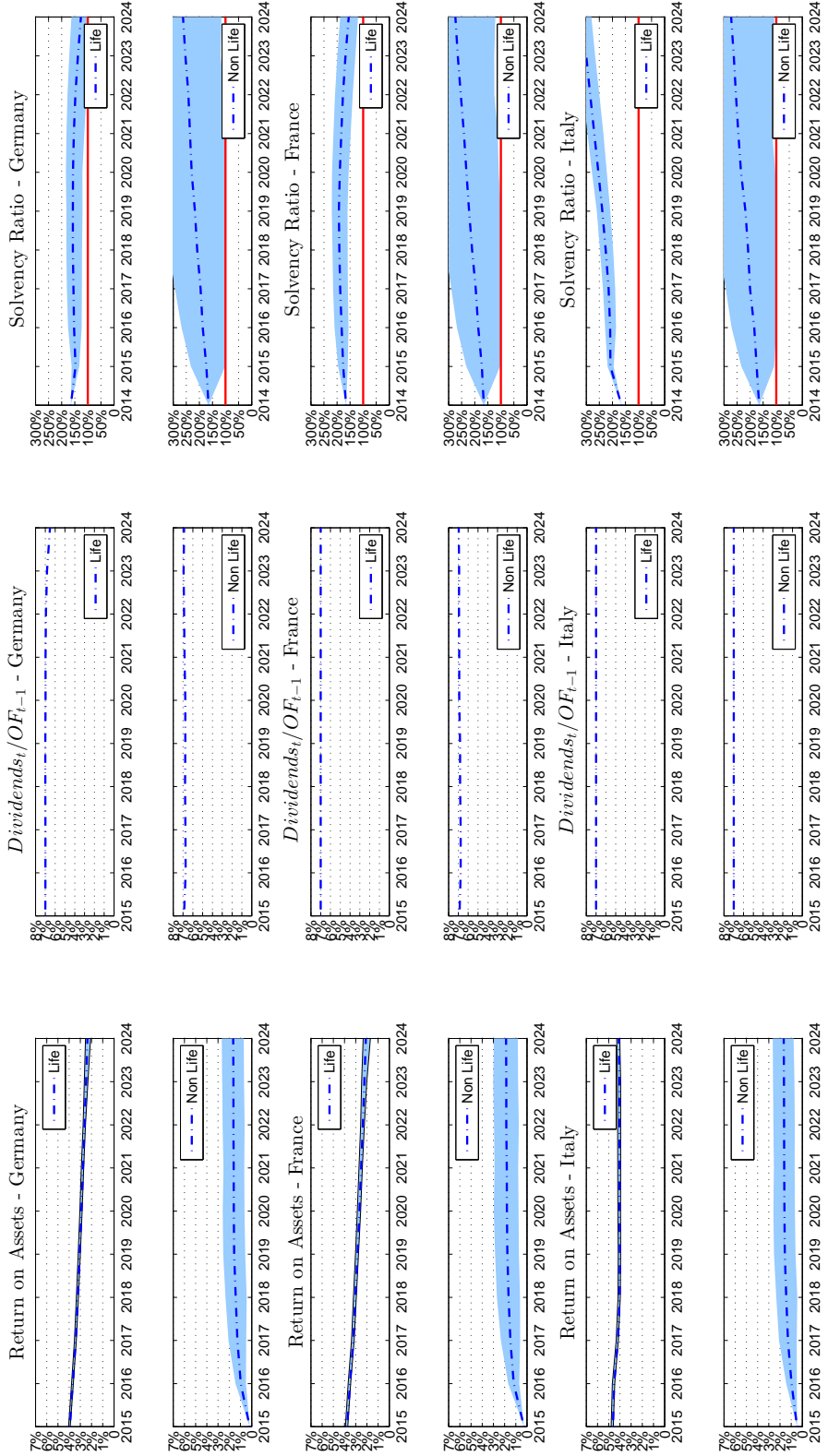


Figure 17: Results - Baseline Scenario - Specification 4: Endowment, Term Life, Annuity and Non-Life Business. The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio both for life and non-life; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

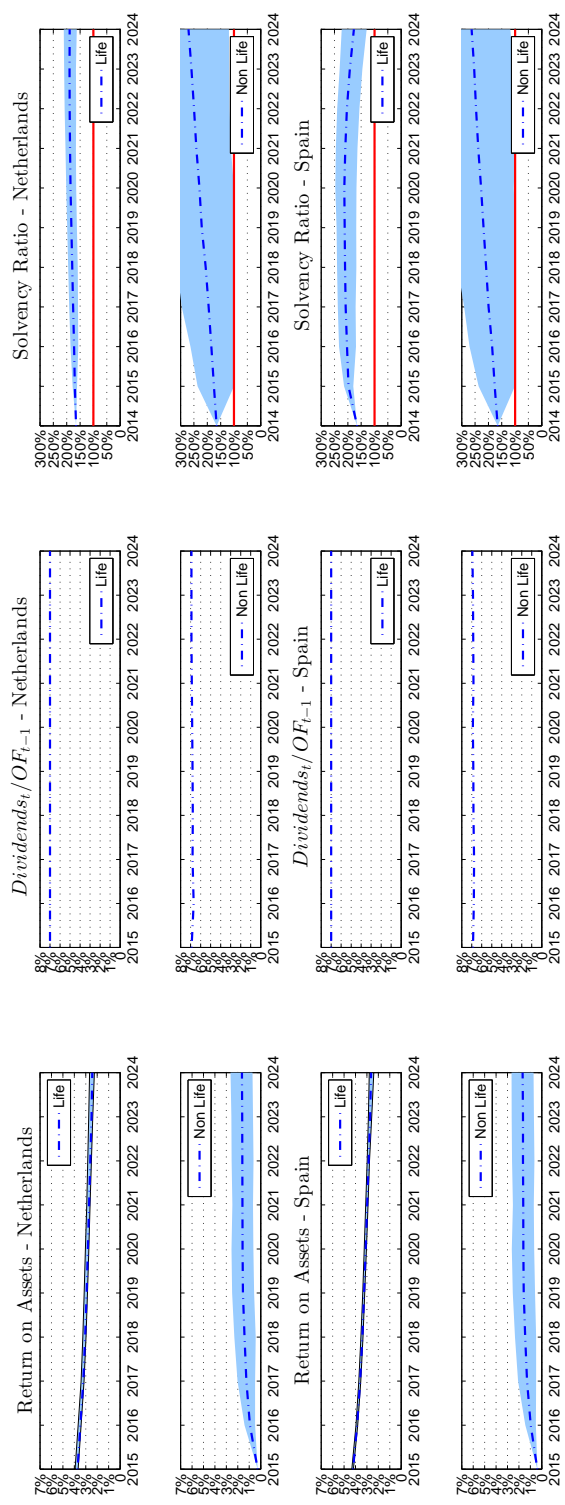


Figure 18: Results - Adverse Scenario - Specification 1: Endowment Business.

The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

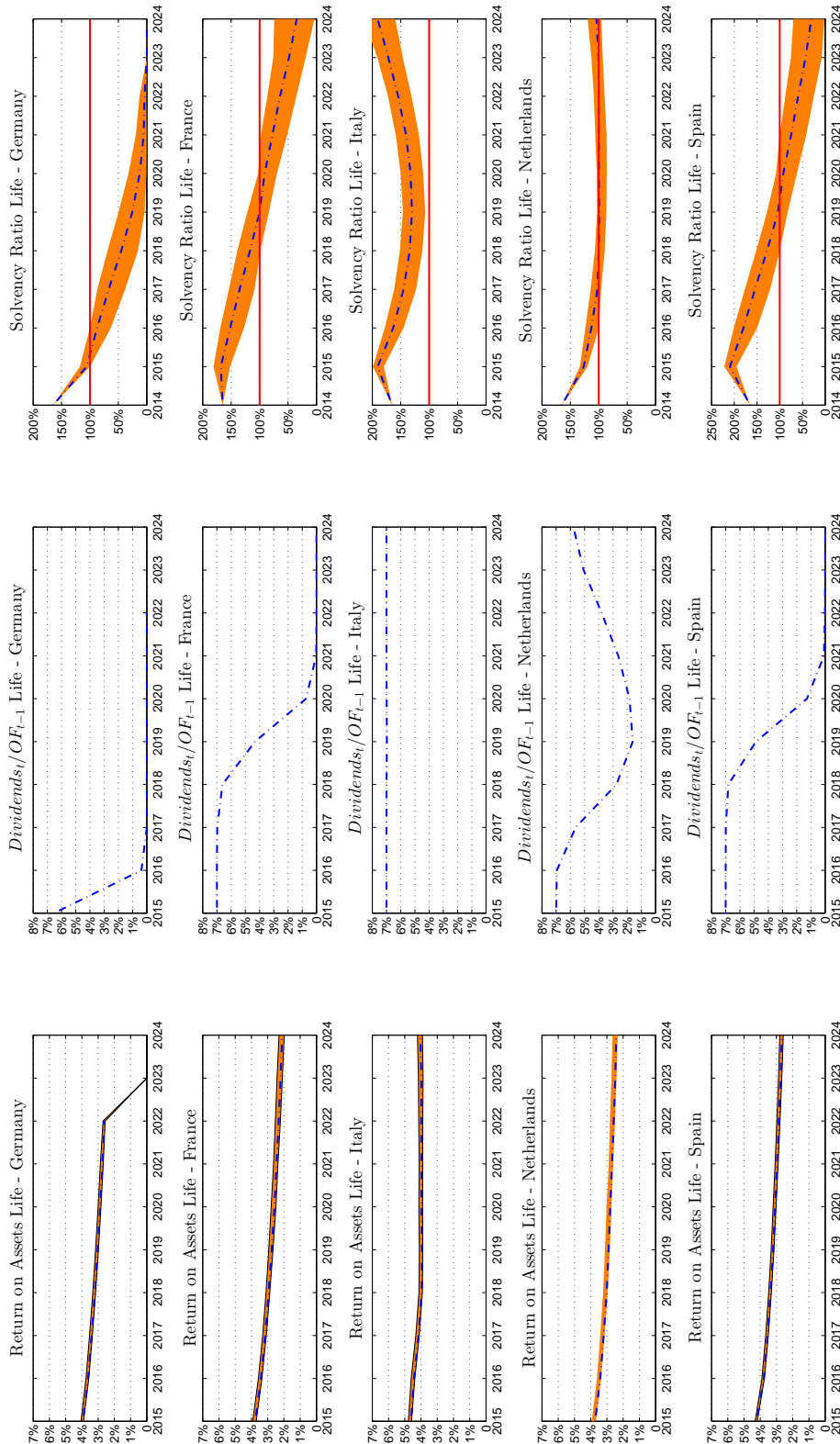


Figure 19: Results - Adverse Scenario - Specification 2: Endowment and Term Life Business.

The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

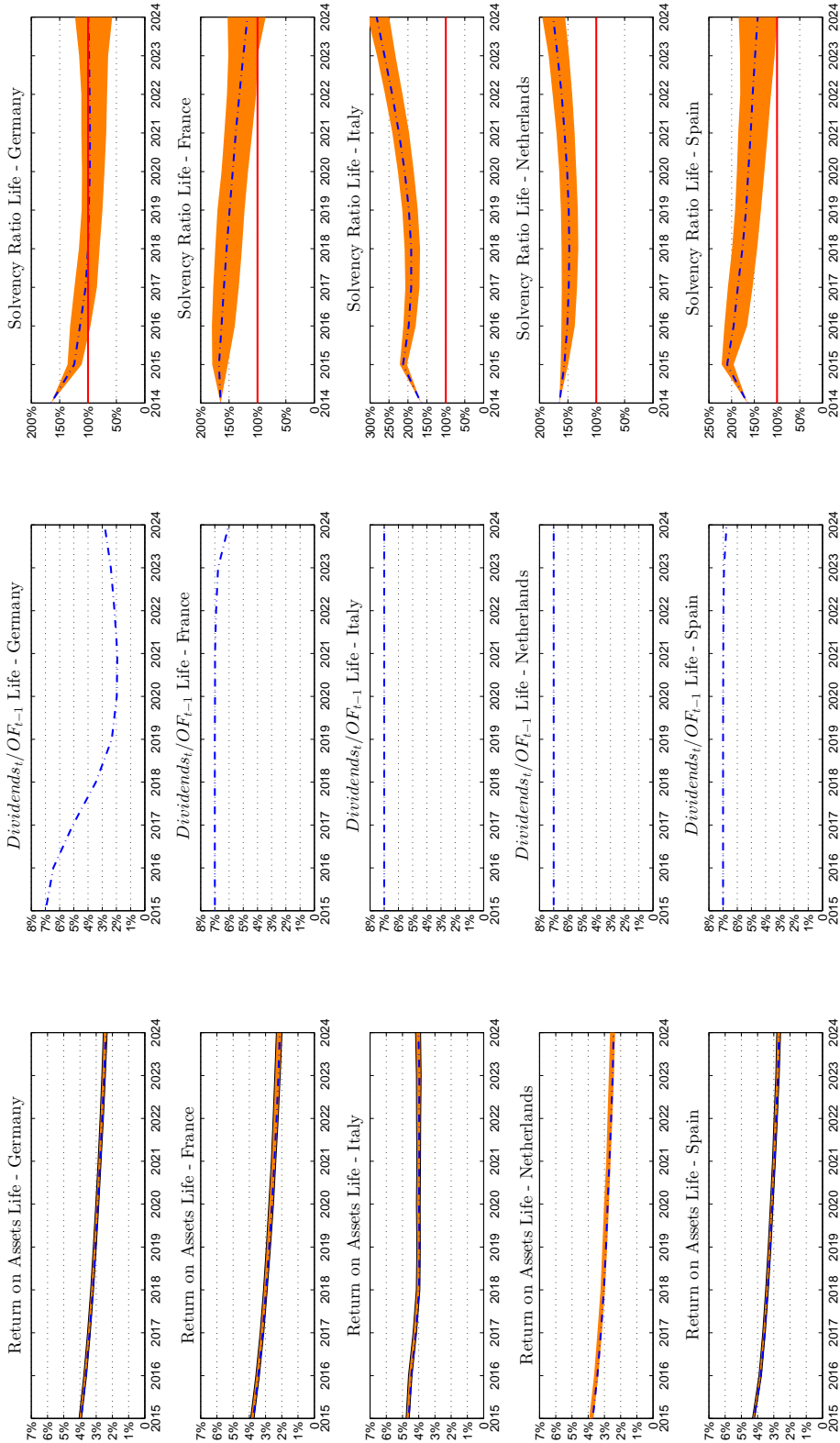


Figure 20: Results - Adverse Scenario - Specification 3: Endowment, Term Life and Annuity Business. The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

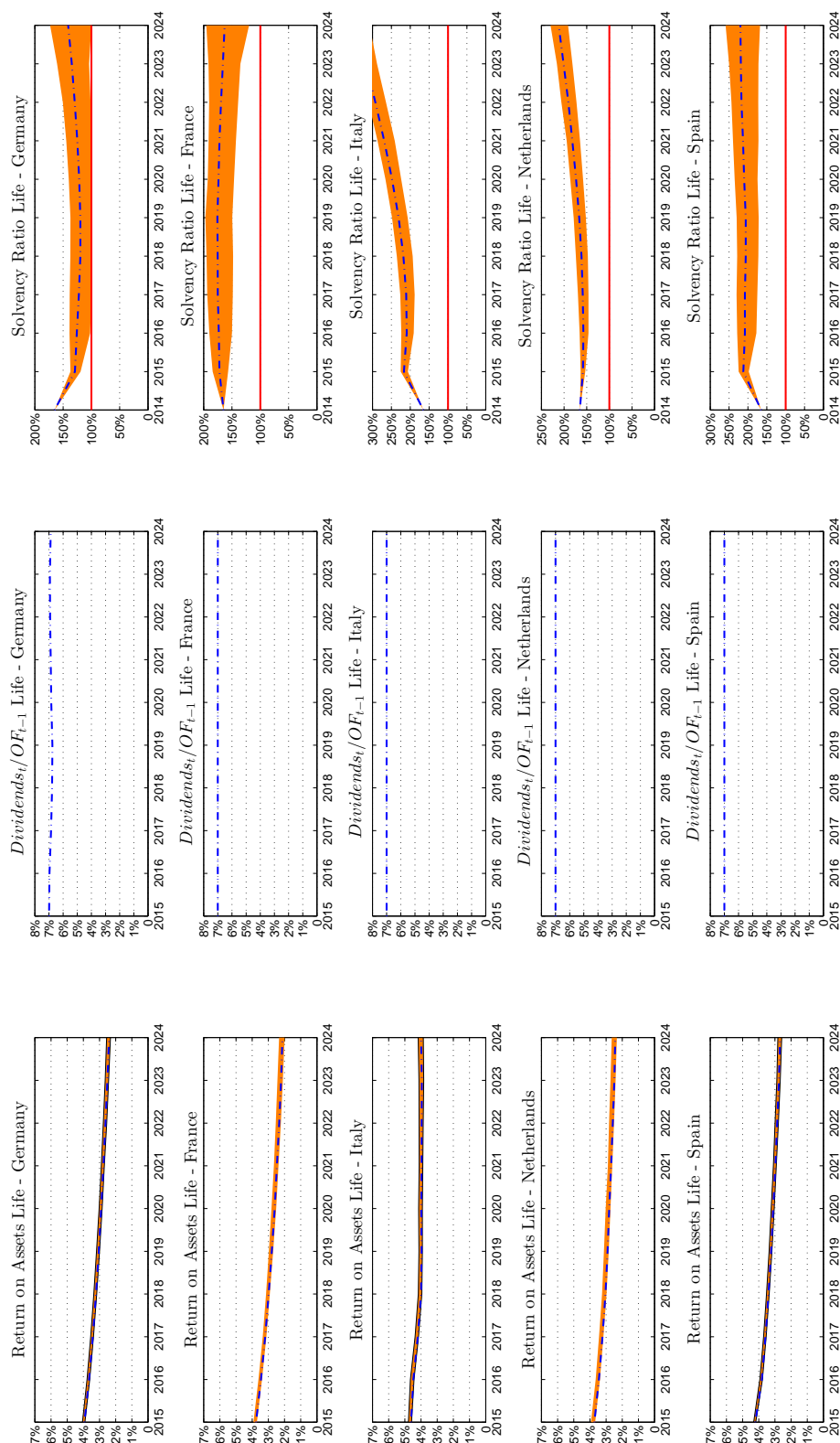


Figure 21: Results - Adverse Scenario - Specification 4: Endowment, Term Life, Annuity and Non-Life Business. The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio both for life and non-life; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

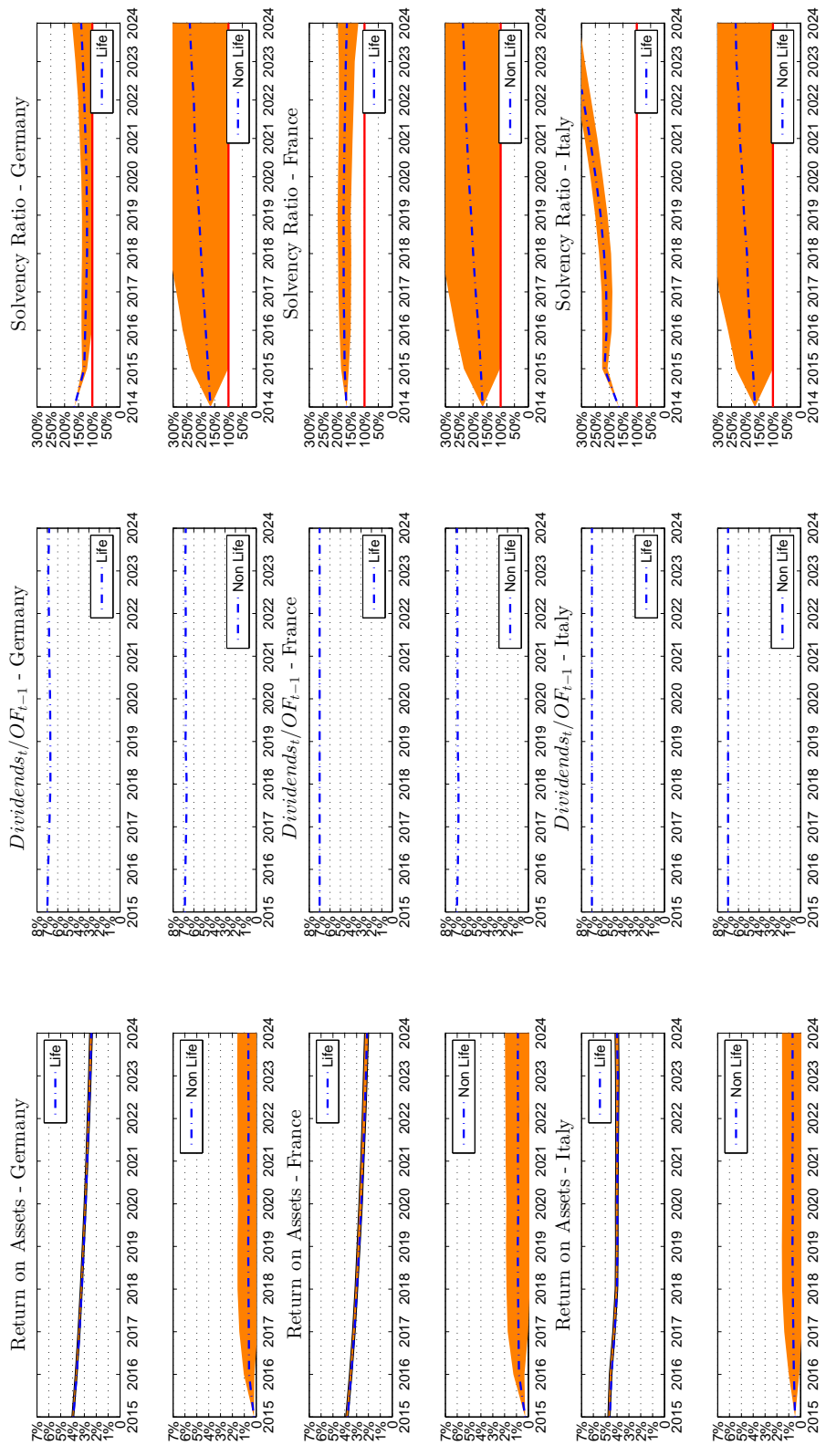


Figure 22: Results - Adverse Scenario - Specification 4: Endowment, Term Life, Annuity and Non-Life Business. The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio both for life and non-life; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

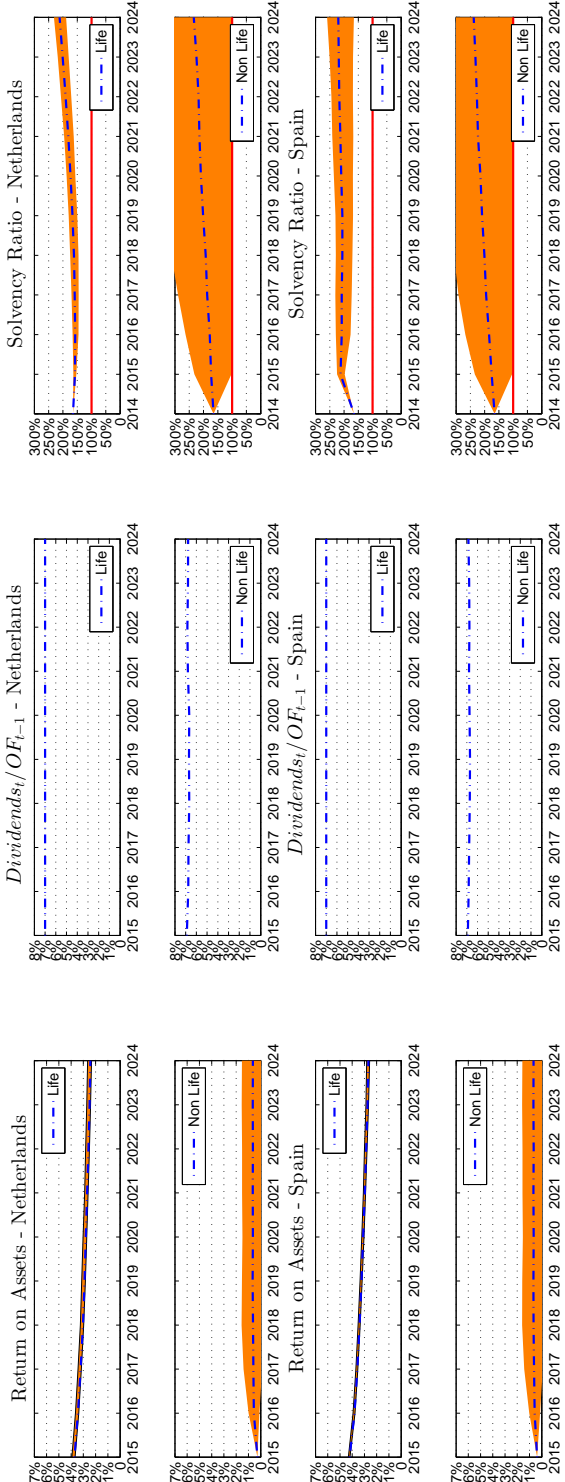


Figure 23: Results - Severely Adverse Scenario - Specification 1: Endowment Business.

The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

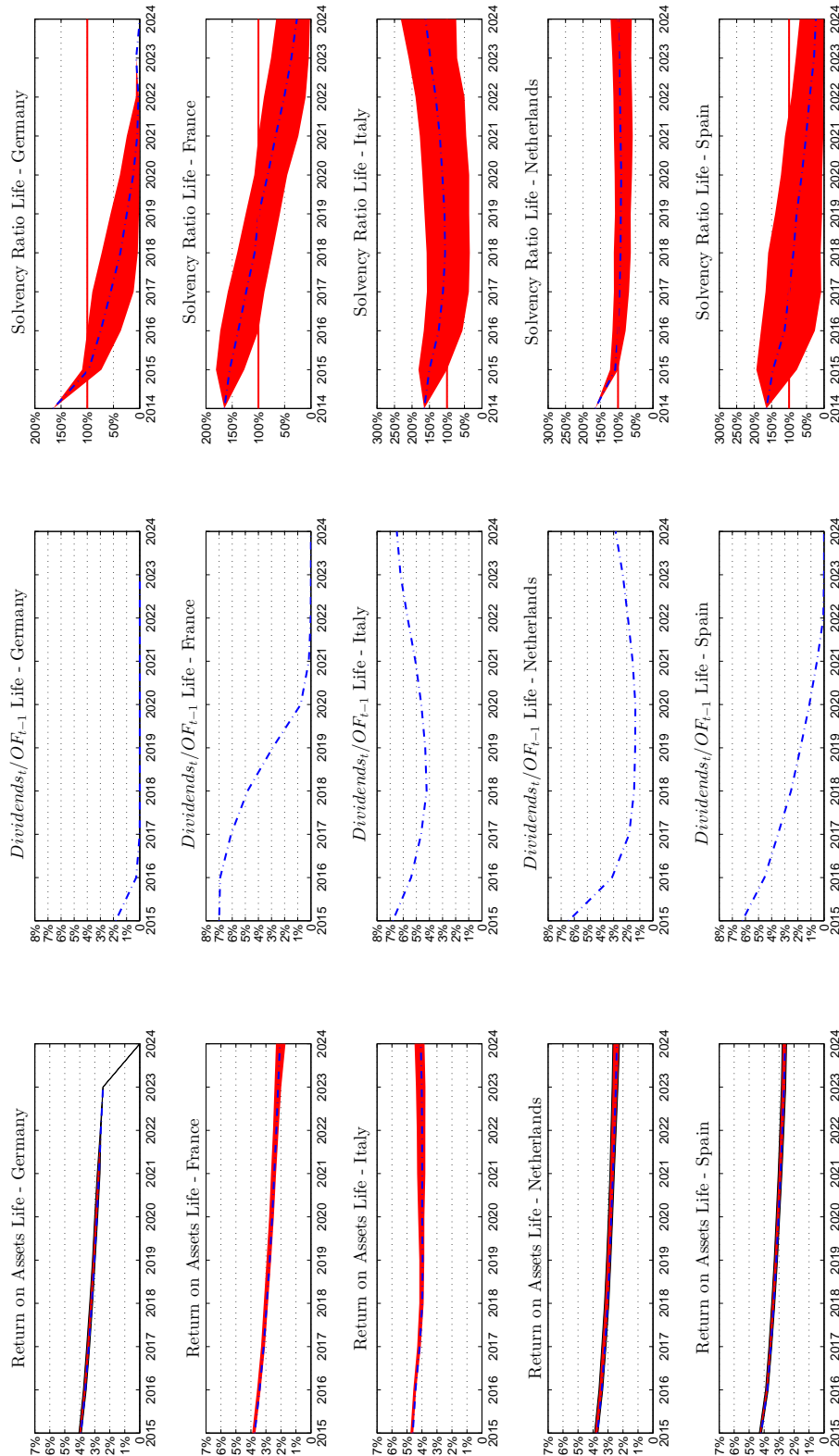


Figure 24: Results - Severely Adverse Scenario - Specification 2: Endowment and Term Life Business. The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

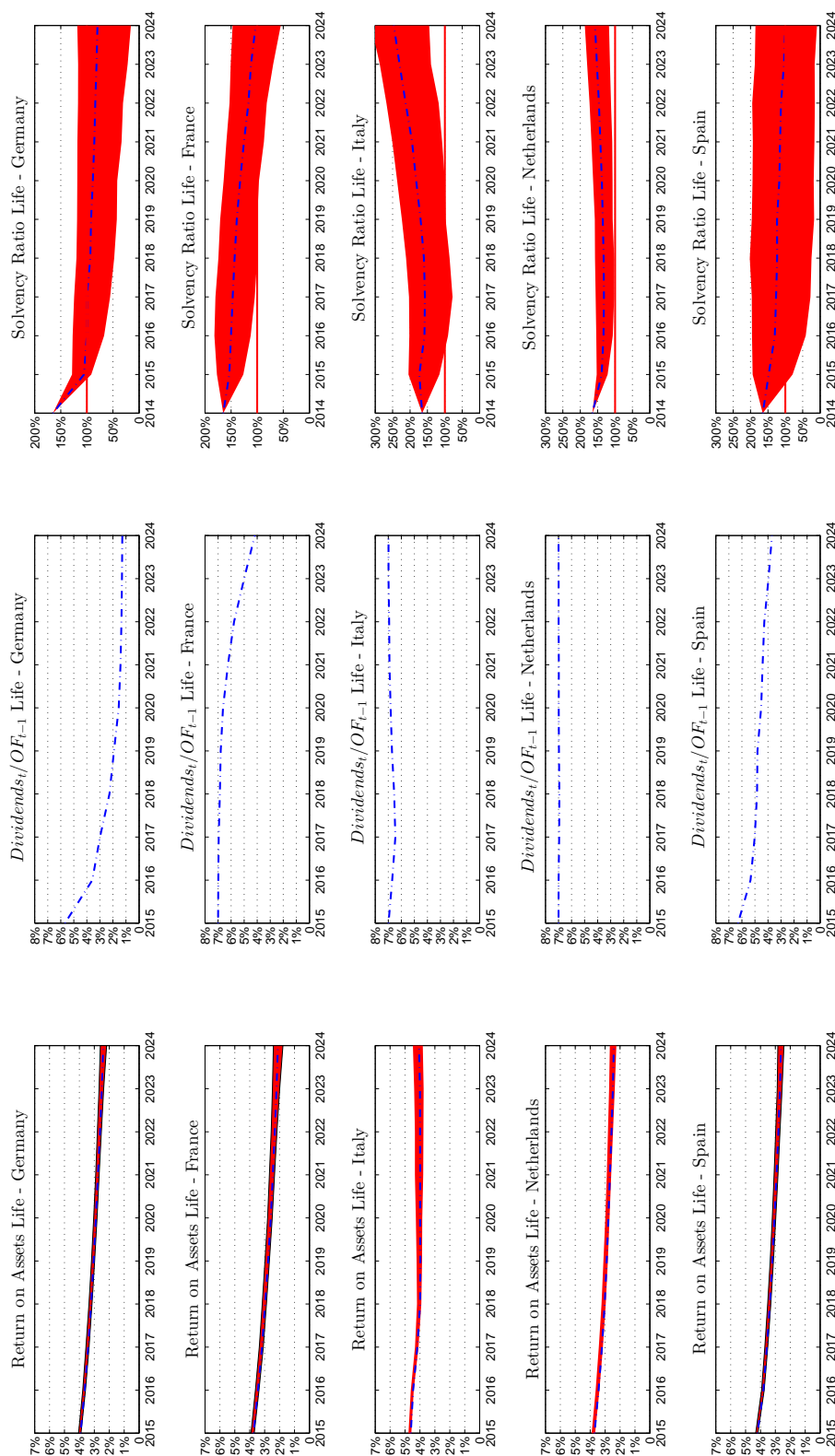


Figure 25: Results - Severely Adverse Scenario - Specification 3: Endowment, Term Life and Annuity Business. The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

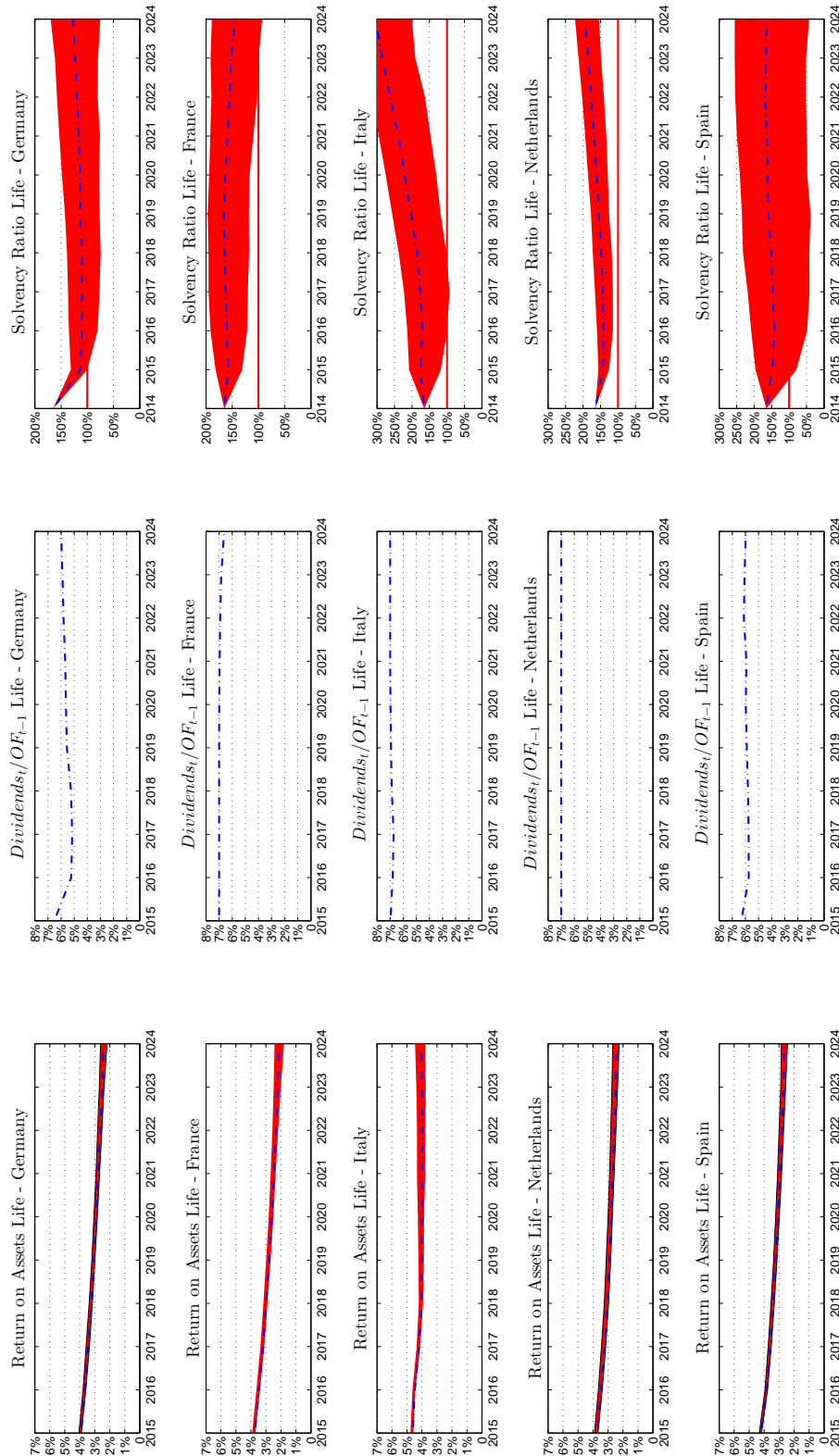


Figure 26: Results - Severely Adverse Scenario - Specification 4: Endowment, Term Life, Annuity and Non-Life Business.

The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio both for life and non-life; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

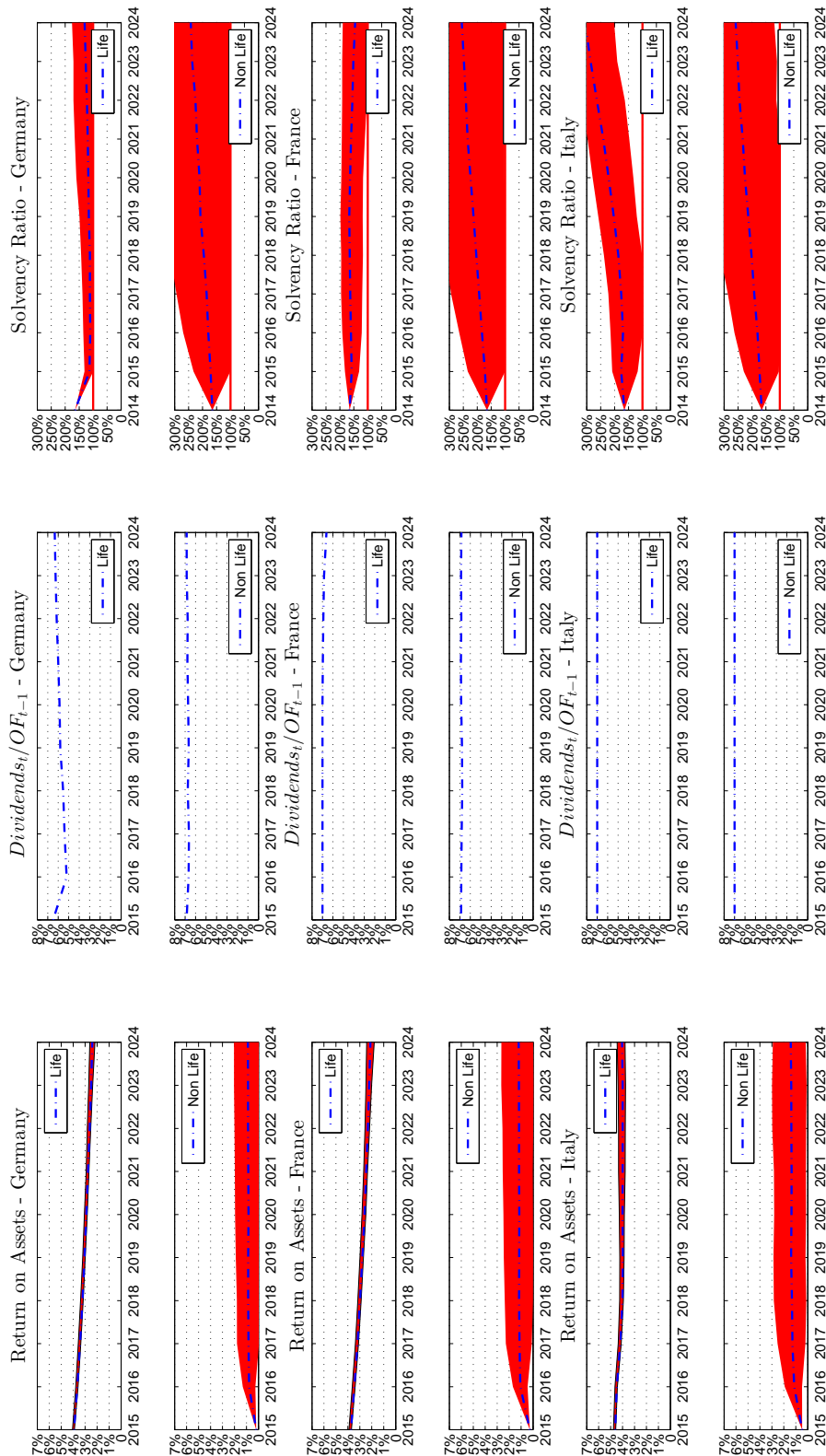


Figure 27: Results - Severely Adverse Scenario - Specification 4: Endowment, Term Life, Annuity and Non-Life Business.

The graphs show the return on assets, the return on equity ($Dividends_t/OF_{t-1}$) and the solvency ratio both for life and non-life; for the return on assets and for the solvency ratio we report the 95% confidence interval (shaded area) and the median (dotted line), whereas for the return on equity we only report the mean.

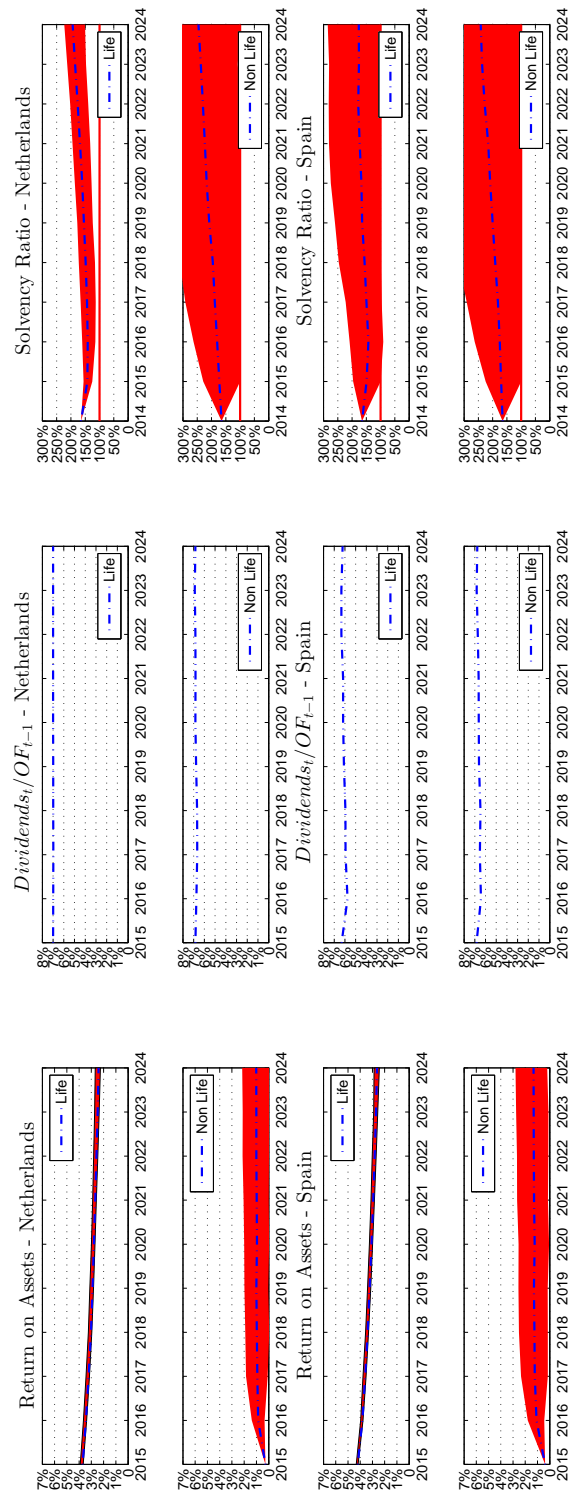
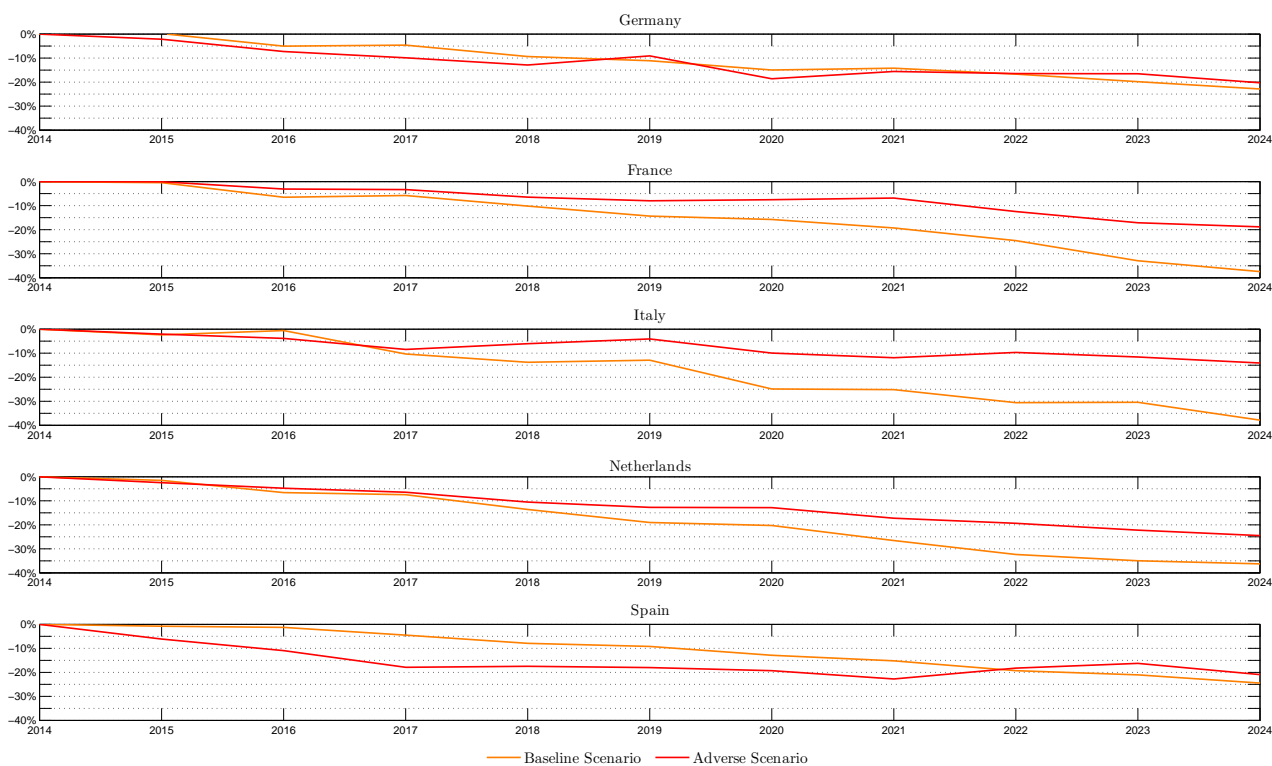


Figure 28: Median Non-Life Solvency Ratio Reduction with respect to Baseline Scenario.

The graphs show the differences between the median solvency ratio for non life under the Adverse Scenario (orange) and the Severely Adverse Scenario (red) with respect to the Baseline median solvency ratio. Figures display the absolute percentage points change in the median solvency ratio.



C Tables

Table 1: Financial Markets Dynamics: the Vasicek Model was calibrated on the EIONIA rate between January 2008 and December 2014; All other parameters under Baseline Scenario and Adverse Scenario were calibrated during the pre-crisis period, i.e. January 1999 to December 2007, whereas Severely Adverse Scenario was calibrated over the period January 1999 to December 2014. Data for Sovereign Bonds was obtained on Datastream, whereas for Corporate Bonds data were obtained from Moody's. Stocks indexes parameters were estimated from main national indexes (DAX, CAC 40, FTSE-MIB, AEX and IBEX 35), whereas Real Estate parameters were estimated on national REIT indexes. All series are at monthly frequency. Parameters for Sovereign bonds and Corporate bonds are obtained by constructing a series generated by the mean across maturities of the spread versus the German yield curve.

| | Baseline Scenario | | Adverse Scenario | | Severely Adverse Scenario | |
|------------------------|-------------------|----------|------------------|----------|---------------------------|----------|
| Vasicek Model | | | | | | |
| r_0 | -0.08% | | -0.08% | | -0.08% | |
| k | 0.5462 | | 0.5462 | | 0.5462 | |
| σ_r | 0.61% | | 0.61% | | 0.61% | |
| λ | -1 | | -1 | | -1 | |
| θ | 1% | | 0% | | 0% | |
| | μ | σ | μ | σ | μ | σ |
| Sovereign Bonds | | | | | | |
| Germany | 0% | 0% | 0% | 0% | 0% | 0% |
| France | 0.01% | 0.18% | 0.01% | 0.18% | 0.17% | 0.31% |
| Italy | 0.05% | 0.19% | 0.05% | 0.19% | 0.72% | 1.12% |
| Netherlands | -0.08% | 0.18% | -0.08% | 0.18% | -0.02% | 0.22% |
| Spain | -0.06% | 0.20% | -0.06% | 0.20% | 0.71% | 1.28% |
| Corporate Bonds | | | | | | |
| AAA | 0.50% | 0.28% | 0.50% | 0.28% | 0.51% | 0.29% |
| AA | 0.72% | 0.35% | 0.72% | 0.35% | 0.92% | 0.52% |
| A | 1.02% | 0.44% | 1.02% | 0.44% | 1.31% | 0.74% |
| BBB | 1.57% | 0.59% | 1.57% | 0.59% | 2.11% | 1.15% |
| Stocks | | | | | | |
| Germany | 4.40% | 28.26% | 4.40% | 28.26% | 3.98% | 25.81% |
| France | 4.60% | 24.09% | 4.60% | 24.09% | 0.83% | 23.68% |
| Italy | 2.54% | 20.09% | 2.54% | 20.09% | -2.91% | 24.52% |
| Netherlands | 0.38% | 23.09% | 0.38% | 23.09% | -1.34% | 25.04% |
| Spain | 5.09% | 19.56% | 5.09% | 19.56% | 0.68% | 22.14% |
| Real Estate | | | | | | |
| Germany | 7.66% | 28.93% | 7.66% | 28.93% | 0.74% | 34.51% |
| France | 15.71% | 15.53% | 15.71% | 15.53% | 8.64% | 21.39% |
| Italy | 15.04% | 23.73% | 15.04% | 23.73% | 0.60% | 38.38% |
| Netherlands | 7.99% | 11.41% | 7.99% | 11.41% | 1.01% | 19.25% |
| Spain | 14.63% | 27.80% | 14.63% | 27.80% | -25.63% | 68.69% |

Table 2: Correlations: Baseline Scenario and Adverse Scenario were calibrated during the pre-crisis period, i.e. January 1999 to December 2007, whereas Severely Adverse Scenario was calibrated over the period January 1999 to December 2014. Data for Sovereign Bonds was obtained on Datastream, whereas for Corporate Bonds data were obtained from Moody's. Stocks indexes parameters were estimated from main national indexes (DAX, CAC 40, FTSE-MIB, AEX and IBEX 35), whereas Real Estate parameters were estimated on national REIT indexes. All series are at monthly frequency. Coefficients were computed on first differences, i.e. $\frac{x_t - x_{t-1}}{x_{t-1}}$: correlations between the German sovereign and dr (i.e. the overnight rate) was set to 0 since the term structure is generated directly by the Vasicek model; correlation for all other sovereign was computed by constructing a series generated by the mean across maturities of the spread versus the German yield curve; correlations for corporate bonds for computed by constructing a series generated by the mean of A-rated corporate bonds across maturities of the spread versus the German yield curve.

| | scenario 1 | | | | | scenario 2 | | | | | scenario 3 | | | | |
|-------------|-------------|-------------|-------------|--------|-----------|------------|-------------|-------------|--------|-----------|------------|-------------|-------------|--------|-----------|
| | dr | $d\delta_g$ | $d\delta_c$ | dS_s | dS_{re} | dr | $d\delta_g$ | $d\delta_c$ | dS_s | dS_{re} | dr | $d\delta_g$ | $d\delta_c$ | dS_s | dS_{re} |
| Germany | dr | 1 | - | - | - | 1 | - | - | - | - | 1 | - | - | - | - |
| | $d\delta_g$ | 0 | 1 | - | - | 0 | 1 | - | - | 0 | 1 | - | - | - | - |
| | $d\delta_c$ | 0.059 | 0 | 1 | - | 0.059 | 0 | 1 | - | 0.080 | 0 | 1 | - | - | - |
| | dS_s | 0.018 | 0 | -0.019 | 1 | 0.018 | 0 | -0.019 | 1 | 0.169 | 0 | -0.270 | 1 | - | - |
| | dS_{re} | 0.026 | 0 | 0.061 | 0.534 | 1 | 0.026 | 0 | 0.061 | 0.534 | 1 | 0.174 | 0 | -0.205 | 0.545 |
| France | dr | 1 | - | - | - | 1 | - | - | - | - | 1 | - | - | - | - |
| | $d\delta_g$ | -0.083 | 1 | - | - | -0.083 | 1 | - | - | -0.114 | 1 | - | - | - | - |
| | $d\delta_c$ | 0.059 | 0.040 | 1 | - | 0.059 | 0.040 | 1 | - | 0.080 | 0.021 | 1 | - | - | - |
| | dS_s | 0.017 | 0.117 | -0.010 | 1 | 0.017 | 0.117 | -0.010 | 1 | 0.219 | 0.033 | -0.297 | 1 | - | - |
| | dS_{re} | -0.062 | 0.164 | -0.087 | 0.394 | 1 | -0.062 | 0.164 | -0.087 | 0.394 | 1 | 0.178 | 0.033 | -0.368 | 0.594 |
| Italy | dr | 1 | - | - | - | 1 | - | - | - | - | 1 | - | - | - | - |
| | $d\delta_g$ | 0.043 | 1 | - | - | 0.043 | 1 | - | - | 0.015 | 1 | - | - | - | - |
| | $d\delta_c$ | 0.059 | 0.037 | 1 | - | 0.059 | 0.037 | 1 | - | 0.080 | 0.023 | 1 | - | - | - |
| | dS_s | 0.010 | -0.024 | -0.036 | 1 | 0.010 | -0.024 | -0.036 | 1 | 0.234 | -0.008 | -0.328 | 1 | - | - |
| | dS_{re} | -0.086 | -0.026 | -0.075 | 0.540 | 1 | -0.086 | -0.026 | -0.075 | 0.540 | 1 | 0.083 | -0.022 | -0.404 | 0.549 |
| Netherlands | dr | 1 | - | - | - | 1 | - | - | - | - | 1 | - | - | - | - |
| | $d\delta_g$ | 0.200 | 1 | - | - | 0.200 | 1 | - | - | 0.035 | 1 | - | - | - | - |
| | $d\delta_c$ | 0.059 | 0.060 | 1 | - | 0.059 | 0.060 | 1 | - | 0.080 | 0.035 | 1 | - | - | - |
| | dS_s | 0.024 | 0.065 | -0.048 | 1 | 0.024 | 0.065 | -0.048 | 1 | 0.149 | 0.059 | -0.385 | 1 | - | - |
| | dS_{re} | -0.081 | -0.086 | -0.044 | 0.422 | 1 | -0.081 | -0.086 | -0.044 | 0.422 | 1 | 0.198 | 0.046 | -0.315 | 0.555 |
| Spain | dr | 1 | - | - | - | 1 | - | - | - | - | 1 | - | - | - | - |
| | $d\delta_g$ | 0.103 | 1 | - | - | 0.103 | 1 | - | - | 0.060 | 1 | - | - | - | - |
| | $d\delta_c$ | 0.059 | -0.049 | 1 | - | 0.059 | -0.049 | 1 | - | 0.080 | 0.058 | 1 | - | - | - |
| | dS_s | 0.035 | 0.006 | 0.010 | 1 | 0.035 | 0.006 | 0.010 | 1 | 0.189 | 0.005 | -0.284 | 1 | - | - |
| | dS_{re} | -0.112 | -0.103 | 0.022 | 0.407 | 1 | -0.112 | -0.103 | 0.022 | 0.407 | 1 | 0.138 | -0.071 | -0.158 | 0.272 |

Table 3: Lee-Carter Model: all parameters were estimated on the country (yearly) mortality data, i.e. central death rates, exposure to risk and number of deaths, from 1956 to 2013, males only. Source: [The Human Mortality Database](#).

| | α (<i>s.e.</i>) | σ_k (<i>s.e.</i>) |
|-------------|-----------------------------|-------------------------------|
| Germany | -1.7623 (0.3704) | 2.7352 (1.4585) |
| France | -1.6367 (0.3574) | 2.7614 (1.2293) |
| Italy | -1.9097 (0.4030) | 3.0814 (1.7774) |
| Netherlands | -1.3806 (0.3473) | 2.6221 (1.4513) |
| Spain | -1.7275 (0.4620) | 3.4860 (1.7392) |

Adverse Selection (Gatzert and Wesker, 2012)

| | | | |
|--------------------|-------------------|--------------------|------------------------|
| $\phi_1 = -0.0275$ | $\phi_2 = 1.1618$ | $\phi_3 = -0.0004$ | $\sigma_{as} = 0.1292$ |
|--------------------|-------------------|--------------------|------------------------|

Table 4: Claims Development

| Stochastic Claims | | |
|-------------------|------------------|------------------|
| Germany | $\mu_C = -0.005$ | $\sigma_C = 0.1$ |
| France | $\mu_C = -0.005$ | $\sigma_C = 0.1$ |
| Italy | $\mu_C = -0.005$ | $\sigma_C = 0.1$ |
| Netherlands | $\mu_C = -0.005$ | $\sigma_C = 0.1$ |
| Spain | $\mu_C = -0.005$ | $\sigma_C = 0.1$ |

Table 5: Asset Portfolio Composition: (1) reports the main asset classes weight in the total asset portfolio, (2) reports the relative weight of each sub-portfolio within the main asset class, (3) reports the relative weight of each sub-portfolio within the total asset portfolio.

| | Germany | | | France | | | Italy | | | Netherlands | | | Spain | | |
|------------------------|---------|-------|-------|--------|-------|-------|-------|------|------|-------------|-------|-------|-------|-------|-------|
| | (1) | (2) | (3) | (1) | (2) | (3) | (1) | (2) | (3) | (1) | (2) | (3) | (1) | (2) | (3) |
| Sovereign Bonds | DE | 73.0% | 41.4% | 11.2% | 4.2% | 4.2% | 0.7% | 0.4% | 0.4% | 17.1% | 9.8% | 9.8% | 7.6% | 4.6% | 4.6% |
| | FR | 6.8% | 3.8% | 55.2% | 20.6% | 0.7% | 0.7% | 0.4% | 0.4% | 17.1% | 9.8% | 9.8% | 7.6% | 4.6% | 4.6% |
| | NL | 6.8% | 3.8% | 37.2% | 4.2% | 61.6% | 0.7% | 0.4% | 0.4% | 57.1% | 18.0% | 18.0% | 7.6% | 4.6% | 4.6% |
| | IT | 6.8% | 3.8% | 11.2% | 4.2% | 97.4% | 60.0% | 0.4% | 0.4% | 17.1% | 9.8% | 9.8% | 7.6% | 4.6% | 4.6% |
| | ES | 6.8% | 3.8% | 11.2% | 4.2% | 0.7% | 0.4% | 0.4% | 0.4% | 17.1% | 9.8% | 9.8% | 69.5% | 42.0% | 42.0% |
| Corporate Bonds | AAA | 23.6% | 8.1% | 23.6% | 11.3% | 6.5% | 23.6% | 6.5% | 6.3% | 23.6% | 6.3% | 6.3% | 23.6% | 7.5% | 7.5% |
| | AA | 16.9% | 5.8% | 16.9% | 8.1% | 16.9% | 4.6% | 4.6% | 4.5% | 16.9% | 4.5% | 4.5% | 16.9% | 5.3% | 5.3% |
| | A | 34.3% | 11.6% | 48.1% | 16.2% | 27.4% | 33.7% | 9.2% | 9.2% | 26.8% | 9.0% | 9.0% | 33.7% | 10.7% | 10.7% |
| | BBB | 25.8% | 8.9% | 25.8% | 12.4% | 25.8% | 7.1% | 7.1% | 6.9% | 25.8% | 6.9% | 6.9% | 25.8% | 8.2% | 8.2% |
| Stocks | DE | 60.0% | 3.4% | 10.0% | 1.1% | 1.1% | 10.0% | 1.0% | 1.0% | 60.0% | 9.2% | 9.2% | 10.0% | 0.3% | 0.3% |
| | FR | 10.0% | 0.6% | 60.0% | 6.7% | 10.0% | 10.0% | 1.0% | 1.0% | 10.0% | 1.5% | 1.5% | 10.0% | 0.3% | 0.3% |
| | NL | 10.0% | 0.6% | 11.2% | 1.1% | 9.5% | 10.0% | 1.0% | 1.0% | 15.3% | 1.5% | 1.5% | 10.0% | 0.3% | 0.3% |
| | IT | 10.0% | 0.6% | 10.0% | 1.1% | 60.0% | 5.7% | 5.7% | 5.7% | 10.0% | 1.5% | 1.5% | 10.0% | 0.3% | 0.3% |
| | ES | 10.0% | 0.6% | 10.0% | 1.1% | 10.0% | 1.0% | 1.0% | 1.0% | 10.0% | 1.5% | 1.5% | 60.0% | 1.8% | 1.8% |
| Real Estate | DE | 60.0% | 2.0% | 10.0% | 0.4% | 0.4% | 10.0% | 0.2% | 0.2% | 60.0% | 0.5% | 0.5% | 10.0% | 0.5% | 0.5% |
| | FR | 10.0% | 0.3% | 60.0% | 2.1% | 10.0% | 10.0% | 0.2% | 0.2% | 10.0% | 0.1% | 0.1% | 10.0% | 0.5% | 0.5% |
| | NL | 10.0% | 0.3% | 3.5% | 0.4% | 1.5% | 10.0% | 0.2% | 0.2% | 0.8% | 0.1% | 0.1% | 10.0% | 0.5% | 0.5% |
| | IT | 10.0% | 0.3% | 10.0% | 0.4% | 60.0% | 0.9% | 0.9% | 0.9% | 10.0% | 0.1% | 0.1% | 10.0% | 0.5% | 0.5% |
| | ES | 10.0% | 0.3% | 10.0% | 0.4% | 10.0% | 0.2% | 0.2% | 0.2% | 10.0% | 0.1% | 0.1% | 60.0% | 2.9% | 2.9% |

Table 6: Guarantees in (Endowment) Life Business Portfolio: data for Germany is based on Assekurata surveys, data for France is taken from *Moody's Investors Service - insurance sector in depth (26/3/2015)*, data for Italy and Spain were implied by taking the 60% of the past 10 YTM sovereign yield in the respective countries and rounded to 25 bps, whereas for the Netherlands we relied to insurance experts of the Dutch Central Bank.

| Germany | | France | | Italy | | Netherlands | | Spain | |
|-------------|--------------|--------------|--------|--------------|--------|--------------|--------|--------------|--------|
| r^i | weight | r^i | weight | r^i | weight | r^i | weight | r^i | weight |
| 4.00% | 24% | 3.50% | 15% | 3.50% | 6.70% | 4.00% | 40% | 5.00% | 10% |
| 3.50% | 18% | 3.00% | 5% | 3.25% | 6.70% | 3.00% | 40% | 4.00% | 5% |
| 3.25% | 14% | 2.50% | 5% | 3.00% | 13.3% | 0.00% | 20% | 3.50% | 15% |
| 2.75% | 12% | 0.00% | 75% | 2.75% | 20.0% | | | 3.00% | 35% |
| 2.25% | 20% | | | 2.50% | 33.3% | | | 2.50% | 25% |
| 1.75% | 12% | | | 2.25% | 13.3% | | | 2.00% | 10% |
| | | | | 2.00% | 6.70% | | | | |
| avg. | 3.04% | 0.80% | | 2.67% | | 2.80% | | 3.10% | |

Table 7: (mod.) Duration of Assets and Liabilities in (Endowment) Life Business: on the asset side, figures only include bonds, whereas on the liability side it only includes endowment/annuity business; numbers are expressed in years.

| Germany | | France | | Italy | | Netherlands | | Spain | |
|-------------|-------------|-------------|-------|-------------|-------|-------------|-------|-------------|-------|
| D^A | D^L | D^A | D^L | D^A | D^L | D^A | D^L | D^A | D^L |
| 7.93 | 11.43 | 7.12 | 9.68 | 6.81 | 7.44 | 7.97 | 11.46 | 8.04 | 9.47 |
| $D^L - D^A$ | 3.51 | 2.56 | | 0.64 | | 3.50 | | 1.43 | |

Table 8: Model's Specifications

| | Specifications | | | |
|---------------------------|------------------------|-----------------------|-----------------------|---|
| | (1) | (2) | (3) | (4) |
| Endowment Business | Yes | Yes | Yes | Yes |
| | $\omega^{e/a} = 100\%$ | $\omega^{e/a} = 95\%$ | $\omega^{e/a} = 95\%$ | $\omega^{e/a} = 95\%$ |
| Term Life Business | No | Yes | Yes | Yes |
| | $\omega^{tl} = 0\%$ | $\omega^{tl} = 5\%$ | $\omega^{tl} = 5\%$ | $\omega^{tl} = 5\%$ |
| Annuity Business | No | No | Yes | Yes |
| | $\theta^a = 0\%$ | $\theta^a = 0\%$ | $\theta^a = 5\%$ | $\theta^a = 5\%$ |
| Non-Life Business | No | No | No | Yes |
| | $\omega^{nl} = 0\%$ | $\omega^{nl} = 0\%$ | $\omega^{nl} = 0\%$ | $\omega^{nl} = \text{country specific}$ |

Table 9: Other Balance Sheet Parameters

| Balance Sheet Parameters | | Germany | France | Italy | Netherlands | Spain |
|-------------------------------|------------------------------------|--------------|--------------|--------------|--------------|--------------|
| Life | description | | | | | |
| $\omega^{e/a}$ * | share of L^l allocated to e/a | 100% - 95% | 100% - 95% | 100% - 95% | 100% - 95% | 100% - 95% |
| ω^{tl} * | share of L^l allocated to tl | 0% - 5% | 0% - 5% | 0% - 5% | 0% - 5% | 0% - 5% |
| θ^a * | share of $\omega^{e/a}$ annuitized | 0% - 5% | 0% - 5% | 0% - 5% | 0% - 5% | 0% - 5% |
| ω^l * | share of L allocated to l | 100% - 87.1% | 100% - 90.3% | 100% - 87.8% | 100% - 81.4% | 100% - 85.6% |
| $N^{l,e}$ | nr. of cohorts e/a | 25 | 20 | 15 | 25 | 20 |
| $N^{l,tl}$ | nr. of cohorts tl | 15 | 15 | 15 | 15 | 15 |
| $T^{l,e/a}$ | exp. time to maturity for e/a | 25 | 20 | 15 | 25 | 20 |
| $T^{l,tl}$ | exp. time to maturity for tl | 15 | 15 | 15 | 15 | 15 |
| mw | money's worth ratio | 0.98 | 0.98 | 0.98 | 0.98 | 0.98 |
| $\varrho^{e/a}$ | loading for mortality for e/a | -18.7% | -18.7% | -18.7% | -18.7% | -18.7% |
| ϱ^{tl} | loading for mortality for tl | +34% | +34% | +34% | +34% | +34% |
| ϱ^l | loading factor for premiums | 1% | 1% | 1% | 1% | 1% |
| $\pi^{e/a}$ | premium | 10 | 10 | 10 | 10 | 10 |
| π^{tl} | premium | 1 | 1 | 1 | 1 | 1 |
| ϑ | recovery value | 99% | 99% | 99% | 99% | 99% |
| v^a | minimum share of r^a | 90% | 85% | 80% | 0% | 80% |
| v^q | minimum return on r^q | 90% | 90% | 0% | 0% | 0% |
| $rm^{e/a}$ | risk margin for e/a | 1.83% | 1.83% | 1.83% | 1.83% | 1.83% |
| rm^{tl} | risk margin for tl | 8.24% | 8.24% | 8.24% | 8.24% | 8.24% |
| Non-Life | | | | | | |
| ω^{nl} * | share of L allocated to nl | 0% - 12.9% | 0% - 9.7% | 0% - 12.2% | 0% - 18.6% | 0% - 14.4% |
| ϱ^{nl} | loading factor | 5% | 5% | 5% | 5% | 5% |
| π^{nl} | premium | 2 | 2 | 2 | 2 | 2 |
| rm^{nl} | risk margin | 6.39% | 6.39% | 6.39% | 6.39% | 6.39% |
| Other | | | | | | |
| r_{target}^{sh} | dividend payout target | 7% | 7% | 7% | 7% | 7% |
| $\frac{OF_0}{SCR_0}$ | solvency ratio | 165% | 165% | 165% | 165% | 165% |
| Mortality Developments | | | | | | |
| x (years) | | 40 | 40 | 40 | 40 | 40 |
| ω (years) | | 105 | 105 | 105 | 105 | 105 |
| Simulations | | | | | | |
| I^f | iterations for financial markets | 1000 | 1000 | 1000 | 1000 | 1000 |
| I^m | iterations for mortality | 1000 | 1000 | 1000 | 1000 | 1000 |

*: depending on the specification

Table 10: Main results of the scenario analysis conducted in the paper reported as averages over the 10 years horizon; 3 main variables are taken into consideration for each country and balance sheet composition: i) the return on assets computed at book values (ROA), ii) the return on equity measured as the ratio of the dividends paid out over the amount of own funds (ROE) and iii) the solvency ratio (SR).

| | Baseline Scenario | | | Adverse Scenario | | | Severely Adverse Scenario | | |
|--|-------------------|-----|-------|------------------|-----|-------|---------------------------|-----|-------|
| | ROA | ROE | SR | ROA | ROE | SR | ROA | ROE | SR |
| Endowment business | | | | | | | | | |
| Germany | 2.7 | 1.2 | 51.7 | 2.5 | 0.6 | 35.2 | 2.5 | 0.6 | 35.2 |
| France | 2.7 | 3.9 | 105.6 | 2.7 | 3.2 | 98.7 | 2.7 | 2.8 | 88.7 |
| Italy | 4.1 | 6.9 | 150.4 | 4.1 | 6.9 | 155.3 | 4.1 | 5.3 | 127.1 |
| Netherlands | 2.9 | 3.6 | 102.8 | 2.9 | 4.3 | 104.5 | 2.9 | 2.4 | 96.2 |
| Spain | 3.2 | 3.5 | 97.9 | 3.2 | 3.4 | 107.5 | 3.2 | 2.0 | 73.2 |
| Endowment and term life business | | | | | | | | | |
| Germany | 3.0 | 4.7 | 110.2 | 3.0 | 3.5 | 102.9 | 3.0 | 3.5 | 103.0 |
| France | 2.8 | 6.7 | 152.5 | 2.7 | 6.8 | 144.9 | 2.7 | 6.2 | 132.2 |
| Italy | 4.1 | 6.9 | 214.4 | 4.1 | 6.9 | 220.8 | 4.1 | 6.8 | 188.4 |
| Netherlands | 2.9 | 6.9 | 158.1 | 2.9 | 6.9 | 156.4 | 2.9 | 6.9 | 140.7 |
| Spain | 3.2 | 6.5 | 156.9 | 3.2 | 6.9 | 170.1 | 3.2 | 4.7 | 120.0 |
| Endowment, term life and annuity business | | | | | | | | | |
| Germany | 3.0 | 6.9 | 149.2 | 3.0 | 6.8 | 126.7 | 3.0 | 6.8 | 126.7 |
| France | 2.8 | 6.9 | 179.8 | 2.7 | 6.9 | 171.5 | 2.7 | 6.9 | 158.4 |
| Italy | 4.1 | 6.9 | 251.6 | 4.1 | 6.9 | 255.4 | 4.1 | 6.9 | 222.3 |
| Netherlands | 2.9 | 6.9 | 182.0 | 2.9 | 6.9 | 176.0 | 2.9 | 6.9 | 161.7 |
| Spain | 3.2 | 6.9 | 202.6 | 3.2 | 6.9 | 211.9 | 3.2 | 5.9 | 157.3 |
| Endowment, term life, annuity and non-life business | | | | | | | | | |
| Life business | | | | | | | | | |
| Germany | 3.0 | 6.9 | 149.0 | 3.0 | 6.8 | 126.3 | 3.0 | 5.9 | 117.7 |
| France | 2.8 | 6.9 | 180.2 | 2.7 | 6.9 | 172.0 | 2.7 | 6.9 | 158.7 |
| Italy | 4.1 | 6.9 | 251.9 | 4.1 | 6.9 | 255.8 | 4.1 | 6.9 | 222.9 |
| Netherlands | 2.9 | 6.9 | 182.0 | 2.9 | 6.9 | 175.9 | 2.9 | 6.9 | 161.5 |
| Spain | 3.2 | 6.9 | 202.6 | 3.2 | 6.9 | 211.7 | 3.2 | 6.1 | 163.2 |
| Non-life business | | | | | | | | | |
| Germany | 1.3 | 6.8 | 220.3 | 0.5 | 6.7 | 208.5 | 0.7 | 6.7 | 207.5 |
| France | 1.5 | 6.8 | 225.0 | 0.7 | 6.8 | 208.3 | 1.0 | 6.8 | 216.7 |
| Italy | 1.3 | 6.8 | 225.3 | 0.6 | 6.7 | 206.4 | 1.2 | 6.8 | 217.1 |
| Netherlands | 1.3 | 6.8 | 223.0 | 0.5 | 6.7 | 203.1 | 0.8 | 6.7 | 209.7 |
| Spain | 1.3 | 6.8 | 221.5 | 0.6 | 6.7 | 209.9 | 1.1 | 6.6 | 204.7 |

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